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AP

COMPUTER SCIENCE A

7TH EDITION

Roselyn Teukolsky, M.S.
Formerly, Ithaca High School
Ithaca, New York

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As you review the content in this book to work toward earning that 5 on your AP Computer Science A exam, here are five things that you MUST know above everything else:

1. **The Basics.** Every AP exam question uses at least one of these:
   - Types and Identifiers (p. 60)
   - Operators (p. 63)
   - Control structures (p. 69)

2. **Objects, Classes, and Inheritance.** You may have to write your own class. You’ll definitely need to interpret at least one class that’s given.
   - Methods (p. 95)
   - Subclasses (p. 131)
   - Abstract classes (p. 142)
   - Interfaces (p. 144)

3. **Lists and Arrays.** Learn to manipulate a list. Search, delete an item, insert an item. It seems as if every second question on the AP exam uses a list!
   - One-dimensional arrays (p. 233)
   - ArrayLists (p. 244)

4. **Two-dimensional Arrays.** Learn to manipulate a matrix. This topic has become more prominent on the AP exam in recent years.
   - Two-dimensional arrays (p. 249)
   - Row-column traversal (p. 251)
   - for-each loop traversal (p. 251)
   - Row-by-row array processing (p. 251)

5. **Sorting and Searching.** Know these algorithms!
   - Selection Sort (p. 324)
   - Insertion Sort (p. 325)
   - Merge Sort (p. 325)
   - Binary Search (p. 329)
This book is aimed at students reviewing for the AP Computer Science A exam. It would normally be used at the completion of an AP course. However, it contains a complete summary of all topics for the exam, and it can be used for self-study if accompanied by a suitable textbook.

The book provides a review of object-oriented programming, algorithm analysis, and data structures. It can therefore be used as a supplement to first-year college courses where Java is the programming language and as a resource for teachers of high school and introductory college courses.

This seventh edition includes all features of Java that will be tested on the AP exam. The AP Computer Science Development Committee is placing greater emphasis on two-dimensional arrays. As a result, the following new sections have been added:

- using a for-each loop traversal
- treating a matrix as an array of arrays

All students should be able to create, initialize, modify, and traverse two-dimensional arrays. More questions on two-dimensional arrays have been added for this edition.

The GridWorld Case Study is gone! Starting in May 2015 there will be no questions on GridWorld. All GridWorld questions in the practice exams have been replaced by new questions, both multiple-choice and free-response.

The AP Computer Science Labs were developed as a replacement for GridWorld. However, there will be no questions on the specific content of the labs on the AP exam. Instead, there will be questions that test the concepts developed in the labs.

This seventh edition has a new chapter that summarizes the labs and highlights the concepts that are emphasized in them. The chapter contains a new section of multiple-choice questions based on these concepts. A new symbol in the margin, as shown here, is used throughout the book to draw attention to these concepts.

Another topic that is gone is the Comparable interface, which will no longer be tested on the AP exam. Students will, however, be expected to understand how the compareTo method is used for type String.

The style of all questions and examples in the book has been revamped to better reflect the style of recent exams.

There are three complete practice exams. The exams follow the format of the AP exam, with multiple-choice and free-response sections. One exam is presented after the introduction to the book for possible use as a diagnostic test. A diagnostic chart accompanies this test. Detailed solutions with explanations are provided for all exams. Two additional exams are provided on the optional CD-ROM. This edition contains several new questions. There is no overlap of questions between the exams.

Note that the scoring worksheets that accompany each exam, in both the book and CD-ROM, have been updated in this edition. They reflect the new College Board policy of not penalizing students for wrong answers on the multiple-choice section.
ACKNOWLEDGMENTS

I owe thanks to many people who helped in the creation of this book.

I am most grateful to my excellent editor, Linda Turner, of Barron’s, for her friendly guidance and moral support throughout this project, over many years. I also thank all the other members of the Barron’s staff who worked on the production of the book.

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A very special thank you to Judy Hromcik and Chris Nevison, who went way beyond the call of duty to help me with this new edition.

My husband, Saul, continues to be my partner in this project—typesetting the manuscript, producing the figures, and giving advice and moral support every step of the way. This book is dedicated to him.

Roselyn Teukolsky
Ithaca, NY
July 2014
Introduction

Computer Science: The boring art
of coping with a large number of trivialities.

GENERAL INFORMATION ABOUT THE EXAM

The AP Computer Science exam is a three-hour written exam. No books, calculators, or computers are allowed! The exam consists of two parts that have equal weight:

- Section I: 40 multiple-choice questions in 1 hour and 15 minutes.
- Section II: 4 free-response questions in 1 hour and 45 minutes.

Section I is scored by machine—you will bubble your answers with a pencil on a mark-sense sheet. Each question correctly answered is worth 1 point. There are no deductions for incorrect answers, and a question left blank is ignored.

Section II is scored by human readers—you will write your answers in a booklet provided. Free-response questions typically involve writing methods in Java to solve a given problem. Sometimes there are questions analyzing algorithms or designing and modifying data structures. You may be asked to write or design an entire class. To ensure consistency in the grading, each grader follows the same rubric, and each of your four answers may be examined by more than one reader. Each question is worth 9 points, with partial credit awarded where applicable. Your name and school are hidden from the readers.

Your raw score for both sections is converted to an integer score from 1 to 5, where 1 represents “Not at all qualified” and 5 represents “Extremely well qualified.” Be aware that the awarding of AP credit varies enormously from college to college. The exam covers roughly a one-semester introductory college course.

The language of the AP exam is Java. Only a subset of the Java language will be tested on the exam. In writing your solutions to the free-response questions, however, you may use any Java features, including those that are not in the AP subset. For a complete description of this subset, see the College Board website at http://www.collegeboard.com/student/testing/ap/subjects.html. Every language topic in this review book is part of the AP Java subset unless explicitly stated otherwise. Note that the entire subset is covered in the book.

For both the multiple-choice and free-response sections of the exam, there will be a quick reference in the appendix. You can look at this ahead of time at http://apcentral.collegeboard.com/apc/public/repository/ap_comp_sci_a_quick_reference.pdf.

The quick reference contains The standard Java interfaces and classes with lists of their required methods.
HINTS FOR TAKING THE EXAM

The Multiple-Choice Section

• Since there are no deductions for wrong answers, you should guess when you’ve eliminated what you can.
• You have a little less than two minutes per question, so don’t waste time on any given question. You can always come back to it if you have time at the end.
• Seemingly complicated array questions can often be solved by hand tracing the code with a small array of two or three elements. The same is true for matrices.
• Many questions ask you to compare two pieces of code that supposedly implement the same algorithm. Often one program segment will fail because it doesn’t handle endpoint conditions properly (e.g., `num == 0`). Be aware of endpoint conditions throughout the exam.
• Since the mark-sense sheet is scanned by machine, make sure that you erase completely if you change an answer.

The Free-Response Section

• Each free-response question is worth 9 points. Take a minute to read through the whole exam so that you can start with a question that you feel confident about. It gives you a psychological leg up to have a solid question in the bag.
• Don’t omit a question just because you can’t come up with a complete solution. Remember, partial credit is awarded. Also, if you can’t do part (a) of a question, don’t omit part (b)—they are graded independently.
• In writing solutions to a question, you must use the public methods of classes provided in that question wherever possible. If you write a significant chunk of code that can be replaced by a call to one of these methods, you will probably not receive full credit for the question.
• If an algorithm is suggested to solve a problem, just follow it. Don’t reinvent the wheel.
• Don’t waste time writing comments: the graders generally ignore them. The occasional brief comment that clarifies a segment of code is OK.
• Points are not deducted for inefficient code unless efficiency is an issue in the question.
• Most of the standard Java library methods are not included in the AP subset. They are accepted on the exam if you use them correctly. However, there is always an alternative solution that uses the AP subset and you should try to find it.
• Don’t cross out an answer until you have written a replacement. Graders are instructed not to read anything crossed out, even if it would have gotten credit.
• Have some awareness that this section is graded by humans. It is in your interest to have the graders understand your solutions. With this in mind,
  - Use a sharp pencil, write legibly, space your answers, and indent correctly.
  - Use self-documenting names for variables, methods, and so on.
- Use the identifiers that are given in a question. You will lose usage points if you persist in using the wrong names.
- Write clear readable code. This is your goal. Don’t write one obscure convoluted statement when you can write two short clear statements. The APCS exam is not the place to demonstrate that you’re a genius.

**HOW TO USE THIS BOOK**

Each chapter in the book contains a comprehensive review of a topic, multiple-choice questions that focus on the topic, and detailed explanations of answers. These focus questions help you to review parts of the Java subset that you should know. A few questions are not typical AP exam questions—for example, questions that test low-level details of syntax. Most of the focus questions, however, and all the multiple-choice questions in the practice exams are representative of actual exam questions.

You should also note that several groups of focus questions are preceded by a single piece of code to which the questions refer. Be aware that the AP exam will usually restrict the number of questions per code example to two.

In both the text and questions/explanations, a special code font is used for parts of the text that are Java code.

```
//This is an example of code font
```

A different font is used for pseudo-code.

```
< Here is pseudo-code font. >
```

A small number of optional topics that are not part of the AP Java subset are included in the book because they are useful in the free-response questions. Sections in the text and multiple-choice questions that are optional topics are clearly marked as such. Some sections are marked by a lightning bolt, as shown here in the margin. This means wake up! Here is a concept that is likely to be tested on the AP exam because it was emphasized in the new AP Computer Science labs.

Three complete practice exams are provided in the book. One exam is at the start of the book and may be used as a diagnostic test. It is accompanied by a diagnostic chart that refers you to related topics in the review book. The other two exams are at the end of the book. There are two additional exams on the optional CD-ROM provided with the book.

Each of the five exams has an answer key, complete solutions and explanations for the free-response questions, and detailed explanations for the multiple-choice questions. There is no overlap in the questions.

An answer sheet is provided for the Section I questions of each exam. When you have completed an entire exam, and have checked your answers, you may wish to calculate your approximate AP score. Use the scoring worksheet provided on the back of the answer sheet.

An appendix at the end of the book provides a glossary of computer terms that occasionally crop up on the exam.

A final hint about the book: Try the questions before you peek at the answers. Good luck!
PRACTICE EXAM ONE / DIAGNOSTIC TEST

The exam that follows has the same format as that used on the actual AP exam. There are two ways you may use it:

1. As a diagnostic test before you start reviewing. Following the answer key is a diagnostic chart that relates each question to sections that you should review. In addition, complete explanations are provided for each solution.

2. As a practice exam when you have completed your review. Complete solutions with explanations are provided for the free-response questions.
### Answer Sheet: Practice Exam One

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<tr>
<td>40</td>
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</tbody>
</table>
How to Calculate Your (Approximate) AP Computer Science Score

**Multiple Choice**

Number correct (out of 40) = \[ \text{Multiple-Choice Score} \]

**Free Response**

<table>
<thead>
<tr>
<th>Question</th>
<th>Score (out of 9)</th>
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<tr>
<td>3</td>
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</table>

Total \( \times 1.11 = \text{Free-Response Score} \) (Do not round.)

**Final Score**

\[ \text{Multiple-Choice Score} + \text{Free-Response Score} = \text{Final Score} \]

(round to nearest whole number)

**Chart to Convert to AP Grade**

<table>
<thead>
<tr>
<th>Score Range</th>
<th>AP Grade*</th>
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<tbody>
<tr>
<td>62–80</td>
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<td>47–61</td>
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<tr>
<td>37–46</td>
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<td>29–36</td>
<td>2</td>
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*The score range corresponding to each grade varies from exam to exam and is approximate.
Practice Exam One

COMPUTER SCIENCE

SECTION I

Time—1 hour and 15 minutes
Number of questions—40
Percent of total grade—50

Directions: Determine the answer to each of the following questions or incomplete statements, using the available space for any necessary scratchwork. Then decide which is the best of the choices given and fill in the corresponding oval on the answer sheet. Do not spend too much time on any one problem.

Notes:
• Assume that the classes in the Quick Reference have been imported where needed.
• Assume that variables and methods are declared within the context of an enclosing class.
• Assume that method calls that have no object or class name prefixed, and that are not shown within a complete class definition, appear within the context of an enclosing class.
• Assume that parameters in method calls are not null unless otherwise stated.
6 Practice Exam

1. Consider this inheritance hierarchy, in which Novel and Textbook are subclasses of Book.

Which of the following is a false statement about the classes shown?
(A) The Textbook class can have private instance variables that are in neither Book nor Novel.
(B) Each of the classes—Book, Novel, and Textbook—can have a method computeShelfLife, whose code in Book and Novel is identical, but different from the code in Textbook.
(C) If the Book class has private instance variables title and author, then Novel and Textbook cannot directly access them.
(D) Both Novel and Textbook inherit the constructors in Book.
(E) If the Book class has a private method called readFile, this method may not be accessed in either the Novel or Textbook classes.
2. A programmer is designing a program to catalog all books in a library. He plans to have a `Book` class that stores features of each book: `author`, `title`, `isOnShelf`, and so on, with operations like `getAuthor`, `getTitle`, `getShelfInfo`, and `setShelfInfo`. Another class, `LibraryList`, will store an array of `Book` objects. The `LibraryList` class will include operations such as `listAllBooks`, `addBook`, `removeBook`, and `searchForBook`. The programmer plans to implement and test the `Book` class first, before implementing the `LibraryList` class. The programmer's plan to write the `Book` class first is an example of
(A) top-down development.
(B) bottom-up development.
(C) procedural abstraction.
(D) information hiding.
(E) a driver program.

3. The color of a pixel can be represented using the RGB (Red, Green, Blue) color model, which stores values for red, green, and blue, each ranging from 0 to 255. How many bits (binary digits) would be needed to represent a color in the RGB model?
(A) 8
(B) 16
(C) 24
(D) 32
(E) 40
Questions 4–5 refer to the Card and Deck classes shown below.

```java
public class Card {
    private String suit;
    private int value; // 0 to 12

    public Card(String cardSuit, int cardValue)
    { /* implementation */ }

    public String getSuit()
    { return suit; }

    public int getValue()
    { return value; }

    public String toString()
    { String faceValue = "";
      if (value == 11)
        faceValue = "J";
      else if (value == 12)
        faceValue = "Q";
      else if (value == 0)
        faceValue = "K";
      else if (value == 1)
        faceValue = "A";
      if (value >= 2 && value <= 10)
        return value + " of " + suit;
      else
        return faceValue + " of " + suit;
    }
}

global class Deck {
    private Card[] deck;
    public final static int NUMCARDS = 52;

    public Deck()
    { ... }

    /** Simulate shuffling the deck. */
    public void shuffle()
    { ... }

    // Other methods are not shown.
}
```

Go on to the next page.
4. Which of the following represents correct /* implementation */ code for the constructor in the Card class?

(A) suit = cardSuit;
    value = cardValue;

(B) cardSuit = suit;
    cardValue = value;

(C) Card = new Card(suit, value);

(D) Card = new Card(cardSuit, cardValue);

(E) suit = getSuit();
    value = getValue();

5. Consider the implementation of a writeDeck method that is added to the Deck class.

/** Write the cards in deck, one per line. */
public void writeDeck()
{
    /* implementation code */
}

Which of the following is correct /* implementation code */?

I System.out.println(deck);
II for (Card card : deck)
    System.out.println(card);
III for (Card card : deck)
    System.out.println((String) card);

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) II and III only

GO ON TO THE NEXT PAGE.
6. Refer to the following method that finds the smallest value in an array.

```java
/** Precondition: arr is initialized with int values.
 * @param arr the array to be processed
 * @return the smallest value in arr
 */
public static int findMin(int[] arr)
{
    int min = /* some value */;
    int index = 0;
    while (index < arr.length)
    {
        if (arr[index] < min)
            min = arr[index];
        index++;
    }
    return min;
}
```

Which replacement(s) for /* some value */ will always result in correct execution of the `findMin` method?

I Integer.MIN_VALUE
II Integer.MAX_VALUE
III arr[0]

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) II and III only

GO ON TO THE NEXT PAGE.
7. Consider the following loop, where $n$ is some positive integer.

```java
for (int i = 0; i < n; i += 2)
{
    if (/* test */)
        /* perform some action */
}
```

In terms of $n$, which Java expression represents the maximum number of times that /* perform some action */ could be executed?
(A) $n / 2$
(B) $(n + 1) / 2$
(C) $n$
(D) $n - 1$
(E) $(n - 1) / 2$

8. A method is to be written to search an array for a value that is larger than a given item and return its index. The problem specification does not indicate what should be returned if there are several such values in the array. Which of the following actions would be best?
(A) The method should be written on the assumption that there is only one value in the array that is larger than the given item.
(B) The method should be written to return the index of every occurrence of a larger value.
(C) The specification should be modified to indicate what should be done if there is more than one index of larger values.
(D) The method should be written to output a message if more than one larger value is found.
(E) The method should be written to delete all subsequent larger items after a suitable index is returned.
9. When will method `whatIsIt` cause a stack overflow (i.e., cause computer memory to be exhausted)?

```java
public static int whatIsIt(int x, int y)
{
    if (x > y)
        return x * y;
    else
        return whatIsIt(x - 1, y);
}
```

(A) Only when \( x < y \)
(B) Only when \( x \leq y \)
(C) Only when \( x > y \)
(D) For all values of \( x \) and \( y \)
(E) The method will never cause a stack overflow.

10. The boolean expression `a[i] == max || !(max != a[i])` can be simplified to

(A) `a[i] == max`
(B) `a[i] != max`
(C) `a[i] < max || a[i] > max`
(D) `true`
(E) `false`

11. Suppose the characters 0, 1, ..., 8, 9, A, B, C, D, E, F are used to represent a hexadecimal (base-16) number. Here A = 10, B = 11, ..., F = 15. What is the largest base-10 integer that can be represented with a two-digit hexadecimal number, such as 14 or 3A?

(A) 32
(B) 225
(C) 255
(D) 256
(E) 272

12. Consider a Clown class that has a default constructor. Suppose a list `ArrayList<Clown> list` is initialized. Which of the following will not cause an `IndexOutOfBoundsException` to be thrown?

(A) `for (int i = 0; i <= list.size(); i++)
    list.set(i, new Clown());`
(B) `list.add(list.size(), new Clown());`
(C) `Clown c = list.get(list.size());`
(D) `Clown c = list.remove(list.size());`
(E) `list.add(-1, new Clown());`

GO ON TO THE NEXT PAGE.
Refer to the following class for Questions 13 and 14.

```java
public class Tester
{
    private int[] testArray = {3, 4, 5};

    /** @param n an int to be incremented by 1 */
    public void increment (int n)
    { n++; }

    public void firstTestMethod()
    {
        for (int i = 0; i < testArray.length; i++)
        {
            increment(testArray[i]);
            System.out.print(testArray[i] + " ");
        }
    }

    public void secondTestMethod()
    {
        for (int element : testArray)
        {
            increment(element);
            System.out.print(element + " ");
        }
    }
}
```

13. What output will be produced by invoking `firstTestMethod` for a `Tester` object?
   (A) 3 4 5
   (B) 4 5 6
   (C) 5 6 7
   (D) 0 0 0
   (E) No output will be produced. An `ArrayIndexOutOfBoundsException` will be thrown.

14. What output will be produced by invoking `secondTestMethod` for a `Tester` object, assuming that `testArray` contains 3, 4, 5?
   (A) 3 4 5
   (B) 4 5 6
   (C) 5 6 7
   (D) 0 0 0
   (E) No output will be produced. An `ArrayIndexOutOfBoundsException` will be thrown.
Questions 15–17 refer to the Point, Quadrilateral, and Rectangle classes below:

```java
public class Point {
    private int xCoord;
    private int yCoord;

    //constructor
    public Point(int x, int y) {
        ...}
    }

    //accessors
    public int get_x() {
        ...}
    }
    public int get_y() {
        ...}
    }

    //Other methods are not shown.
}

public abstract class Quadrilateral {
    private String labels;  //e.g., "ABCD"

    //constructor
    public Quadrilateral(String quadLabels) {
        labels = quadLabels; }
    }

    public String getLabels() {
        return labels; }

    public abstract int perimeter();
    public abstract int area();
}
```

GO ON TO THE NEXT PAGE.
public class Rectangle extends Quadrilateral {
    private Point topLeft; //coords of top left corner
    private Point botRight; //coords of bottom right corner

    //constructor
    public Rectangle(String theLabels, Point theTopLeft, Point theBotRight) {
        /* implementation code */
    }

    public int perimeter() {
        /* implementation not shown */
    }

    public int area() {
        /* implementation not shown */
    }

    //Other methods are not shown.
}

15. Which statement about the Quadrilateral class is false?
   (A) The perimeter and area methods are abstract because there’s no suitable
       default code for them.
   (B) The getLabels method is not abstract because any subclasses of
       Quadrilateral will have the same code for this method.
   (C) If the Quadrilateral class is used in a program, it must be used as a super-
       class for at least one other class.
   (D) No instances of a Quadrilateral object can be created in a program.
   (E) Any subclasses of the Quadrilateral class must provide implementation
       code for the perimeter and area methods.

16. Which represents correct /* implementation code */ for the Rectangle constructor?

    I super(theLabels);
    II super(theLabels, theTopLeft, theBotRight);
    III super(theLabels);
        topLeft = theTopLeft;
        botRight = theBotRight;

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) II and III only
17. Refer to the Parallelogram and Square classes below.

```java
public class Parallelogram extends Quadrilateral {
    //Private instance variables and constructor are not shown.
    ...

    public int perimeter()
    { /* implementation not shown */ }

    public int area()
    { /* implementation not shown */ }
}

public class Square extends Rectangle {
    //Private instance variables and constructor are not shown.
    ...

    public int perimeter()
    { /* implementation not shown */ }

    public int area()
    { /* implementation not shown */ }
}
```

Consider an ArrayList<Quadrilateral> quadList whose elements are of type Rectangle, Parallelogram, or Square. Refer to the following method, writeAreas:

```java
/** Precondition: quadList contains Rectangle, Parallelogram, or Square objects in an unspecified order.
 * @param quadList the list of quadrilaterals
 */
public static void writeAreas(List<Quadrilateral> quadList) {
    for (Quadrilateral quad : quadList)
        System.out.println("Area of " + quad.getLabels() + " is " + quad.area());
}
```

What is the effect of executing this method?
(A) The area of each Quadrilateral in quadList will be printed.
(B) A compile-time error will occur, stating that there is no area method in abstract class Quadrilateral.
(C) A compile-time error will occur, stating that there is no getLabels method in classes Rectangle, Parallelogram, or Square.
(D) A NullPointerException will be thrown.
(E) A ClassCastException will be thrown.

---

GO ON TO THE NEXT PAGE.
18. Refer to the `doSomething` method:

```java
// postcondition
public static void doSomething(List<SomeType> list, int i, int j)
{
    SomeType temp = list.get(i);
    list.set(i, list.get(j));
    list.set(j, temp);
}
```

Which best describes the `postcondition` for `doSomething`?
(A) Removes from `list` the objects indexed at `i` and `j`.
(B) Replaces in `list` the object indexed at `i` with the object indexed at `j`.
(C) Replaces in `list` the object indexed at `j` with the object indexed at `i`.
(D) Replaces in `list` the objects indexed at `i` and `j` with `temp`.
(E) Interchanges in `list` the objects indexed at `i` and `j`.

19. Consider the `NegativeReal` class below, which defines a negative real number object.

```java
public class NegativeReal
{
    private Double negReal;

    /** Constructor. Creates a NegativeReal object whose value is num. *
     * @param num a negative real number */
    public NegativeReal(double num)
    { /* implementation not shown */ }

    /** @return the value of this NegativeReal */
    public double getValue()
    { /* implementation not shown */ }

    /** @return this NegativeReal rounded to the nearest integer */
    public int getRounded()
    { /* implementation */ }
}
```

Here are some rounding examples:

<table>
<thead>
<tr>
<th>Negative real number</th>
<th>Rounded to nearest integer</th>
</tr>
</thead>
<tbody>
<tr>
<td>−3.5</td>
<td>−4</td>
</tr>
<tr>
<td>−8.97</td>
<td>−9</td>
</tr>
<tr>
<td>−5.0</td>
<td>−5</td>
</tr>
<tr>
<td>−2.487</td>
<td>−2</td>
</tr>
<tr>
<td>−0.2</td>
<td>0</td>
</tr>
</tbody>
</table>

Which /* implementation */ of `getRounded` produces the desired postcondition?
(A) return (int) (getValue() - 0.5);
(B) return (int) (getValue() + 0.5);
(C) return (int) getValue();
(D) return (double) (getValue() - 0.5);
(E) return (double) getValue();
20. Consider the following method.

```java
public static void whatsIt(int n)
{
    if (n > 10)
        whatsIt(n / 10);
    System.out.print(n % 10);
}
```

What will be output as a result of the method call `whatsIt(347)`?
(A) 74
(B) 47
(C) 734
(D) 743
(E) 347

21. A large list of numbers is to be sorted into ascending order. Assuming that a “data movement” is a swap or reassignment of an element, which of the following is a true statement?
(A) If the array is initially sorted in descending order, then insertion sort will be more efficient than selection sort.
(B) The number of comparisons for selection sort is independent of the initial arrangement of elements.
(C) The number of comparisons for insertion sort is independent of the initial arrangement of elements.
(D) The number of data movements in selection sort depends on the initial arrangement of elements.
(E) The number of data movements in insertion sort is independent of the initial arrangement of elements.
22. Refer to the definitions of ClassOne and ClassTwo below.

```java
public class ClassOne
{
    public void methodOne()
    {
        ...
    }

    // Other methods are not shown.
}

public class ClassTwo extends ClassOne
{
    public void methodTwo()
    {
        ...
    }

    // Other methods are not shown.
}
```

Consider the following declarations in a client class. You may assume that ClassOne and ClassTwo have default constructors.

```java
ClassOne c1 = new ClassOne();
ClassOne c2 = new ClassTwo();
```

Which of the following method calls will cause an error?

I  c1.methodTwo();
II c2.methodTwo();
III c2.methodOne();

(A) None  
(B) I only  
(C) II only  
(D) III only  
(E) I and II only

GO ON TO THE NEXT PAGE.
23. Consider the code segment

```java
if (n == 1)
    k++; 
else if (n == 4)
    k += 4;
```

Suppose that the given segment is rewritten in the form

```java
if (/* condition */) /* assignment statement */;
```

Given that n and k are integers and that the rewritten code performs the same task as the original code, which of the following could be used as

1) /* condition */ and 2) /* assignment statement */?

(A) (1) n == 1 && n == 4 (2) k += n
(B) (1) n == 1 && n == 4 (2) k += 4
(C) (1) n == 1 || n == 4 (2) k += 4
(D) (1) n == 1 || n == 4 (2) k += n
(E) (1) n == 1 || n == 4 (2) k = n - k

24. Which of the following will execute without throwing an exception?

I String s = null;
String t = "";
if (s.equals(t))
    System.out.println("empty strings?");

II String s = "holy";
String t = "moly";
if (s.equals(t))
    System.out.println("holy moly!");

III String s = "holy";
String t = s.substring(4);
System.out.println(s + t);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) II and III only
25. Three numbers \(a\), \(b\), and \(c\) are said to be a **Pythagorean Triple** if and only if the sum of the squares of two of the numbers equals the square of the third. A programmer writes a method `isPythTriple` to test if its three parameters form a Pythagorean Triple:

```java
public static boolean isPythTriple(double a, double b, double c) {
    double d = Math.sqrt(a * a + b * b);
    return d == c;
}
```

When the method was tested with known Pythagorean Triples, `isPythTriple` sometimes erroneously returned `false`. What was the most likely cause of the error?

(A) Round-off error was caused by calculations with floating-point numbers.
(B) Type `boolean` was not recognized by an obsolete version of Java.
(C) An overflow error was caused by entering numbers that were too large.
(D) \(c\) and \(d\) should have been cast to integers before testing for equality.
(E) Bad test data were selected.

26. Refer to the following class, containing the `mystery` method.

```java
public class SomeClass {
    private int[] arr;

    /** Constructor. Initializes arr to contain nonnegative * integers k such that 0 <= k <= 9. */
    public SomeClass() {
        /* implementation not shown */
    }

    public int mystery() {
        int value = arr[0];
        for (int i = 1; i < arr.length; i++)
            value = value * 10 + arr[i];
        return value;
    }
}
```

Which best describes what the `mystery` method does?

(A) It sums the elements of `arr`.
(B) It sums the products \(10*arr[0]+10*arr[1]++10*arr[arr.length-1]\).
(C) It builds an integer of the form \(d_1d_2d_3\ldots d_n\), where \(d_1 = arr[0]\), \(d_2 = arr[1]\ldots, d_n = arr[arr.length-1]\).
(D) It builds an integer of the form \(d_1d_2d_3\ldots d_n\), where \(d_1 = arr[arr.length-1], d_2 = arr[arr.length-2], \ldots, d_n = arr[0]\).
(E) It converts the elements of `arr` to base-10.

GO ON TO THE NEXT PAGE.
Questions 27 and 28 refer to the search method in the Searcher class below.

```java
public class Searcher {
    private int[] arr;

    /** Constructor. Initializes arr with integers. */
    public Searcher() {
        // implementation not shown
    }

    /**
     * Precondition: arr[first]...arr[last] sorted in ascending order.
     * Postcondition: Returns index of key in arr. If key not in arr,
     * returns -1.
     */
    public int search(int first, int last, int key) {
        int mid;
        while (first <= last) {
            mid = (first + last) / 2;
            if (arr[mid] == key) //found key, exit search
                return mid;
            else if (arr[mid] < key) //key to right of arr[mid]
                first = mid + 1;
            else //key to left of arr[mid]
                last = mid - 1;
        }
        return -1; //key not in list
    }
}
```

27. Which assertion is true just before each execution of the while loop?
   (A) arr[first] < key < arr[last]
   (B) arr[first] ≤ key ≤ arr[last]
   (C) arr[first] < key < arr[last] or key is not in arr
   (D) arr[first] ≤ key ≤ arr[last] or key is not in arr
   (E) key ≤ arr[first] or key ≥ arr[last] or key is not in arr

28. Consider the array a with values as shown:

    4, 7, 19, 25, 36, 37, 50, 100, 101, 205, 220, 271, 306, 321

where 4 is a[0] and 321 is a[13]. Suppose that the search method is called with
first = 0 and last = 13 to locate the key 205. How many iterations of the while
loop must be made in order to locate it?
   (A) 3
   (B) 4
   (C) 5
   (D) 10
   (E) 13

GO ON TO THE NEXT PAGE.
29. Consider the following RandomList class.

```java
public class RandomList {
    private int[] ranList;

    public RandomList() {
        ranList = getList();
    }

    /** @return array with random Integers from 0 to 100
     * inclusive */
    public int[] getList() {
        System.out.println("How many integers? ");
        int listLength = IO.readInt(); //read user input
        int[] list = new int[listLength];
        for (int i = 0; i < listLength; i++) {
            /* code to add integer to list */
        }
        return list;
    }

    /** Print all elements of this list. */
    public void printList() {
        ...
    }
}
```

Which represents correct /* code to add integer to list */?

(A) `list[i] = (int) (Math.random() * 101);`
(B) `list.add((int) (Math.random() * 101));`
(C) `list[i] = (int) (Math.random() * 100);`
(D) `list.add(new Integer(Math.random() * 100))`
(E) `list[i] = (int) (Math.random() * 100) + 1;`
30. Refer to method `insert` described here. The `insert` method has two string parameters and one integer parameter. The method returns the string obtained by inserting the second string into the first starting at the position indicated by the integer parameter `pos`. For example, if `str1` contains `xy` and `str2` contains `cat`, then

- `insert(str1, str2, 0)` returns `catxy`
- `insert(str1, str2, 1)` returns `xcaty`
- `insert(str1, str2, 2)` returns `xycat`

Method `insert` follows:

```java
public static String insert(String str1, String str2, int pos) {
    String first, last;
    /* more code */
    return first + str2 + last;
}
```

Which of the following is a correct replacement for `/* more code */`?

(A) `first = str1.substring(0, pos);
    last = str1.substring(pos);`

(B) `first = str1.substring(0, pos - 1);
    last = str1.substring(pos);`

(C) `first = str1.substring(0, pos + 1);
    last = str1.substring(pos + 1);`

(D) `first = str1.substring(0, pos);
    last = str1.substring(pos + 1, str1.length());`

(E) `first = str1.substring(0, pos);
    last = str1.substring(pos, str1.length() + 1);`

GO ON TO THE NEXT PAGE.
31. A matrix (two-dimensional array) is declared as

```java
int[][] mat = new int[2][3];
```

Consider the following method:

```java
public static void changeMatrix(int[][] mat)
{
    for (int r = 0; r < mat.length; r++)
        for (int c = 0; c < mat[r].length; c++)
            if (r == c)
                mat[r][c] = Math.abs(mat[r][c]);
}
```

If `mat` is initialized to be

```
-1 -2 -6
-2 -4  5
```

which matrix will be the result of a call to `changeMatrix(mat)`?

(A) `1 2 -6`
   `-2 4  5`

(B) `-1 2 -6`
   `2 -4  5`

(C) `-1 -2 -6`
   `-2 -4 -5`

(D) `1 2 -6`
   `2 4  5`

(E) `1 2  6`
   `2 4  5`
Diagnostic Test

Practice Exam

Use the following program description for Questions 32–34.

A programmer plans to write a program that simulates a small bingo game (no more than six players). Each player will have a bingo card with 20 numbers from 0 to 90 (no duplicates). Someone will call out numbers one at a time, and each player will cross out a number on his card as it is called. The first player with all the numbers crossed out is the winner. In the simulation, as the game is in progress, each player’s card is displayed on the screen.

The programmer envisions a short driver class whose main method has just two statements:

```java
BingoGame b = new BingoGame();
b.playBingo();
```

The BingoGame class will have several objects: a Display, a Caller, and a PlayerGroup. The PlayerGroup will have a list of Players, and each Player will have a BingoCard.

32. The relationship between the PlayerGroup and Player classes is an example of
   (A) an interface.
   (B) encapsulation.
   (C) composition.
   (D) inheritance.
   (E) independent classes.

33. Which is a reasonable data structure for a BingoCard object? Recall that there are 20 integers from 0 to 90 on a BingoCard, with no duplicates. There should also be mechanisms for crossing off numbers that are called, and for detecting a winning card (i.e., one where all the numbers have been crossed off).

   I int[] bingoCard; //will contain 20 integers
   //bingoCard[k] is crossed off by setting it to -1.
   int numCrossedOff; //player wins when numCrossedOff reaches 20.

   II boolean[] bingoCard; //will contain 91 boolean values, of which
   //20 are true. All the other values are false.
   //Thus, if bingoCard[k] is true, then k is
   //on the card, 0 <= k <= 90. A number k is
   //crossed off by changing the value of
   //bingoCard[k] to false.
   int numCrossedOff; //player wins when numCrossedOff reaches 20.

   III ArrayList<Integer> bingoCard; //will contain 20 integers.
   //A number is crossed off by removing it from the ArrayList.
   //Player wins when bingoCard.size() == 0.

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) I, II, and III

GO ON TO THE NEXT PAGE.
34. The programmer decides to use a `List<Integer>`, which is implemented as an `ArrayList<Integer>`, to store the numbers to be called by the `Caller`:

```java
public class Caller {
    private List<Integer> numbers;

    public Caller() {
        numbers = getList();
        shuffleNumbers();
    }

    /** @return the numbers 0...90 in order */
    private List<Integer> getList() {
        /* implementation not shown */
    }

    /** Shuffle the numbers. */
    private void shuffleNumbers() {
        /* implementation not shown */
    }
}
```

When the programmer tests the constructor of the `Caller` class, she gets a `NullPointerException`. Which could be the cause of this error?

(A) The `Caller` object in the driver class was not created with `new`.
(B) The programmer forgot the `return` statement in `getList` that returns the list of `Integer`s.
(C) The declaration of `numbers` is incorrect. It needed to be
    ```java
    private List<Integer> numbers = null;
    ```
(D) In the `getList` method, an attempt was made to add an `Integer` to an `ArrayList` that had not been created with `new`.
(E) The `shuffleNumbers` algorithm went out of range, causing a `null` `Integer` to be shuffled into the `ArrayList`.

GO ON TO THE NEXT PAGE.
35. Consider method `findSomething` below:

```java
/** Precondition: a.length is equal to b.length. */
public static boolean findSomething(int[] a, int[] b)
{
    for (int aValue: a)
    {
        boolean found = false;
        for (int bValue: b)
        {
            if (bValue == aValue)
                found = true;
        }
        if (!found)
            return false;
    }
    return true;
}
```

Which best describes what method `findSomething` does? Method `findSomething` returns `true` only if
(A) Arrays a and b contain identical elements in the same order.
(B) Arrays a and b contain identical elements in reverse order.
(C) Arrays a and b are permutations of each other.
(D) Array a contains at least one element that is also in b.
(E) Every element of array a is also in b, and every element of array b is also in a.
36. Consider a program that has a two-dimensional array `mat` of int values. The program has several methods that change `mat` by reflecting elements of `mat` across a mirror placed symmetrically on the matrix. Here are five such methods:

<table>
<thead>
<tr>
<th>Method</th>
<th>Transforms</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>mirrorVerticalLeftToRight</td>
<td>transforms</td>
<td>2 4 6 to 1 3 5</td>
</tr>
<tr>
<td></td>
<td>8 9 0</td>
<td>2 4 2</td>
</tr>
<tr>
<td>mirrorVerticalRightToLeft</td>
<td>transforms</td>
<td>2 4 6 to 1 3 5</td>
</tr>
<tr>
<td></td>
<td>8 9 0</td>
<td>6 4 6</td>
</tr>
<tr>
<td>mirrorHorizontalTopToBottom</td>
<td>transforms</td>
<td>2 4 6 to 1 3 5</td>
</tr>
<tr>
<td></td>
<td>8 9 0</td>
<td>2 4 6</td>
</tr>
<tr>
<td>mirrorHorizontalBottomToTop</td>
<td>transforms</td>
<td>2 4 6 to 1 3 5</td>
</tr>
<tr>
<td></td>
<td>8 9 0</td>
<td>8 9 0</td>
</tr>
<tr>
<td>mirrorDiagonalRightToLeft</td>
<td>transforms</td>
<td>2 4 6 to 1 3 5</td>
</tr>
<tr>
<td></td>
<td>8 9 0</td>
<td>6 5 0</td>
</tr>
</tbody>
</table>

Consider the following method that transforms the matrix in one of the ways shown above:

```java
public static void someMethod(int[][] mat)
{
    int height = mat.length;
    int numCols = mat[0].length;
    for (int col = 0; col < numCols; col++)
    {
        for (int row = 0; row < height/2; row++)
            mat[height - row - 1][col] = mat[row][col];
}
```

Which method described above corresponds to `someMethod`?

(A) mirrorVerticalLeftToRight
(B) mirrorVerticalRightToLeft
(C) mirrorHorizontalTopToBottom
(D) mirrorHorizontalBottomToTop
(E) mirrorDiagonalRightToLeft
Refer to the following for Questions 37 and 38.

A word creation game uses a set of small letter tiles, all of which are initially in a tile bag. A partial implementation of a TileBag class is shown below.

```java
public class TileBag {
    //tiles contains all the tiles in the bag
    private List<Tile> tiles;
    //size is the number of not-yet-used tiles
    private int size;

    //Constructors and other methods are not shown.
}
```

Consider the following method in the TileBag class that allows a player to get a new tile from the TileBag.

```java
public Tile getNewTile() {
    if (size == 0) //no tiles left
        return null;
    int index = (int) (Math.random() * size);
    size--;
    Tile temp = tiles.get(index);
    /* code to swap tile at position size with tile at position index */
    return temp;
}
```

37. Which /* code to swap tile at position size with tile at position index */ performs the swap correctly?
(A) tiles.set(size, temp);
    tiles.set(index, tiles.get(size));
(B) tiles.set(index, tiles.get(size));
    tiles.set(size, temp);
(C) tiles.swap(index, size);
(D) tiles.get(size, temp);
    tiles.get(index, tiles.set(size));
(E) tiles.get(index, tiles.set(size));
    tiles.get(size, temp);

38. Which is true about the getNewTile algorithm?
(A) The algorithm allows the program to keep track of both used and unused tiles.
(B) The tiles list becomes one element shorter when getNewTile is executed.
(C) The algorithm selects a random Tile from all tiles in the list.
(D) The tiles list has used tiles in the beginning and unused tiles at the end.
(E) The tiles list contains only tiles that have not been used.

GO ON TO THE NEXT PAGE.
39. Consider the following two classes.

```java
public class Bird
{
    public void act()
    {
        System.out.print("fly ");
        makeNoise();
    }

    public void makeNoise()
    {
        System.out.print("chirp ");
    }
}

public class Dove extends Bird
{
    public void act()
    {
        super.act();
        System.out.print("waddle ");
    }

    public void makeNoise()
    {
        super.makeNoise();
        System.out.print("coo ");
    }
}
```

Suppose the following declaration appears in a class other than Bird or Dove:

```java
Bird pigeon = new Dove();
```

What is printed as a result of the call `pigeon.act()`?
(A) fly
(B) fly chirp
(C) fly chirp waddle
(D) fly chirp waddle coo
(E) fly chirp coo waddle
40. Consider a method `partialProd` that returns an integer array `prod` such that for all `k`, `prod[k]` is equal to `arr[0] * arr[1] * · · · * arr[k]`. For example, if `arr` contains the values `{2,5,3,4,10}`, the array `prod` will contain the values `{2,10,30,120,1200}`.

```java
public static int[] partialProd(int[] arr)
{
    int[] prod = new int[arr.length];
    for (int j = 0; j < arr.length; j++)
        prod[j] = 1;
    /* missing code */
    return prod;
}
```

Consider the following two implementations of `/* missing code */`.

Implementation 1

```java
for (int j = 1; j < arr.length; j++)
{
    prod[j] = prod[j - 1] * arr[j];
}
```

Implementation 2

```java
for (int j = 0; j < arr.length; j++)
    for (int k = 0; k <= j; k++)
        prod[j] = prod[j] * arr[k];
```

Which of the following statements is true?

(A) Both implementations work as intended but Implementation 1 is faster than Implementation 2.
(B) Both implementations work as intended but Implementation 2 is faster than Implementation 1.
(C) Both implementations work as intended and are equally fast.
(D) Implementation 1 doesn’t work as intended because the elements of `prod` are incorrectly assigned.
(E) Implementation 2 doesn’t work as intended because the elements of `prod` are incorrectly assigned.

END OF SECTION I
1. This question manipulates one-dimensional and two-dimensional arrays. In part (a) you will write a method to reverse elements of a one-dimensional array. In parts (b) and (c) you will write methods to reverse elements of a two-dimensional array.

(a) Consider the following incomplete ArrayUtil class, which contains a static reverseArray method.

```java
public class ArrayUtil {
    /** Reverses elements of array arr.
     * Precondition: arr.length > 0.
     * Postcondition: The elements of arr have been reversed.
     * @param arr the array to manipulate *
     */
    public static void reverseArray(int[] arr) {
        /* to be implemented in part (a) */
    }

    // Other methods are not shown.
}
```

GO ON TO THE NEXT PAGE.
Write the ArrayUtil method `reverseArray`. For example, if `arr` is the array `{2,7,5,1,0}`, the call to `reverseArray` changes `arr` to be `{0,1,5,7,2}`.

Complete method `reverseArray` below.

```java
/** Reverses elements of array arr.
 *  * Precondition: arr.length > 0.
 *  * Postcondition: The elements of arr have been reversed.
 *  * @param arr the array to manipulate
 */
public static void reverseArray(int[] arr)
```

(b) Consider the following incomplete `Matrix` class, which represents a two-dimensional matrix of integers. Assume that the matrix contains at least one integer.

```java
public class Matrix {
    private int[][] mat;
    /** Constructs a matrix of integers. */
    public Matrix (int[][] m)
    { mat = m; }
    /** Reverses the elements in each row of mat.
     *  * Postcondition: The elements in each row have been reversed.
     */
    public void reverseAllRows()
    { /* to be implemented in part (b) */ }
    /** Reverses the elements of mat.
     *  * Postcondition:
     *  * - The final elements of mat, when read in row-major order,
     *  * - are the same as the original elements of mat when read
     *  * - from the bottom corner, right to left, going upward.
     *  * - mat[0][0] contains what was originally the last element.
     *  * - mat[mat.length-1][mat[0].length-1] contains what was
     *  * - originally the first element.
     */
    public void reverseMatrix()
    { /* to be implemented in part (c) */ }
    //Other instance variables, constructors and methods are not shown.
}
```
Write the Matrix method reverseAllRows. This method reverses the elements of each row. For example, if mat1 refers to a Matrix object, then the call mat1.reverseAllRows() will change the matrix as shown below.

<table>
<thead>
<tr>
<th>Before call</th>
<th>After call</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 1 2 3 4</td>
<td>0 4 3 2 1</td>
</tr>
<tr>
<td>1 5 6 7 8</td>
<td>1 8 7 6 5</td>
</tr>
<tr>
<td>2 9 10 11 12</td>
<td>2 12 11 10 9</td>
</tr>
</tbody>
</table>

In writing reverseAllRows, you must call the reverseArray method in part (a). Assume that reverseArray works correctly regardless of what you wrote in part (a).

Complete method reverseAllRows below.

```java
/** Reverses the elements in each row of mat.
 * Postcondition: The elements in each row have been reversed.
 */
public void reverseAllRows()
```

(c) Write the Matrix method reverseMatrix. This method reverses the elements of a matrix such that the final elements of the matrix, when read in row-major order, are the same as the original elements when read from the bottom corner, right to left, going upward. Again let mat1 be a reference to a Matrix object. The call mat1.reverseMatrix() will change the matrix as shown below.

<table>
<thead>
<tr>
<th>Before call</th>
<th>After call</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 1 2</td>
<td>0 6 5</td>
</tr>
<tr>
<td>1 3 4</td>
<td>1 4 3</td>
</tr>
<tr>
<td>2 5 6</td>
<td>2 1 1</td>
</tr>
</tbody>
</table>

In writing reverseMatrix, you must call the reverseAllRows method in part (b). Assume that reverseAllRows works correctly regardless of what you wrote in part (b).

Complete method reverseMatrix below.

```java
/** Reverses the elements of mat.
 * Postcondition:
 * - The final elements of mat, when read in row-major order,
 *   are the same as the original elements of mat when read
 *   from the bottom corner, right to left, going upward.
 * - mat[0][0] contains what was originally the last element.
 * - mat[mat.length-1][mat[0].length-1] contains what was
 *   originally the first element.
 */
public void reverseMatrix()
```
2. A text-editing program uses a Sentence class that manipulates a single sentence. A sentence contains letters, blanks, and punctuation. The first character in a sentence is a letter, and the last character is a punctuation mark. Any two words in the sentence are separated by a single blank. A partial implementation of the Sentence class is as follows.

```java
public class Sentence {
    /** The sentence to manipulate */
    private String sentence;

    /** @return an ArrayList of integer positions containing a blank in this sentence. If there are no blanks in the sentence, returns an empty list. */
    public List<Integer> getBlankPositions()
    { /* to be implemented in part (a) */ }

    /** @return the number of words in this sentence
     * Precondition: Sentence contains at least one word.
     */
    public int countWords()
    { /* to be implemented in part (b) */ }

    /** @return the array of words in this sentence
     * Precondition:
     * - Any two words in the sentence are separated by one blank.
     * - The sentence contains at least one word.
     * Postcondition: String[] returned containing the words in this sentence.
     */
    public String[] getWords()
    { /* to be implemented in part (c) */ }

    //Constructor and other methods are not shown.
}
```

(a) Write the Sentence method getBlankPositions, which returns an ArrayList of integers that represent the positions in a sentence containing blanks. If there are no blanks in the sentence, getBlankPositions should return an empty list.

Some results of calling getBlankPositions are shown below.

<table>
<thead>
<tr>
<th>Sentence</th>
<th>Result of call to getBlankPositions</th>
</tr>
</thead>
<tbody>
<tr>
<td>I love you!</td>
<td>[1, 6]</td>
</tr>
<tr>
<td>The cat sat on the mat.</td>
<td>[3, 7, 11, 14, 18]</td>
</tr>
<tr>
<td>Why?</td>
<td>[]</td>
</tr>
</tbody>
</table>

GO ON TO THE NEXT PAGE.
Complete method `getBlankPositions()` below.

```java
/** @return an ArrayList of integer positions containing a 
 * blank in this sentence. If there are no blanks in the 
 * sentence, returns an empty list. */
public List<Integer> getBlankPositions()
```

(b) Write the `Sentence` method `countWords()`, which returns the number of words in a sentence. Words are sequences of letters or punctuation, separated by a single blank. You may assume that every sentence contains at least one word.

For example:

<table>
<thead>
<tr>
<th>Sentence</th>
<th>Result returned by <code>countWords</code></th>
</tr>
</thead>
<tbody>
<tr>
<td>I love you!</td>
<td>3</td>
</tr>
<tr>
<td>The cat sat on the mat.</td>
<td>6</td>
</tr>
<tr>
<td>Why?</td>
<td>1</td>
</tr>
</tbody>
</table>

Complete method `countWords()` below.

```java
/** @return the number of words in this sentence 
 * Precondition: Sentence contains at least one word. */
public int countWords()
```

(c) Write the `Sentence` method `getWords()`, which returns an array of words in the sentence. A word is defined as a string of letters and punctuation, and does not contain any blanks. You may assume that a sentence contains at least one word.

Some examples of calling `getWords()` are shown below.

<table>
<thead>
<tr>
<th>Sentence</th>
<th>Result returned by <code>getWords</code></th>
</tr>
</thead>
<tbody>
<tr>
<td>The bird flew away.</td>
<td>{The, bird, flew, away.}</td>
</tr>
<tr>
<td>Wow!</td>
<td>{Wow!}</td>
</tr>
<tr>
<td>Hi! How are you?</td>
<td>{Hi!, How, are, you?}</td>
</tr>
</tbody>
</table>

In writing method `getWords()`, you **must** use methods `getBlankPositions` and `countWords()`, which were written in parts (a) and (b). You may assume that these methods work correctly, irrespective of what you wrote in parts (a) and (b).

Complete method `getWords()` below.

```java
/** @return the array of words in this sentence 
 * Precondition: 
 * - Any two words in the sentence are separated by one blank. 
 * - The sentence contains at least one word. 
 * Postcondition: String[] returned containing the words in 
 * this sentence. */
public String[] getWords()
```

GO ON TO THE NEXT PAGE.
3. In this question you will implement two methods for a class Tournament that keeps track of the players who have registered for a tournament. The Tournament class uses the Player class shown below. A Player has a name and player number specified when a player is constructed.

```java
public class Player
{
    public Player(String name, int playerNumber)
    { /* implementation not shown */ }

    public int getPlayerNumber()
    { /* implementation not shown */ }

    //Private instance variables and other methods are not shown.
}
```

An incomplete declaration for the Tournament class is shown below. There are 100 available slots for players in the tournament, and the players are numbered 0,1,2,...,99.

```java
public class Tournament
{
    /** The list of slots in the tournament.
    * Each element corresponds to a slot in the tournament.
    * If slots[i] is null, the slot is not yet taken;
    * otherwise it contains a reference to a Player.
    * For example, slots[i].getPlayerNumber() returns i.
    */
    private Player[] slots;

    /** The list of names of players who wish to participate in
    * the tournament, but cannot because all slots are taken.
    */
    private List<String> waitingList;
}
```

GO ON TO THE NEXT PAGE.
public Player requestSlot(String playerName)
{ /* to be implemented in part (a) */ }

/** Release the slot for player p, thus removing that player
* from the tournament. If there are any names in waitingList,
* remove the first name and create a Player in the
* canceled slot for this person. Return the new Player.
* If waitingList is empty, mark the slot specified by p as
* empty and return null.
* Precondition: p is a valid Player for some slot in
* this tournament.
* @param p the player who will be removed from the tournament
* @return the new Player placed in the canceled slot
* */
public Player cancelAndReassignSlot(Player p)
{ /* to be implemented in part (b) */ }

//Constructor and other methods are not shown.

(a) Write the Tournament method requestSlot. Method requestSlot tries to
reserve a slot in the tournament for a given player. If there are any available
slots in the tournament, one of them is assigned to the named player, and
the newly created Player is returned. If there are no available slots, the
player’s name is added to the end of the waiting list and null is returned.

Complete method requestSlot below.

/** If there are any empty slots (slots with no Player)
* assign the player with the specified playerName to an
* empty slot. Create and return the new Player.
* If there are no available slots, add the player’s name
* to the end of the waiting list and return null.
* @playerName the name of the person requesting a slot
* @return the new Player
* */
public Player requestSlot(String playerName)
(b) Write the Tournament method cancelAndReassignSlot. This method releases a previous player's slot. If the waiting list for the tournament contains any names, the newly available slot is reassigned to the person at the front of the list. That person's name is removed from the waiting list, and the newly created Player is returned. If the waiting list is empty, the newly released slot is marked as empty, and null is returned.

In writing cancelAndReassignSlot, you may use any accessible methods in the Player and Tournament classes. Assume that these methods work as specified.

Complete method cancelAndReassignSlot below.

```java
/** Release the slot for player p, thus removing that player
 * from the tournament. If there are any names in waitingList,
 * remove the first name and create a Player in the
 * canceled slot for this person. Return the new Player.
 * If waitingList is empty, mark the slot specified by p as
 * empty and return null.
 * Precondition: p is a valid Player for some slot in
 * this tournament.
 * @param p the player who will be removed from the tournament
 * @return the new Player placed in the canceled slot */
public Player cancelAndReassignSlot(Player p)
```

4. A chemical solution is said to be *acidic* if it has a pH integer value from 1 to 6, inclusive. The lower the pH, the more acidic the solution. An experiment has a large number of chemical solutions arranged in a line and a mechanical arm that moves back and forth along the line, so that the acidity of each solution can be altered by adding various chemicals. A chemical solution is specified by the Solution interface below.
public interface Solution {
    /** @return an integer value that ranges from 1 (very acidic)
    * to 14 */
    int getPH();

    /** Set PH to newValue.
    * @param newValue the new PH value */
    void setPH(int newValue);
}

The experiment keeps track of the solutions and the mechanical arm. The figure below represents the solutions and mechanical arm in an experiment. The arm, indicated by the arrow, is currently at index 4 and is facing left. The second row of integers represents the pH values of the solutions.

<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>4</td>
<td>10</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>13</td>
</tr>
</tbody>
</table>

In this experiment, the most acidic solution is at index 1, since its pH value is the lowest.

The state of the mechanical arm includes the index of its location and direction it is facing (to the right or to the left). A mechanical arm is specified by the MechanicalArm interface below.

public interface MechanicalArm {
    /** @return the index of the current location of the mechanical arm */
    int getCurrentIndex();

    /** @return true if the mechanical arm is facing right
    * (toward solutions with larger indexes),
    * false if the mechanical arm is facing left
    * (toward solutions with smaller indexes) */
    boolean isFacingRight();

    /** Changes the current direction of the mechanical arm */
    void changeDirection();

    /** Moves the mechanical arm forward in its current direction
    * by the number of locations specified.
    * @param numLocs the number of locations to move
    * Precondition: numLocs >= 0. */
    void moveForward(int numLocs);
}
An experiment is represented by the `Experiment` class shown below.

```java
public class Experiment {
    /** The mechanical arm used to process the solutions */
    private MechanicalArm arm;

    /** The list of solutions */
    private List<Solution> solutions;

    /** Resets the experiment.
     * Postcondition:
     * - The mechanical arm has a current index of 0.
     * - It is facing right.
     */
    public void reset() {
        /* to be implemented in part (a) */
    }

    /** Finds and returns the index of the most acidic solution.
     * @return index the location of the most acidic solution
     * or -1 if there are no acidic solutions
     * Postcondition:
     * - The mechanical arm is facing right.
     * - Its current index is at the most acidic solution, or at
     * 0 if there are no acidic solutions.
     */
    public int mostAcidic() {
        /* to be implemented in part (b) */
    }
}
```

(a) Write the `Experiment` method `reset` that places the mechanical arm facing right, at index 0.

For example, suppose the experiment contains the solutions with pH values shown. The arrow represents the mechanical arm.

<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>4</td>
<td>10</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>13</td>
</tr>
</tbody>
</table>

A call to `reset` will result in

<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>4</td>
<td>10</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>13</td>
</tr>
</tbody>
</table>
Information repeated from the beginning of the question

```java
public interface Solution{
    int getPH();
    void setPH(int newValue);
}
```

```java
public interface MechanicalArm{
    int getCurrentIndex();
    boolean isFacingRight();
    void changeDirection();
    void moveForward(int numLocs);
}
```

```java
public class Experiment{
    private MechanicalArm arm;
    private List<Solution> solutions;
    public void reset(){
        // Reset the experiment.
        postcondition:
        - The mechanical arm has a current index of 0.
        - It is facing right.
    }
    public int mostAcidic(){
        // Write the Experiment method mostAcidic that returns the index of the most acidic solution and places the mechanical arm facing right at the location of the most acidic solution. A solution is acidic if its pH is less than 7. The lower the pH, the more acidic the solution. If there are no acidic solutions in the experiment, the mostAcidic method should return -1 and place the mechanical arm at index 0, facing right.
        // For example, suppose the experiment has this state:
        //
        // | index | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
        // |------|---|---|---|---|---|---|---|
        // | pH   | 7 | 4 | 10| 5 | 6 | 7 | 13|
        //
        A call to mostAcidic should return the value 1 and result in the following state for the experiment:
        //
        // | index | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
        // |------|---|---|---|---|---|---|---|
        // | pH   | 7 | 4 | 10| 5 | 6 | 7 | 13|
    }
}
```

Complete method reset below.

```java
/** Resets the experiment.
 * Postcondition:
 * - The mechanical arm has a current index of 0.
 * - It is facing right.
 */
public void reset()
```

(b) Write the Experiment method mostAcidic that returns the index of the most acidic solution and places the mechanical arm facing right at the location of the most acidic solution. A solution is acidic if its pH is less than 7. The lower the pH, the more acidic the solution. If there are no acidic solutions in the experiment, the mostAcidic method should return -1 and place the mechanical arm at index 0, facing right.
For example, suppose the experiment has this state:

```
<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>4</td>
<td>10</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>13</td>
</tr>
</tbody>
</table>
```

A call to mostAcidic should return the value 1 and result in the following state for the experiment:

```
<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>4</td>
<td>10</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>13</td>
</tr>
</tbody>
</table>
```
If the experiment has this state,

<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>9</td>
<td>8</td>
<td>8</td>
<td>12</td>
<td>13</td>
<td>14</td>
</tr>
</tbody>
</table>

a call to `mostAcidic` should return the value -1 and result in the following state for the experiment:

<table>
<thead>
<tr>
<th>index</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7</td>
<td>9</td>
<td>8</td>
<td>8</td>
<td>12</td>
<td>13</td>
<td>14</td>
</tr>
</tbody>
</table>

Information repeated from the beginning of the question

```java
public interface Solution

int getPH()
void setPH(int newValue)
```

```java
public interface MechanicalArm

int getCurrentIndex()
boolean isFacingRight()
void changeDirection()
void moveForward(int numLocs)
```

```java
public class Experiment

private MechanicalArm arm
private List<Solution> solutions
public void reset()
public int mostAcidic()
```

Complete method `mostAcidic` below.

```java
/** Finds and returns the index of the most acidic solution.
   * @return index the location of the most acidic solution
   * or -1 if there are no acidic solutions
   * Postcondition:
   * - The mechanical arm is facing right.
   * - Its current index is at the most acidic solution, or at
   *   0 if there are no acidic solutions.
   */
public int mostAcidic()
```

END OF EXAMINATION
**ANSWER KEY (Section I)**

<p>| | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1. D</td>
<td>15. E</td>
<td>29. A</td>
<td></td>
</tr>
<tr>
<td>3. C</td>
<td>17. A</td>
<td>31. A</td>
<td></td>
</tr>
<tr>
<td>6. E</td>
<td>20. E</td>
<td>34. D</td>
<td></td>
</tr>
<tr>
<td>10. A</td>
<td>24. E</td>
<td>38. A</td>
<td></td>
</tr>
<tr>
<td>13. A</td>
<td>27. D</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**DIAGNOSTIC CHART FOR PRACTICE EXAM**

Each multiple-choice question has a complete explanation (p. 47).

The following table relates each question to sections that you should review. For any given question, the topic(s) in the chart represent the concept(s) tested in the question. These topics are explained on the corresponding page(s) in the chart and should provide further insight into answering that question.
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<th>Question</th>
<th>Topic</th>
<th>Page</th>
</tr>
</thead>
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<td>135</td>
</tr>
<tr>
<td>2</td>
<td>Implementing classes</td>
<td>212</td>
</tr>
<tr>
<td>3</td>
<td>Storage of integers</td>
<td>61</td>
</tr>
<tr>
<td>4</td>
<td>Constructors</td>
<td>95</td>
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<td>5</td>
<td>The toString method</td>
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<td></td>
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<td>61</td>
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<td>for loop</td>
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</tr>
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<td>8</td>
<td>Program specification</td>
<td>208</td>
</tr>
<tr>
<td>9</td>
<td>Recursion</td>
<td>291</td>
</tr>
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<td>10</td>
<td>Boolean expressions</td>
<td>65</td>
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</tr>
<tr>
<td>12</td>
<td>IndexOutOfBoundsException for ArrayList</td>
<td>244</td>
</tr>
<tr>
<td>13</td>
<td>Passing parameters</td>
<td>236</td>
</tr>
<tr>
<td>14</td>
<td>Passing parameters</td>
<td>236</td>
</tr>
<tr>
<td>15</td>
<td>Abstract classes</td>
<td>142</td>
</tr>
<tr>
<td>16</td>
<td>Subclass constructors and super keyword</td>
<td>135</td>
</tr>
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<td>17</td>
<td>Polymorphism</td>
<td>138</td>
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<td>18</td>
<td>swap method</td>
<td>237</td>
</tr>
<tr>
<td>19</td>
<td>Rounding real numbers</td>
<td>61</td>
</tr>
<tr>
<td>20</td>
<td>Recursion</td>
<td>293</td>
</tr>
<tr>
<td>21</td>
<td>Selection and insertion sort</td>
<td>324</td>
</tr>
<tr>
<td>22</td>
<td>Subclass method calls</td>
<td>141</td>
</tr>
<tr>
<td>23</td>
<td>Compound boolean expressions</td>
<td>65</td>
</tr>
<tr>
<td>24</td>
<td>String class equals method</td>
<td>178</td>
</tr>
<tr>
<td>25</td>
<td>String class substring method</td>
<td>180</td>
</tr>
<tr>
<td>26</td>
<td>Round-off error</td>
<td>62</td>
</tr>
<tr>
<td>27</td>
<td>Array processing</td>
<td>235</td>
</tr>
<tr>
<td>28</td>
<td>Assertions about algorithms</td>
<td>219</td>
</tr>
<tr>
<td></td>
<td>Binary search</td>
<td>329</td>
</tr>
<tr>
<td>29</td>
<td>Binary search</td>
<td>329</td>
</tr>
<tr>
<td>30</td>
<td>Random integers</td>
<td>185</td>
</tr>
<tr>
<td>31</td>
<td>String class substring method</td>
<td>180</td>
</tr>
<tr>
<td>32</td>
<td>Two-dimensional arrays</td>
<td>249</td>
</tr>
<tr>
<td>33</td>
<td>Relationships between classes</td>
<td>216</td>
</tr>
<tr>
<td>34</td>
<td>Array of objects</td>
<td>239</td>
</tr>
<tr>
<td></td>
<td>ArrayList</td>
<td>244</td>
</tr>
<tr>
<td>35</td>
<td>NullPointerException</td>
<td>103</td>
</tr>
<tr>
<td>36</td>
<td>Traversing an array</td>
<td>235</td>
</tr>
<tr>
<td></td>
<td>The if statement</td>
<td>69</td>
</tr>
<tr>
<td>37</td>
<td>Processing a 2-D array</td>
<td>251</td>
</tr>
<tr>
<td></td>
<td>Mirror images</td>
<td>357</td>
</tr>
<tr>
<td>38</td>
<td>Using ArrayList</td>
<td>245</td>
</tr>
<tr>
<td>39</td>
<td>Using ArrayList</td>
<td>245</td>
</tr>
<tr>
<td>40</td>
<td>Using super in a subclass</td>
<td>139</td>
</tr>
<tr>
<td></td>
<td>One-dimensional arrays</td>
<td>233</td>
</tr>
</tbody>
</table>
ANSWERS EXPLAINED

Section I

1. (D) Constructors are never inherited. If a subclass has no constructor, the default constructor for the superclass is generated. If the superclass does not have a default constructor, a compile-time error will occur.

2. (B) The programmer is using an object-oriented approach to writing the program and plans to test the simplest classes first. This is bottom-up development. In top-down development (choice A), high-level classes are broken down into subsidiary classes. Procedural abstraction (choice C) is the use of helper methods in a class. Information hiding (choice D) is restriction of access to private data and methods in a class. Choice E is wrong because a driver program is one whose sole purpose is to test a given method or class. Implementing the simplest classes first may involve driver programs that test the various methods, but the overall plan is not an example of a driver program.

3. (C) 8 bits (1 byte) are required to represent the values from 0 to 255. The base 2 number 11111111 represents $1 + 2 + 4 + 8 + 16 + 32 + 64 + 128 = 255$. Since there are 3 such values in an RGB representation, $(8)(3) = 24$ bits are needed.

4. (A) In the constructor, the private instance variables suit and value must be initialized to the appropriate parameter values. Choice A is the only choice that does this.

5. (B) Implementation II invokes the toString method of the Card class. Implementation I fails because there is no default toString method for arrays. Implementation III will cause a ClassCastException: You cannot cast a Card to a String.

6. (E) Since the values in arr cannot be greater than Integer.MAX_VALUE, the test in the while loop will be true at least once and will lead to the smallest element being stored in min. (If all the elements of the array are Integer.MAX_VALUE, the code still works.) Similarly, initializing min to arr[0], the first element in the array, ensures that all elements in arr will be examined and the smallest will be found. Choice I, Integer.MIN_VALUE, fails because the test in the loop will always be false! There is no array element that will be less than the smallest possible integer. The method will (incorrectly) return Integer.MIN_VALUE.

7. (B) The maximum number will be achieved if /* test */ is true in each pass through the loop. So the question boils down to: How many times is the loop executed? Try one odd and one even value of n:

\[
\begin{align*}
\text{If } n &= 7, \quad i = 0, 2, 4, 6 \quad \text{Ans} = 4 \\
\text{If } n &= 8, \quad i = 0, 2, 4, 6 \quad \text{Ans} = 4
\end{align*}
\]

Notice that choice B is the only expression that works for both $n = 7$ and $n = 8$.

8. (C) Here is one of the golden rules of programming: Don’t start planning the program until every aspect of the specification is crystal clear. A programmer should never make unilateral decisions about ambiguities in a specification.

9. (B) When $x \leq y$, a recursive call is made to whatIsIt($x - 1$, $y$). If $x$ decreases at every recursive call, there is no way to reach a successful base case. Thus, the method never terminates and eventually exhausts all available memory.
10. (A) The expression \( ! (\text{max } != \text{a[i]}) \) is equivalent to \( \text{max } == \text{a[i]} \), so the given expression is equivalent to \( \text{a[i]} == \text{max } || \text{max } == \text{a[i]} \), which is equivalent to \( \text{a[i]} == \text{max} \).

11. (C) A base-b number can be represented with b characters. Thus, base-2 uses 0,1 for example, and base-10 uses 0,1,2,3,4,5,6,7,8,9. A hexadecimal (base-16) number is represented with 16 characters: 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F, where A = 10, B = 11, C = 12, D = 13, E = 14, F = 15. The largest two-place base-2 integer is

\[ 11 = 1 \times 2^2 + 1 \times 2^1 = 3 \]

The largest two-place base-10 integer is

\[ 99 = 9 \times 10^1 + 9 \times 10^0 \]

The largest two-place base-16 integer is

\[ FF = F \times 16^1 + F \times 16^0 \]

The character F represents 15, so

\[ FF = 15 \times 16^1 + 15 \times 16^0 = 255 \]

Here's another way to think about this problem: Each hex digit is 4 binary digits (bits), since \( 16 = 2^4 \). Therefore a two-digit hex number is 8 bits. The largest base-10 number that can be represented with 8 bits is \( 2^8 - 1 = 255 \).

12. (B) The index range for ArrayList is \( 0 \leq \text{index} \leq \text{size()}-1 \). Thus, for methods get, remove, and set, the last in-bounds index is \( \text{size()}-1 \). The one exception is the add method—to add an element to the end of the list takes an index parameter \( \text{list.size()} \).

13. (A) The array will not be changed by the increment method. Here are the memory slots:

Before the first call, increment(3):

<table>
<thead>
<tr>
<th>testArray</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 4 5</td>
</tr>
</tbody>
</table>

Just after the first call:

<table>
<thead>
<tr>
<th>testArray</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 4 5</td>
</tr>
</tbody>
</table>

Just before exiting increment(3):

<table>
<thead>
<tr>
<th>testArray</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 4 5</td>
</tr>
</tbody>
</table>

Just after exiting increment(3):

<table>
<thead>
<tr>
<th>testArray</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 4 5</td>
</tr>
</tbody>
</table>

The same analysis applies to the method calls increment(4) and increment(5).

14. (A) As in the previous question, the array will not be changed by the increment method. Nor will the local variable element! What will be changed by increment is the copy of the parameter during each pass through the loop.
15. (E) Subclasses of Quadrilateral may also be abstract, in which case they will inherit perimeter and/or area as abstract methods.

16. (C) Segment I starts correctly but fails to initialize the additional private variables of the Rectangle class. Segment II is wrong because by using super with the TopLeft and theBotRight, it implies that these values are used in the Quadrilateral superclass. This is false—there isn’t even a constructor with three arguments in the superclass.

17. (A) During execution the appropriate area method for each quad in quadList will be determined (polymorphism or dynamic binding).

18. (E) The algorithm has three steps:
   1. Store the object at i in temp.
   2. Place at location i the object at j.
   3. Place temp at location j.

   This has the effect of swapping the objects at i and j. Notice that choices B and C, while incomplete, are not incorrect. The question, however, asks for the best description of the postcondition, which is found in choice E.

19. (A) Subtracting 0.5 from a negative real number and then truncating it produces the number correctly rounded to the nearest integer. Note that casting to an int truncates a real number. The expression in choice B is correct for rounding a positive real number. Choice C won’t round correctly. For example, −3.7 will be rounded to −3 instead of −4. Choices D and E don’t make sense. Why cast to double if you’re rounding to the nearest integer?

20. (E) The method call `whatsIt(347)` puts on the stack `System.out.print(7)`.
    The method call `whatsIt(34)` puts on the stack `System.out.print(4)`.
    The method call `whatsIt(3)` is a base case and writes out 3.
    Now the stack is popped from the top, and the 3 that was printed is followed by 4, then 7. The result is 347.

21. (B) Recall that insertion sort takes each element in turn and (a) finds its insertion point and (b) moves elements to insert that element in its correct place. Thus, if the array is in reverse sorted order, the insertion point will always be at the front of the array, leading to the maximum number of comparisons and data moves—very inefficient. Therefore choices A, C, and E are false.
    Selection sort finds the smallest element in the array and swaps it with a[0] and then finds the smallest element in the rest of the array and swaps it with a[1], and so on. Thus, the same number of comparisons and moves will occur, irrespective of the original arrangement of elements in the array. So choice B is true, and choice D is false.

22. (E) Method call I fails because ClassOne does not have access to the methods of its subclass. Method call II fails because c2 needs to be cast to ClassTwo to be able to access methodTwo. Thus, the following would be OK:

    ```java
    ((ClassTwo) c2).methodTwo();
    ```

    Method call III works because ClassTwo inherits methodOne from its superclass, ClassOne.

23. (D) Notice that in the original code, if n is 1, k is incremented by 1, and if n is 4, k is incremented by 4. This is equivalent to saying “if n is 1 or 4, k is incremented
by n.”

24. (E) Segment I will throw a NullPointerException when \texttt{s.equals...} is invoked, because \texttt{s} is a null reference. Segment III looks suspect, but when the \texttt{startIndex} parameter of the substring method equals \texttt{s.length()}, the value returned is the empty string. If, however, \texttt{startIndex > s.length()}, a StringIndexOutOfBoundsException is thrown.

25. (A) Since results of calculations with floating-point numbers are not always represented exactly (round-off error), direct tests for equality are not reliable. Instead of the boolean expression \texttt{d == c}, a test should be done to check whether the difference of \texttt{d} and \texttt{c} is within some acceptable tolerance interval (see the Box on comparing floating-point numbers, p. 65).

26. (C) If \texttt{arr} has elements 2, 3, 5, the values of value are

\[
\begin{align*}
2 & \quad \text{/after initialization} \\
2*10 + 3 &= 23 & \text{/when } i = 1 \\
23*10 + 5 &= 235 & \text{/when } i = 2
\end{align*}
\]

27. (D) The point of the binary search algorithm is that the interval containing \texttt{key} is repeatedly narrowed down by splitting it in half. For each iteration of the while loop, if \texttt{key} is in the list, \texttt{arr[first] ≤ key ≤ arr[last]}. Note that (i) the endpoints of the interval must be included, and (ii) \texttt{key} is not necessarily in the list.

28. (B)

<table>
<thead>
<tr>
<th>first</th>
<th>last</th>
<th>mid</th>
<th>a[mid]</th>
</tr>
</thead>
<tbody>
<tr>
<td>After first iteration</td>
<td>0</td>
<td>13</td>
<td>6</td>
</tr>
<tr>
<td>After second iteration</td>
<td>7</td>
<td>13</td>
<td>10</td>
</tr>
<tr>
<td>After third iteration</td>
<td>7</td>
<td>9</td>
<td>8</td>
</tr>
<tr>
<td>After fourth iteration</td>
<td>9</td>
<td>9</td>
<td>9</td>
</tr>
</tbody>
</table>

29. (A) The data structure is an array, not an ArrayList, so you cannot use the \texttt{add} method for inserting elements into the list. This eliminates choices B and D. The expression to return a random integer from 0 to \texttt{k-1} inclusive is

\[
\texttt{(int) (Math.random() * k)}
\]

Thus, to get integers from 0 to 100 requires \texttt{k} to be 101, which eliminates choice C. Choice E fails because it gets integers from 1 to 100.

30. (A) Suppose \texttt{str1} is \texttt{strawberry} and \texttt{str2} is \texttt{cat}. Then \texttt{insert(str1, str2, 5)} will return the following pieces, concatenated:

\[
\texttt{straw + cat + berry}
\]

Recall that \texttt{s.substring(k, m)} (a method of \texttt{String}) returns a substring of \texttt{s} starting at position \texttt{k} and ending at position \texttt{m-1}. String \texttt{str1} must be split into two parts, \texttt{first} and \texttt{last}. Then \texttt{str2} will be inserted between them. Since \texttt{str2} is inserted starting at position 5 (the “b”), \texttt{first = straw}, namely \texttt{str1.substring(0, pos)}. (Start at 0 and take all the characters up to and including location \texttt{pos-1}, namely 4.) Notice that \texttt{last}, the second substring of \texttt{str1}, must start at the index for “b”, which is \texttt{pos}, the index at which \texttt{str2} was inserted. The expression \texttt{str1.substring(pos)} returns the substring of \texttt{str1} that starts at \texttt{pos} and continues to the end of the string, which was required. Note
that you don’t need any “special case” tests. In the cases where str2 is inserted at
the front of str1 (i.e., pos is 0) or the back of str1 (i.e., pos is str1.length()),
the code for the general case works.

31. (A) Method changeMatrix examines each element and changes it to its absolute
value if its row number equals its column number. The only two elements that
satisfy the condition r == c are mat[0][0] and mat[1][1]. Thus, -1 is changed to
1 and -4 is changed to 4, resulting in the matrix in choice A.

32. (C) Composition is the has-a relationship. A PlayerGroup has-a Player (several
of them, in fact). Inheritance, (choice D) is the is-a relationship, which doesn’t
apply here. None of the choices A, B, or E apply in this example: An interface
is a single class composed of only abstract methods (see p. 144); encapsulation is
the bundling together of data fields and operations into a single unit, a class (see
p. 93); and PlayerGroup and Player are clearly dependent on each other since
PlayerGroup contains several Player objects (see p. 212).

33. (E) All of these data structures are reasonable. They all represent 20 bingo num-
bers in a convenient way and provide easy mechanisms for crossing off numbers
and recognizing a winning card. Notice that data structure II provides a very
quick way of searching for a number on the card. For example, if 48 is called,
bingoCard[48] is inspected. If it is true, then it was one of the 20 original num-
bers on the card and gets crossed out. If false, 48 was not on that player’s card.
Data structures I and II require a linear search to find any given number that is
called. (Note: There is no assumption that the array is sorted, which would allow
a more efficient binary search.)

34. (D) A NullPointerException is thrown whenever an attempt is made to invoke
a method with an object that hasn’t been created with new. Choice A doesn’t
make sense: To test the Caller constructor requires a statement of the form

\[
\text{Caller c = new Caller();}
\]

Choice B is wrong: A missing return statement in a method triggers a compile-
time error. Choice C doesn’t make sense: In the declaration of numbers, its de-
fault initialization is to null. Choice E is bizarre. Hopefully you eliminated it
immediately!

35. (E) For each element in a, found is switched to true if that element is found
anywhere in b. Notice that for any element in a, if it is not found in b, the method
returns false. Thus, to return true, every element in a must also be in b. Notice
that this doesn’t necessarily mean that a and b are permutations of each other.
For example, consider the counterexample of a=[1,1,2,3] and b=[1,2,2,3].

36. (C) In the example given, height = 3, height/2 = 1, and numCols = 3. Notice
that in each pass through the loop, row has value 0, while col goes from 0 through
2. So here are the assignments:

\[
\begin{align*}
\text{mat[2][0]} &= \text{mat[0][0]} \\
\text{mat[2][1]} &= \text{mat[0][1]} \\
\text{mat[2][2]} &= \text{mat[0][2]} 
\end{align*}
\]

From this you should see that row 2 is being replaced by row 0.

37. (B) Eliminate choices D and E immediately, since assignment of new values in an
ArrayList is done with the set method, not get. Eliminate choice C since you do not
know that the TileBag class has a swap method. Choice A fails because it
replaces the element at position `size` before storing it. Choice B works because
the element at position `index` has been saved in `temp`.

38. (A) The `size` variable stores the number of unused tiles, which are in the `tiles`
list from position 0 to position `size`. A random `int` is selected in this range,
giving the index of the `Tile` that will be swapped to the end of the unused part of
the `tiles` list. Note that the length of the `tiles ArrayList` stays constant. Each
execution of `getNewTile` decreases the “unused tiles” part of the list and increases
the “already used” part at the end of the list. In this way, both used and unused
tiles are stored.

39. (E) When `pigeon.act()` is called, the `act` method of `Dove` is called. (This is an
example of polymorphism.) The `act` method of `Dove` starts with `super.act()`
which goes to the `act` method of `Bird`, the superclass. This prints `fly`, then calls
`makeNoise()`. Using polymorphism, the `makeNoise` method in `Dove` is called,
which starts with `super.makeNoise()`, which prints `chirp`. Completing the
`makeNoise` method in `Dove` prints `coo`. Thus, so far we’ve printed `fly chirp`
`coo`. But we haven’t completed `Dove`’s `act` method, which ends with printing out
`waddle`! The rule of thumb is: When `super` is used, find the method in the super-
class. But if that method calls a method that’s been overridden in the subclass,
go back there for the overridden method. You also mustn’t forget to check that
you’ve executed any pending lines of code in that superclass method!

40. (D) In Implementation 1, the first element assigned is `prod[1]`, and it multi-
plies `arr[1]` by `prod[0]`, which was initialized to 1. To fix this implementa-
tion, you need a statement preceding the loop, which correctly assigns `prod[0]`:
`prod[0]=arr[0];`
Section II

1. (a) public static void reverseArray(int[] arr)
   {
       int mid = arr.length/2;
       for (int i = 0; i < mid; i++)
       {
           int temp = arr[i];
           arr[i] = arr[arr.length - i - 1];
           arr[arr.length - i - 1] = temp;
       }
   }

(b) public void reverseAllRows()
   {
       for (int[] row: mat)
           ArrayUtil.reverseArray (row);
   }

(c) public void reverseMatrix()
   {
       reverseAllRows();
       int mid = mat.length/2;
       for (int i = 0; i < mid; i++)
       {
           for (int col = 0; col < mat[0].length; col++)
           {
               int temp = mat[i][col];
               mat[i][col] = mat[mat.length - i - 1][col];
               mat[mat.length - i - 1][col] = temp;
           }
       }
   }

   Alternative solution:
   public void reverseMatrix()
   {
       reverseAllRows();
       int mid = mat.length/2;
       for (int i = 0; i < mid; i++)
       {
           int[] temp = mat[i];
           mat[i] = mat[mat.length - i - 1];
           mat[mat.length - i - 1] = temp;
       }
   }

   NOTE
   • Parts (a) and the alternative solution in part (c) use the same algorithm, swapping the first and last elements, then the second and second last, etc., moving toward the middle. If there is an odd number of elements, the middle element does not move. In part (a) the elements are integers. In part (c) they are rows in the matrix.
   • In the first solution of part (c), start by reversing all rows. Then for each column, swap the elements in the first and last rows, then the second and second last, and so on, moving toward the middle.
   • The alternative solution in part (c) is more elegant. It is not, however, part of the AP subset to replace one row of a matrix with a different array.
2. (a) public List<Integer> getBlankPositions()
   {
      List<Integer> posList = new ArrayList<Integer>();
      for (int i = 0; i < sentence.length(); i++)
      {
         if (sentence.substring(i, i + 1).equals(" "))
            posList.add(i);
      }
      return posList;
   }

   Alternatively (an inferior, unnecessarily complicated solution!),
   
   public List<Integer> getBlankPositions()
   {
      List<Integer> posList = new ArrayList<Integer>();
      String s = sentence;
      int diff = 0;
      int index = s.indexOf(" ");
      while (index >= 0)
      {
         posList.add(index + diff);
         diff = sentence.length() - (s.substring(index + 1)).length();
         s = s.substring(index + 1);
         index = s.indexOf(" ");
      }
      return posList;
   }

   (b) public int countWords()
   {
      return getBlankPositions().size() + 1;
   }

   (c) public String[] getWords()
   {
      List<Integer> posList = getBlankPositions();
      int numWords = countWords();
      String[] wordArr = new String[numWords];
      for (int i = 0; i < numWords; i++)
      {
         if (i == 0)
         {
            if (posList.size() != 0)
               wordArr[i] = sentence.substring(0, posList.get(0));
            else
               wordArr[i] = sentence;
         }
         else if (i == posList.size())
            wordArr[i] = sentence.substring(posList.get(i - 1));
         else
            wordArr[i] = sentence.substring(posList.get(i - 1),
                                             posList.get(i));
      }
      return wordArr;
   }
NOTE

- In part (a), it would also work to have the test
  
  i < sentence.length() - 1;

  in the for loop. But you don't need the -1 because the last character is a punctuation mark, not a blank.

- In the alternative part (a), you can't just store the positions of index as you loop over the sentence. Finding s.indexOf(" ") will give a value that is too small, because you are successively taking shorter substrings of s. The local variable, diff, represents the difference between the length of the original sentence and the length of the current substring. This is what must be added to the current value of index, so that you get the position of the blank in the original sentence.

- Part (b) takes advantage of the precondition that there is one and only one blank between words. This means that the number of words will always be the number of blanks plus one.

- In part (c), you have to be careful when you get the first word. If there's only one word in the sentence, there are no blanks, which means posList is empty, and you can't use posList.get(0) (because that will throw an IndexOutOfBoundsException).

- Also in part (c), the second test deals with getting the last word in the sentence. You have to distinguish between the cases of more than one word in the sentence and exactly one word in the sentence.

3. (a) public Player requestSlot(String playerName)
    {
        for (int i = 0; i < slots.length; i++)
            {
                if (slots[i] == null)
                    {
                        Player p = new Player(playerName, i);
                        slots[i] = p;
                        return p;
                    }
            }
        waitingList.add(playerName);
        return null;
    }

(b) public Player cancelAndReassignSlot(Player p)
    {
        int i = p.getPlayerNumber();
        if (waitingList.size() != 0)
            {
                slots[i] = new Player(waitingList.get(0), i);
                waitingList.remove(0);
            }
        else
            {
                slots[i] = null;
            }
        return slots[i];
    }
NOTE

- In part (a), the last two lines of the method will be executed only if you are still in the method, namely no available slot was found.
- In part (b), the final line will return either a new player, or null if the waiting list was empty.

4. (a) public void reset()
   {
      if(arm.isFacingRight())
         arm.changeDirection();
      arm.moveForward(arm.getCurrentIndex());
      arm.changeDirection();
   }

(b) public int mostAcidic()
   {
      reset();
      int minPH = Integer.MAX_VALUE, minIndex = 0;
      int index = 0;
      while (index < solutions.size())
      {
         Solution s = solutions.get(index);
         if (s.getPH() < minPH)
         {
            minPH = s.getPH();
            minIndex = index;
         }
         index++;
      }
      if (minPH >= 7)
         return -1;
      else
      {
         arm.moveForward(minIndex);
         return minIndex;
      }
   }

NOTE

- In part (b), a for-each loop won’t work, because you need to save an index.
- In part (b), notice that resetting the mechanical arm causes the arm to face right.
- In part (b), you could initialize minPH to any integer greater than or equal to 7 for this algorithm to work. You just must be careful not to set it to an “acidic” number, namely 1 to 6.
Introductory Java
Language Features

Fifty loops shalt thou make . . .
—Exodus 26:5

Chapter Goals
- Packages and classes
- Types and identifiers
- Operators
- Input/output
- Storage of numbers
- Binary and hexadecimal numbers
- Control structures
- Errors and exceptions

The AP Computer Science course includes algorithm analysis, data structures, and the techniques and methods of modern programming, specifically, object-oriented programming. A high-level programming language is used to explore these concepts. Java is the language currently in use on the AP exam.

Java was developed by James Gosling and a team at Sun Microsystems in California; it continues to evolve. The AP exam covers a clearly defined subset of Java language features that are presented throughout this book. The College Board website, http://www.collegeboard.com/student/testing/ap/subjects.html, contains a complete listing of this subset.

Java provides basic control structures such as the if-else statement, for loop, for-each loop, and while loop, as well as fundamental built-in data types. But the power of the language lies in the manipulation of user-defined types called objects, many of which can interact in a single program.

PACKAGES AND CLASSES

A typical Java program has user-defined classes whose objects interact with those from Java class libraries. In Java, related classes are grouped into packages, many of which are provided with the compiler. You can put your own classes into a package—this facilitates their use in other programs.
Chapter 1 Introductory Java Language Features

The package java.lang, which contains many commonly used classes, is automatically provided to all Java programs. To use any other package in a program, an import statement must be used. To import all of the classes in a package called packagename, use the form

    import packagename.*;

To import a single class called ClassName from the package, use

    import packagename.ClassName;

Java has a hierarchy of packages and subpackages. Subpackages are selected using multiple dots:

    import packagename.subpackagename.ClassName;

The import statement allows the programmer to use the objects and methods defined in the designated package. By convention Java package names are lowercase. The AP exam does not require knowledge of packages. You will not be expected to write any import statements.

A Java program must have at least one class, the one that contains the main method. The java files that comprise your program are called source files. A compiler converts source code into machine-readable form called bytecode. Here is a typical source file for a Java program.

```java
/** Program FirstProg.java
   * Start with a comment, giving the program name and a brief
   * description of what the program does.
   */
import package1.*;
import package2.subpackage.ClassName;

public class FirstProg //note that the file name is FirstProg.java
{
    public static type1 method1(<parameter list>)
    {
        <code for method 1>
    }
    public static type2 method2(<parameter list>)
    {
        <code for method 2>
    }
    ...

    public static void main(String[] args)
    {
        <your code>
    }
}
```

NOTE

1. All Java methods must be contained in a class, and all program statements must be placed inside a method.
2. Typically, the class that contains the `main` method does not contain many additional methods.

3. The words `class`, `public`, `static`, `void`, and `main` are *reserved words*, also called *keywords*.

4. The keyword `public` signals that the class or method is usable outside of the class, whereas `private` data members or methods (see Chapter 2) are not.

5. The keyword `static` is used for methods that will not access any objects of a class, such as the methods in the `FirstProg` class in the example on the previous page. This is typically true for all methods in a source file that contains no *instance variables* (see Chapter 2). Most methods in Java do operate on objects and are not static. The `main` method, however, must always be static.

6. The program shown on the previous page is a Java *application*. This is not to be confused with a Java *applet*, a program that runs inside a web browser or applet viewer. Applets are not part of the AP subset.

### Javadoc Comments

The Javadoc comments `@param`, `@return`, and `@throws` are part of the AP Java subset. Here is an example.

```java
/** Puts obj at location loc in this grid, and returns
 * the object previously at this location.
 * Returns null if loc was previously unoccupied.
 * Precondition: obj is not null, and loc is valid in this grid.
 * @param loc the location where the object will be placed
 * @param obj the object to be placed
 * @return the object previously at the specified location
 * @throws NullPointerException if the object is null
 */
public E put(Location loc, E obj)
```

This will produce the following Javadoc output:

```
put

public E put (Location loc, E obj)

Puts obj at location loc in this grid, and returns
the object previously at this location.
Returns null if loc was previously unoccupied.
Precondition: obj is not null, and loc is valid in this grid.

Parameters:
loc - the location where the object will be placed
obj - the object to be placed

Returns:
the object previously at the specified location

Throws:
NullPointerException - if the object is null
```
Chapter 1  Introductory Java Language Features

**TYPES AND IDENTIFIERS**

**Identifiers**

An identifier is a name for a variable, parameter, constant, user-defined method, or user-defined class. In Java an identifier is any sequence of letters, digits, and the underscore character. Identifiers may not begin with a digit. Identifiers are case-sensitive, which means that age and Age are different. Wherever possible identifiers should be concise and self-documenting. A variable called area is more illuminating than one called a.

By convention identifiers for variables and methods are lowercase. Uppercase letters are used to separate these into multiple words, for example getName, findSurfaceArea, preTaxTotal, and so on. Note that a class name starts with a capital letter. Reserved words are entirely lowercase and may not be used as identifiers.

**Built-in Types**

Every identifier in a Java program has a type associated with it. The primitive or built-in types that are included in the AP Java subset are

- `int`: An integer. For example, 2, -26, 3000
- `boolean`: A boolean. Just two values, true or false
- `double`: A double precision floating-point number. For example, 2.718, -367189.41, 1.6e4

(Note that primitive type `char` is not included in the AP Java subset.)

Integer values are stored exactly. Because there’s a fixed amount of memory set aside for their storage, however, integers are bounded. If you try to store a value whose magnitude is too big in an int variable, you’ll get an overflow error. (Java gives you no warning. You just get a wrong result!)

An identifier, for example a variable, is introduced into a Java program with a declaration that specifies its type. A variable is often initialized in its declaration. Some examples follow:

```java
int x;
double y, z;
boolean found;
int count = 1; //count initialized to 1
double p = 2.3, q = 4.1; //p and q initialized to 2.3 and 4.1
```

One type can be cast to another compatible type if appropriate. For example,

```java
int total, n;
double average;

average = (double) total/n; //total cast to double to ensure real division is used
```

Alternatively,

```java
average = total/(double) n;
```

Assigning an int to a double automatically casts the int to double. For example,
int num = 5;  
double realNum = num;  //num is cast to double

Assigning a double to an int without a cast, however, causes a compile-time error. For example,

double x = 6.79;  
int intNum = x;  //Error. Need an explicit cast to int

Note that casting a floating-point (real) number to an integer simply truncates the number. For example,

double cost = 10.95;  
int numDollars = (int) cost;  //sets numDollars to 10

If your intent was to round cost to the nearest dollar, you needed to write

int numDollars = (int) (cost + 0.5);  //numDollars has value 11

To round a negative number to the nearest integer:

double negAmount = -4.8;  
int roundNeg = (int) (negAmount - 0.5);  //roundNeg has value 5

The strategy of adding or subtracting 0.5 before casting correctly rounds in all cases.

Storage of Numbers

INTEGERS

Integer values in Java are stored exactly, as a string of bits (binary digits). One of the bits stores the sign of the integer, 0 for positive, 1 for negative.

The Java built-in integral type, byte, uses one byte (eight bits) of storage.

```
0 1 1 1 1 1 1 1
```

The picture represents the largest positive integer that can be stored using type byte: $2^7 - 1$.

Type int in Java uses four bytes (32 bits). Taking one bit for a sign, the largest possible integer stored is $2^{31} - 1$. In general, an $n$-bit integer uses $n/8$ bytes of storage, and stores integers from $-2^{n-1}$ to $2^{n-1} - 1$. (Note that the extra value on the negative side comes from not having to store $-0$.) There are two Java constants that you should know. Integer.MAX_VALUE holds the maximum value an int can hold, $2^{31} - 1$. Integer.MIN_VALUE holds the minimum value an int can hold, $-2^{31}$.

Built-in types in Java are byte (one byte), short (two bytes), int (four bytes), and long (eight bytes). Of these, only int is in the AP Java subset.

FLOATING-POINT NUMBERS

There are two built-in types in Java that store real numbers: float, which uses four bytes, and double, which uses eight bytes. A floating-point number is stored in two parts: a mantissa, which specifies the digits of the number, and an exponent. The JVM (Java Virtual Machine) represents the number using scientific notation:

\[
\text{sign} \times \text{mantissa} \times 2^{\text{exponent}}
\]
In this expression, 2 is the base or radix of the number. In type `double` eleven bits are allocated for the exponent, and (typically) 52 bits for the mantissa. One bit is allocated for the sign. This is a double-precision number. Type `float`, which is single-precision, is not in the AP Java subset.

When floating-point numbers are converted to binary, most cannot be represented exactly, leading to round-off error. These errors are compounded by arithmetic operations. For example,

\[ 0.1_{10} \times 2^{26} \neq 0.1_{10} + 0.1_{10} + \ldots + 0.1_{10} \quad (26 \text{ terms}) \]

In Java, no exceptions are thrown for floating-point operations. There are two situations you should be aware of:

- When an operation is performed that gives an undefined result, Java expresses this result as `NaN`, "not a number." Examples of operations that produce `NaN` are: taking the square root of a negative number, and 0.0 divided by 0.0.
- An operation that gives an infinitely large or infinitely small number, like division by zero, produces a result of `Infinity` or `-Infinity` in Java.

### Hexadecimal and Octal Numbers

A hexadecimal number or hex number uses base (radix) 16 and is represented with the symbols 0 – 9 and A – F (occasionally a – f), where A represents 10, and F represents 15. To denote a hex number in Java, the prefix "0x" or "0X" is used, for example, 0xC2A. On the AP exam, the representation is likely to be with the subscript hex: C2A\text{\_hex}. In expanded form, this number means

\[
(C)(16^2) + (2)(16^1) + (A)(16^0)
= (12)(16^2) + (2)(16) + (10)(1)
= 3114, \text{ or } 3114_{\text{dec}}
\]

The advantages of hex numbers are their compactness, and the ease of conversion between hex and binary. Notice that any hex digit expands to four bits. For example,

\[
5_{\text{hex}} = 0101_{\text{bin}} \quad \text{and} \quad F_{\text{hex}} = 1111_{\text{bin}}
\]

Thus, 5F\text{\_hex} = 01011111\text{\_bin}, which is 10111111\text{\_bin}.

Similarly, to convert a binary number to hex, convert in groups of four from right to left. If necessary, pad with zeroes to complete the last group of four. For example,

\[
10111011_{\text{bin}} = 0101 \quad 1101_{\text{bin}}
= 5 \quad D_{\text{hex}}
= 5D_{\text{hex}}
\]

An octal number uses base 8, and is represented with the symbols 0 – 7. On the AP exam, the representation is likely to be with the subscript oct: 132\text{\_oct}. In expanded form, 132\text{\_oct} means

\[
(1)(8^2) + (3)(8^1) + (2)(8^0)
= (1)(64) + (3)(8) + (2)(1)
= 64 + 24 + 2
= 90, \text{ or } 90_{\text{dec}}
\]
Final Variables

A final variable or user-defined constant, identified by the keyword final, is used to name a quantity whose value will not change. Here are some examples of final declarations:

```java
final double TAX_RATE = 0.08;
final int CLASS_SIZE = 35;
```

NOTE

1. Constant identifiers are, by convention, capitalized.
2. A final variable can be declared without initializing it immediately. For example,

```java
final double TAX_RATE;
if (<some condition>)
    TAX_RATE = 0.08;
else
    TAX_RATE = 0.0;
// TAX_RATE can be given a value just once: its value is final!
```

3. A common use for a constant is as an array bound. For example,

```java
final int MAXSTUDENTS = 25;
int[] classList = new int[MAXSTUDENTS];
```

4. Using constants makes it easier to revise code. Just a single change in the final declaration need be made, rather than having to change every occurrence of a value.

OPERATORS

Arithmetic Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Meaning</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>addition</td>
<td>3 + x</td>
</tr>
<tr>
<td>-</td>
<td>subtraction</td>
<td>p - q</td>
</tr>
<tr>
<td>*</td>
<td>multiplication</td>
<td>6 * i</td>
</tr>
<tr>
<td>/</td>
<td>division</td>
<td>10 / 4 //returns 2, not 2.5!</td>
</tr>
<tr>
<td>%</td>
<td>mod (remainder)</td>
<td>11 % 8 //returns 3</td>
</tr>
</tbody>
</table>

NOTE

1. These operators can be applied to types int and double, even if both types occur in the same expression. For an operation involving a double and an int, the int is promoted to double, and the result is a double.
2. The mod operator %, as in the expression a % b, gives the remainder when a is divided by b. Thus 10 % 3 evaluates to 1, whereas 4.2 % 2.0 evaluates to 0.2.
3. Integer division a/b where both a and b are of type int returns the integer quotient only (i.e., the answer is truncated). Thus, 22/6 gives 3, and 3/4 gives 0. If at least one of the operands is of type double, then the operation becomes
regular floating-point division, and there is no truncation. You can control the kind of division that is carried out by explicitly casting (one or both of) the operands from int to double and vice versa. Thus

\[
\begin{align*}
3.0 / 4 & \rightarrow 0.75 \\
3 / 4.0 & \rightarrow 0.75 \\
(int) 3.0 / 4 & \rightarrow 0 \\
(double) 3 / 4 & \rightarrow 0.75
\end{align*}
\]

You must, however, be careful:

\[
\begin{align*}
(double) (3 / 4) \rightarrow 0.0
\end{align*}
\]

since the integer division 3/4 is computed first, before casting to double.

4. The arithmetic operators follow the normal precedence rules (order of operations):

1. parentheses, from the inner ones out (highest precedence)
2. *, /, %
3. +, - (lowest precedence)

Here operators on the same line have the same precedence, and, in the absence of parentheses, are invoked from left to right. Thus, the expression 19 % 5 * 3 + 14 / 5 evaluates to 4 * 3 + 2 = 14. Note that casting has precedence over all of these operators. Thus, in the expression (double) 3/4, 3 will be cast to double before the division is done.

### Relational Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Meaning</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>==</td>
<td>equal to</td>
<td>if (x == 100)</td>
</tr>
<tr>
<td>!=</td>
<td>not equal to</td>
<td>if (age != 21)</td>
</tr>
<tr>
<td>&gt;</td>
<td>greater than</td>
<td>if (salary &gt; 30000)</td>
</tr>
<tr>
<td>&lt;</td>
<td>less than</td>
<td>if (grade &lt; 65)</td>
</tr>
<tr>
<td>&gt;=</td>
<td>greater than or equal to</td>
<td>if (age &gt;= 16)</td>
</tr>
<tr>
<td>&lt;=</td>
<td>less than or equal to</td>
<td>if (height &lt;= 6)</td>
</tr>
</tbody>
</table>

**NOTE**

1. Relational operators are used in boolean expressions that evaluate to true or false.

   ```java
   boolean x = (a != b);    //initializes x to true if a != b, 
                        //false otherwise
   return p == q;           //returns true if p equals q, false otherwise
   ```

2. If the operands are an int and a double, the int is promoted to a double as for arithmetic operators.

3. Relational operators should generally be used only in the comparison of primitive types (i.e., int, double, or boolean). User-defined types are compared using the equals and compareTo methods (see pp. 145 and 176).

4. Be careful when comparing floating-point values! Since floating-point numbers cannot always be represented exactly in the computer memory, they should not be compared directly using relational operators.
Comparing Floating-Point Numbers

Because of round-off errors in floating-point numbers, you can’t rely on using the `==` or `!=` operators to compare two `double` values for equality. They may differ in their last significant digit or two because of round-off error. Instead, you should test that the magnitude of the difference between the numbers is less than some number about the size of the machine precision. The machine precision is usually denoted $\epsilon$ and is typically about $10^{-16}$ for double precision (i.e., about 16 decimal digits). So you would like to test something like $|x - y| \leq \epsilon$. But this is no good if $x$ and $y$ are very large. For example, suppose $x = 1234567890.123456$ and $y = 1234567890.123457$. These numbers are essentially equal to machine precision, since they differ only in the 16th significant digit. But $|x - y| = 10^{-6}$, not $10^{-16}$. So in general you should check the relative difference:

$$\frac{|x - y|}{\max(|x|, |y|)} \leq \epsilon$$

To avoid problems with dividing by zero, code this as

$$|x - y| \leq \epsilon \max(|x|, |y|)$$

An example of code that uses a correct comparison of real numbers can be found in the `Shape` class on p. 146.

### Logical Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Meaning</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>!</code></td>
<td>NOT</td>
<td>if (!found)</td>
</tr>
<tr>
<td><code>&amp;&amp;</code></td>
<td>AND</td>
<td>if (<code>x &lt; 3 &amp;&amp; y &gt; 4</code>)</td>
</tr>
<tr>
<td>`</td>
<td></td>
<td>`</td>
</tr>
</tbody>
</table>

**NOTE**

1. Logical operators are applied to boolean expressions to form compound boolean expressions that evaluate to `true` or `false`.
2. Values of `true` or `false` are assigned according to the truth tables for the logical operators.

| `&&` | `||` |
|------|------|
| `T`  | `T`  |
| `F`  | `T`  |
| `F`  | `T`  |

<table>
<thead>
<tr>
<th><code>!</code></th>
</tr>
</thead>
<tbody>
<tr>
<td><code>T</code></td>
</tr>
<tr>
<td><code>F</code></td>
</tr>
</tbody>
</table>

For example, `F && T` evaluates to `F`, while `T || F` evaluates to `T`.

3. **Short-circuit evaluation.** The subexpressions in a compound boolean expression are evaluated from left to right, and evaluation automatically stops as
soon as the value of the entire expression is known. For example, consider a boolean OR expression of the form \( A \lor B \), where \( A \) and \( B \) are some boolean expressions. If \( A \) is true, then the expression is true irrespective of the value of \( B \). Similarly, if \( A \) is false, then \( A \land B \) evaluates to false irrespective of the second operand. So in each case the second operand is not evaluated. For example,

\[
\text{if (numScores != 0 && scoreTotal/numScores > 90)}
\]

will not cause a run-time ArithmeticException (division-by-zero error) if the value of numScores is 0. This is because numScores != 0 will evaluate to false, causing the entire boolean expression to evaluate to false without having to evaluate the second expression containing the division.

### Assignment Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Example</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>=</td>
<td>( x = 2 )</td>
<td>simple assignment</td>
</tr>
<tr>
<td>+=</td>
<td>( x += 4 )</td>
<td>( x = x + 4 )</td>
</tr>
<tr>
<td>-=</td>
<td>( y -= 6 )</td>
<td>( y = y - 6 )</td>
</tr>
<tr>
<td>*=</td>
<td>( p *= 5 )</td>
<td>( p = p * 5 )</td>
</tr>
<tr>
<td>/=</td>
<td>( n /= 10 )</td>
<td>( n = n / 10 )</td>
</tr>
<tr>
<td>%=</td>
<td>( n %= 10 )</td>
<td>( n = n % 10 )</td>
</tr>
</tbody>
</table>

### Note

1. All these operators, with the exception of simple assignment, are called compound assignment operators.
2. Chaining of assignment statements is allowed, with evaluation from right to left.

```java
int next, prev, sum;
next = prev = sum = 0; //initializes sum to 0, then prev to 0
//then next to 0
```

### Increment and Decrement Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Example</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>++</td>
<td>( i++ ) or ++i</td>
<td>( i ) is incremented by ( 1 )</td>
</tr>
<tr>
<td>--</td>
<td>( k-- ) or ( --k )</td>
<td>( k ) is decremented by ( 1 )</td>
</tr>
</tbody>
</table>

Note that \( i++ \) (postfix) and ++i (prefix) both have the net effect of incrementing \( i \) by \( 1 \), but they are not equivalent. For example, if \( i \) currently has the value 5, then `System.out.println(i++)` will print 5 and then increment \( i \) to 6, whereas `System.out.println(++i)` will first increment \( i \) to 6 and then print 6. It’s easy to remember: if the ++ is first, you first increment. A similar distinction occurs between k-- and --k. (Note: You do not need to know these distinctions for the AP exam.)
Operator Precedence

highest precedence $\rightarrow$ (1) !, ++, --
(2) *, /, %
(3) +, -
(4) <, >, <=, >=
(5) ==, !=
(6) & &
(7) | |

lowest precedence $\rightarrow$ (8) =, +=, -=, *=, /=, %=

Here operators on the same line have equal precedence. The evaluation of the operators with equal precedence is from left to right, except for rows (1) and (8) where the order is right to left. It is easy to remember: The only “backward” order is for the unary operators (row 1) and for the various assignment operators (row 8).

Example

What will be output by the following statement?

```java
System.out.println(5 + 3 < 6 - 1);
```

Since + and - have precedence over <, 5 + 3 and 6 - 1 will be evaluated before evaluating the boolean expression. Since the value of the expression is false, the statement will output `false`.

---

INPUT/OUTPUT

Input

Since there are so many ways to provide input to a program, user input is not a part of the AP Java subset. If reading input is a necessary part of a question on the AP exam, it will be indicated something like this:

```java
double x = call to a method that reads a floating-point number
```

or

```java
double x = IO.readDouble(); //read user input
```

NOTE

The Scanner class (since Java 5.0) simplifies both console and file input. It will not, however, be tested on the AP exam.

Output

Testing of output will be restricted to `System.out.print` and `System.out.println`. Formatted output will not be tested.

`System.out` is an object in the `System` class that allows output to be displayed on the screen. The `println` method outputs an item and then goes to a new line. The `print` method outputs an item without going to a new line afterward. An item to be printed can be a string, or a number, or the value of a boolean expression (`true` or `false`). Here are some examples:
Chapter 1 Introductory Java Language Features

```java
System.out.print("Hot");
System.out.println("dog"); } prints Hotdog

System.out.println("Hot");
System.out.println("dog"); } prints Hot
dog
System.out.println(7 + 3); } prints 10
System.out.println(7 == 2 + 5); } prints true

int x = 27;
System.out.println(x); } prints 27
System.out.println("Value of x is " + x);
prints Value of x is 27
```

In the last example, the value of \( x \), 27, is converted to the string "27", which is then concatenated to the string "Value of x is ".

To print the "values" of user-defined objects, the toString() method is invoked (see p. 175).

**Escape Sequences**

An escape sequence is a backslash followed by a single character. It is used to print special characters. The three escape sequences that you should know for the AP exam are

<table>
<thead>
<tr>
<th>Escape Sequence</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>\n</td>
<td>newline</td>
</tr>
<tr>
<td>&quot;</td>
<td>double quote</td>
</tr>
<tr>
<td>\</td>
<td>backslash</td>
</tr>
</tbody>
</table>

Here are some examples:

```java
System.out.println("Welcome to\na new line");
```

prints

```
Welcome to
a new line
```

The statement

```java
System.out.println("He is known as \"Hothead Harry\". ");
```

prints

```
He is known as "Hothead Harry".
```

The statement

```java
System.out.println("The file path is d:\myFiles\.. ");
```

prints

```
The file path is d:\myFiles\..
```
CONTROL STRUCTURES

Control structures are the mechanism by which you make the statements of a program run in a nonsequential order. There are two general types: decision making and iteration.

Decision-Making Control Structures

These include the if, if...else, and switch statements. They are all selection control structures that introduce a decision-making ability into a program. Based on the truth value of a boolean expression, the computer will decide which path to follow. The switch statement is not part of the AP Java subset.

THE if STATEMENT

```java
if (boolean expression)
{
    statements
}
```

Here the statements will be executed only if the boolean expression is true. If it is false, control passes immediately to the first statement following the if statement.

THE if...else STATEMENT

```java
if (boolean expression)
{
    statements
}
else
{
    statements
}
```

Here, if the boolean expression is true, only the statements immediately following the test will be executed. If the boolean expression is false, only the statements following the else will be executed.

NESTED if STATEMENT

If the statement part of an if statement is itself an if statement, the result is a nested if statement.

Example 1

```java
if (boolean expr1)
    if (boolean expr2)
        statement;
```

This is equivalent to

```java
if (boolean expr1 && boolean expr2)
    statement;
```
Example 2

Beware the dangling else! Suppose you want to read in an integer and print it if it’s positive and even. Will the following code do the job?

```java
int n = IO.readInt(); //read user input
if (n > 0)
    if (n % 2 == 0)
        System.out.println(n);
    else
        System.out.println(n + " is not positive");
```

A user enters 7 and is surprised to see the output

```
7 is not positive
```

The reason is that else always gets matched with the nearest unpaired if, not the first if as the indenting would suggest.

There are two ways to fix the preceding code. The first is to use {} delimiters to group the statements correctly.

```java
int n = IO.readInt(); //read user input
if (n > 0)
{
    if (n % 2 == 0)
        System.out.println(n);
}
else
    System.out.println(n + " is not positive");
```

The second way of fixing the code is to rearrange the statements.

```java
int n = IO.readInt(); //read user input
if (n <= 0)
    System.out.println(n + " is not positive");
else
    if (n % 2 == 0)
        System.out.println(n);
```

EXTENDED if STATEMENT

For example,

```java
String grade = IO.readString(); //read user input
if (grade.equals("A"))
    System.out.println("Excellent!");
else if (grade.equals("B"))
    System.out.println("Good");
else if (grade.equals("C") || grade.equals("D"))
    System.out.println("Poor");
else if (grade.equals("F"))
    System.out.println("Egregious!");
else
    System.out.println("Invalid grade");
```

If any of A, B, C, D, or F are entered, an appropriate message will be written, and control will go to the statement immediately following the extended if statement. If any other string is entered, the final else is invoked, and the message Invalid grade will be written.
Iteration

Java has three different control structures that allow the computer to perform iterative
tasks: the for loop, while loop, and do...while loop. The do...while loop is not in
the AP Java subset.

THE for LOOP

The general form of the for loop is

```
for (initialization; termination condition; update statement)
{
  statements //body of loop
}
```

The termination condition is tested at the top of the loop; the update statement is
performed at the bottom.

Example 1

```java
//outputs 1 2 3 4
for (i = 1; i < 5; i++)
  System.out.print(i + " ");
```

Here’s how it works. The loop variable i is initialized to 1, and the termination con-
dition i < 5 is evaluated. If it is true, the body of the loop is executed, and then the
loop variable i is incremented according to the update statement. As soon as the termi-
nation condition is false (i.e., i >= 5), control passes to the first statement following
the loop.

Example 2

```java
//outputs 20 19 18 17 16 15
for (k = 20; k >= 15; k--)
  System.out.print(k + " ");
```

Example 3

```java
//outputs 2 4 6 8 10
for (j = 2; j <= 10; j += 2)
  System.out.print(j + " ");
```

NOTE

1. The loop variable should not have its value changed inside the loop body.
2. The initializing and update statements can use any valid constants, variables,
or expressions.
3. The scope (see p. 100) of the loop variable can be restricted to the loop body by
   combining the loop variable declaration with the initialization. For example,
   ```java
   for (int i = 0; i < 3; i++)
   {
     ...
   }
   ```
4. The following loop is syntactically valid:
for (int i = 1; i <= 0; i++)
{
   ...
}

The loop body will not be executed at all, since the exiting condition is true before the first execution.

THE FOR-EACH LOOP

This is used to iterate over an array or collection. The general form of the loop is

```java
for (SomeType element : collection)
{
   statements
}
```

(Read the top line as “For each element of type SomeType in collection...”)

**Example**

```java
//Outputs all elements of arr, one per line.
for (int element : arr)
   System.out.println(element);
```

**NOTE**

1. The for-each loop cannot be used for replacing or removing elements as you traverse.
2. The loop hides the index variable that is used with arrays.

THE while LOOP

The general form of the while loop is

```java
while (boolean test)
{
   statements        //loop body
}
```

The boolean test is performed at the beginning of the loop. If true, the loop body is executed. Otherwise, control passes to the first statement following the loop. After execution of the loop body, the test is performed again. If true, the loop is executed again, and so on.

**Example 1**

```java
int i = 1, mult3 = 3;
while (mult3 < 20)
{
   System.out.print(mult3 + " ");
   i++;
   mult3 *= i;
}          //outputs 3 6 18
```
NOTE

1. It is possible for the body of a while loop never to be executed. This will happen if the test evaluates to false the first time.
2. Disaster will strike in the form of an infinite loop if the test can never be false. Don't forget to change the loop variable in the body of the loop in a way that leads to termination!

Example 2

```java
int power2 = 1;
while (power2 != 20)
{
    System.out.println(power2);
    power2 *= 2;
}
```

Since power2 will never exactly equal 20, the loop will grind merrily along eventually causing an integer overflow.

Example 3

```java
/* Screen out bad data.
 * The loop won't allow execution to continue until a valid
 * integer is entered.
 */
System.out.println("Enter a positive integer from 1 to 100");
int num = IO.readInt(); //read user input
while (num < 1 || num > 100)
{
    System.out.println("Number must be from 1 to 100.");
    System.out.println("Please reenter");
    num = IO.readInt();
}
```

Example 4

```java
/* Uses a sentinel to terminate data entered at the keyboard.
 * The sentinel is a value that cannot be part of the data.
 * It signals the end of the list.
 */
final int SENTINEL = -999;
System.out.println("Enter list of positive integers," +
    " end list with " + SENTINEL);
int value = IO.readInt(); //read user input
while (value != SENTINEL)
{
    process the value
    value = IO.readInt(); //read another value
}
NESTED LOOPS

You create a **nested loop** when a loop is a statement in the body of another loop.

**Example 1**

```java
for (int k = 1; k <= 3; k++)
{
    for (int i = 1; i <= 4; i++)
        System.out.print('*');
    System.out.println();
}
```

Think:

- For each of 3 rows
  - Print 4 stars
  - Go to next line

Output:

```
****
****
****
```

**Example 2**

This example has two loops nested in an outer loop.

```java
for (int i = 1; i <= 6; i++)
{
    for (int j = 1; j <= i; j++)
        System.out.print('+');
    for (int j = 1; j <= 6 - i; j++)
        System.out.print('*');
    System.out.println();
}
```

Output:

```
+*****
++****
+++***
++++**
+++++*
++++++
```

ERRORS AND EXCEPTIONS

An **exception** is an error condition that occurs during the execution of a Java program. For example, if you divide an integer by zero, an `ArithmeticException` will be thrown. If you use a negative array index, an `ArrayIndexOutOfBoundsException` will be thrown.
Errors and Exceptions

An *unchecked exception* is one where you don’t provide code to deal with the error. Such exceptions are automatically handled by Java’s standard exception-handling methods, which terminate execution. You now need to fix your code!

A *checked exception* is one where you provide code to handle the exception, either a `try/catch/finally` statement, or an explicit `throw` clause. These exceptions are not necessarily caused by an error in the code. For example, an unexpected end-of-file could be due to a broken network connection. Checked exceptions are not part of the AP Java subset.

The following exceptions are in the AP Java subset:

<table>
<thead>
<tr>
<th>Exception</th>
<th>Discussed on page</th>
</tr>
</thead>
<tbody>
<tr>
<td>ArithmeticException</td>
<td>on the previous page</td>
</tr>
<tr>
<td>NullPointerException</td>
<td>103</td>
</tr>
<tr>
<td>ClassCastException</td>
<td>142</td>
</tr>
<tr>
<td>ArrayIndexOutOfBoundsException</td>
<td>233</td>
</tr>
<tr>
<td>IndexOutOfBoundsException</td>
<td>244</td>
</tr>
<tr>
<td>IllegalArgumentException</td>
<td>this page</td>
</tr>
</tbody>
</table>

See also `NoSuchElementException` (pp. 247, 248) and `IllegalStateException` (pp. 247, 249), which refer to iterators, an optional topic.

Java allows you to write code that throws a standard unchecked exception. Here are typical examples:

**Example 1**

```java
if (numScores == 0)
    throw new ArithmeticException("Cannot divide by zero");
else
    findAverageScore();
```

**Example 2**

```java
public void setRadius(int newRadius)
{
    if (newRadius < 0)
        throw new IllegalArgumentException("Radius cannot be negative");
    else
        radius = newRadius;
}
```

**NOTE**

1. `throw` and `new` are both reserved words.
2. The error message is optional: The line in Example 1 could have read
   ```java
   throw new ArithmeticException();
   ```
   The message, however, is useful, since it tells the person running the program what went wrong.
3. A `IllegalArgumentException` is thrown to indicate that a parameter does not satisfy a method’s precondition.
Chapter 1  Introductory Java Language Features

Chapter Summary

Be sure that you understand the difference between primitive and user-defined types and between the following types of operators: arithmetic, relational, logical, and assignment. Know which conditions lead to what types of errors.

You should be able to work with numbers—know how to compare them and how to convert between decimal, binary, and hexadecimal numbers. Know how integers and floating-point numbers are stored in memory, and be aware of the conditions that can lead to round-off error.

You should know the Integer constants Integer.MIN_VALUE and Integer.MAX_VALUE.

Be familiar with each of the following control structures: conditional statements, for loops, while loops, and for-each loops.

Be aware of the AP exam expectations concerning input and output.
MULTIPLE-CHOICE QUESTIONS ON INTRODUCTORY JAVA LANGUAGE CONCEPTS

1. Which of the following pairs of declarations will cause an error message?

   I  double x = 14.7;
      int y = x;

   II double x = 14.7;
      int y = (int) x;

   III int x = 14;
      double y = x;

(A) None
(B) I only
(C) II only
(D) III only
(E) I and III only

2. What output will be produced by

   System.out.print("/* This is not
   a comment */");

(A) * This is not a comment *
(B) /* This is not a comment */
(C) * This is not
   a comment *
(D) /** This is not
    a comment */
(E) /* This is not
   a comment */

3. Consider the following code segment

   if (n != 0 && x / n > 100)
      statement1;
   else
      statement2;

If n is of type int and has a value of 0 when the segment is executed, what will happen?

(A) An ArithmeticException will be thrown.
(B) A syntax error will occur.
(C) statement1, but not statement2, will be executed.
(D) statement2, but not statement1, will be executed.
(E) Neither statement1 nor statement2 will be executed; control will pass to the first statement following the if statement.
4. Refer to the following code fragment:

```java
double answer = 13 / 5;
System.out.println("13 / 5 = " + answer);
```

The output is

```
13 / 5 = 2.0
```

The programmer intends the output to be

```
13 / 5 = 2.6
```

Which of the following replacements for the first line of code will not fix the problem?

- (A) `double answer = (double) 13 / 5;`
- (B) `double answer = 13 / (double) 5;`
- (C) `double answer = 13.0 / 5;`
- (D) `double answer = 13 / 5.0;`
- (E) `double answer = (double) (13 / 5);`

5. What value is stored in `result` if

```java
int result = 13 - 3 * 6 / 4 % 3;
```

(A) $-5$

(B) 0

(C) 13

(D) $-1$

(E) 12

6. Suppose that addition and subtraction had higher precedence than multiplication and division. Then the expression

```
2 + 3 * 12 / 7 - 4 + 8
```

would evaluate to which of the following?

- (A) 11
- (B) 12
- (C) 5
- (D) 9
- (E) $-4$

7. Which is true of the following boolean expression, given that `x` is a variable of type `double`?

```java
3.0 == x * (3.0 / x)
```

- (A) It will always evaluate to false.
- (B) It may evaluate to false for some values of `x`.
- (C) It will evaluate to false only when `x` is zero.
- (D) It will evaluate to false only when `x` is very large or very close to zero.
- (E) It will always evaluate to true.
8. Let \( x \) be a variable of type \texttt{double} that is positive. A program contains the boolean expression \((\text{Math.pow}(x,0.5) == \text{Math.sqrt}(x))\). Even though \( x^{1/2} \) is mathematically equivalent to \( \sqrt{x} \), the above expression returns the value \texttt{false} in a student’s program. Which of the following is the most likely reason?

(A) \texttt{Math.pow} returns an \texttt{int}, while \texttt{Math.sqrt} returns a \texttt{double}.
(B) \( x \) was imprecisely calculated in a previous program statement.
(C) The computer stores floating-point numbers with 32-bit words.
(D) There is round-off error in calculating the \texttt{pow} and \texttt{sqrt} functions.
(E) There is overflow error in calculating the \texttt{pow} function.

9. What will the output be for the following poorly formatted program segment, if the input value for \( \texttt{num} \) is 22?

```java
int num = call to a method that reads an integer;
if (num > 0)
  if (num \% 5 == 0)
    System.out.println(num);
  else System.out.println(num + " is negative");

(A) 22
(B) 4
(C) 2 is negative
(D) 22 is negative
(E) Nothing will be output.
```

10. What values are stored in \( x \) and \( y \) after execution of the following program segment?

```java
int x = 30, y = 40;
if (x >= 0)
  {
    if (x <= 100)
      {
        y = x * 3;
        if (y < 50)
          x /= 10;
        }
    else
      y = x * 2;
  }
else
  y = -x;

(A) x = 30 y = 90
(B) x = 30 y = -30
(C) x = 30 y = 60
(D) x = 3 y = -3
(E) x = 30 y = 40
```
11. Which of the following will evaluate to true only if boolean expressions A, B, and C are all false?
   (A) !A && !(B && !C)
   (B) !A || !B || !C
   (C) !(A || B || C)
   (D) !(A && B && C)

12. Assume that a and b are integers. The boolean expression

     !(a <= b) && (a * b > 0)

will always evaluate to true given that
(A) a = b
(B) a > b
(C) a < b
(D) a > b and b > 0
(E) a > b and b < 0

13. Given that a, b, and c are integers, consider the boolean expression

     (a < b) || !(((c == a * b) && (c < a)))

Which of the following will guarantee that the expression is true?
(A) c < a is false.
(B) c < a is true.
(C) a < b is false.
(D) c == a * b is true.
(E) c == a * b is true, and c < a is true.

14. In the following code segment, you may assume that a, b, and n are all type int.

     if (a != b && n / (a - b) > 90)
     {
         /* statement 1 */
     }
     else
     {
         /* statement 2 */
     }
     /* statement 3 */

What will happen if a == b is false?
(A) /* statement 1 */ will be executed.
(B) /* statement 2 */ will be executed.
(C) Either /* statement 1 */ or /* statement 2 */ will be executed.
(D) A compile-time error will occur.
(E) An exception will be thrown.
15. Given that \( n \) and \( \text{count} \) are both of type \textit{int}, which statement is true about the following code segments?

- I  
  \[
  \text{for (count = 1; count <= n; count++)} \\
  \hspace{1cm} \text{System.out.println(count);} 
  \]

- II  
  \[
  \text{count = 1;} \\
  \text{while (count <= n)} \\
  \hspace{1cm} \{ \\
  \hspace{2cm} \text{System.out.println(count);} \\
  \hspace{2cm} \text{count++;} \\
  \hspace{1cm} \} 
  \]

(A) I and II are exactly equivalent for all input values \( n \).
(B) I and II are exactly equivalent for all input values \( n \geq 1 \), but differ when \( n \leq 0 \).
(C) I and II are exactly equivalent only when \( n = 0 \).
(D) I and II are exactly equivalent only when \( n \) is even.
(E) I and II are not equivalent for any input values of \( n \). 

16. The following fragment intends that a user will enter a list of positive integers at the keyboard and terminate the list with a sentinel:

\[
\text{int value = 0;} \\
\text{final int SENTINEL = -999;} \\
\text{while (value != SENTINEL)} \\
\hspace{1cm} \{ \\
\hspace{2cm} \text{//code to process value} \\
\hspace{2cm} \ldots \\
\hspace{2cm} \text{value = IO.readInt();} \quad \text{//read user input} \\
\hspace{1cm} \} 
\]

The fragment is not correct. Which is a true statement?
(A) The sentinel gets processed.
(B) The last nonsentinel value entered in the list fails to get processed.
(C) A poor choice of SENTINEL value causes the loop to terminate before all values have been processed.
(D) The code will always process a value that is not on the list.
(E) Entering the SENTINEL value as the first value causes a run-time error.

17. Suppose that base-2 (binary) numbers and base-16 (hexadecimal) numbers can be denoted with subscripts, as shown below:

\[
2A_{\text{hex}} = 101010_{\text{bin}} 
\]

Which is equal to \( 3D_{\text{hex}} \)?
(A) \( 111101_{\text{bin}} \)
(B) \( 101111_{\text{bin}} \)
(C) \( 10011_{\text{bin}} \)
(D) \( 110100_{\text{bin}} \)
(E) \( 101101_{\text{bin}} \)
18. A common use of hexadecimal numerals is to specify colors on web pages. Every color has a red, green, and blue component. In decimal notation, these are denoted with an ordered triple \((x, y, z)\), where \(x\), \(y\), and \(z\) are the three components, each an int from 0 to 255. For example, a certain shade of red, whose red, green, and blue components are 238, 9, and 63, is represented as \((238, 9, 63)\).

In hexadecimal, a color is represented in the format \#RRGGBB, where \(RR\), \(GG\), and \(BB\) are hex values for the red, green, and blue. Using this notation, the color \((238, 9, 63)\) would be coded as \#EE093F.

Which of the following hex codes represents the color \((14, 20, 255)\)?
(A) \#1418FE
(B) \#0E20FE
(C) \#0E14FF
(D) \#0FE5FE
(E) \#0D14FF

19. In Java, a variable of type \texttt{int} is represented internally as a 32-bit signed integer. Suppose that one bit stores the sign, and the other 31 bits store the magnitude of the number in base 2. In this scheme, what is the largest value that can be stored as type \texttt{int}?
(A) \(2^{32}\)
(B) \(2^{32} - 1\)
(C) \(2^{31}\)
(D) \(2^{31} - 1\)
(E) \(2^{30}\)

20. Consider this code segment:

```java
int x = 10, y = 0;
while (x > 5)
{
    y = 3;
    while (y < x)
    {
        y *= 2;
        if (y % x == 1)
            y += x;
    }
    x -= 3;
}
System.out.println(x + " "+ y);
```

What will be output after execution of this code segment?
(A) 1 6
(B) 7 12
(C) -3 12
(D) 4 12
(E) -3 6
Questions 21 and 22 refer to the following method, checkNumber, which checks the validity of its four-digit integer parameter.

```java
/** @param n a 4-digit integer
 * @return true if n is valid, false otherwise
 */
boolean checkNumber(int n)
{
    int d1,d2,d3,checkDigit,nRemaining,rem;
    //strip off digits
    checkDigit = n % 10;
    nRemaining = n / 10;
    d3 = nRemaining % 10;
    nRemaining /= 10;
    d2 = nRemaining % 10;
    nRemaining /= 10;
    d1 = nRemaining % 10;
    //check validity
    rem = (d1 + d2 + d3) % 7;
    return rem == checkDigit;
}
```

A program invokes method checkNumber with the statement

```java
boolean valid = checkNumber(num);
```

21. Which of the following values of num will result in valid having a value of true?
   (A) 6143
   (B) 6144
   (C) 6145
   (D) 6146
   (E) 6147

22. What is the purpose of the local variable nRemaining?
   (A) It is not possible to separate n into digits without the help of a temporary variable.
   (B) nRemaining prevents the parameter num from being altered.
   (C) nRemaining enhances the readability of the algorithm.
   (D) On exiting the method, the value of nRemaining may be reused.
   (E) nRemaining is needed as the left-hand side operand for integer division.
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23. What output will be produced by this code segment? (Ignore spacing.)

```java
for (int i = 5; i >= 1; i--)
{
    for (int j = i; j >= 1; j--)
    {
        System.out.print(2 * j - 1);
    }
    System.out.println();
}
```

(A) 9 7 5 3 1  
    9 7 5 3  
    9 7 5  
    9 7  
    9

(B) 9 7 5 3 1  
    7 5 3 1  
    5 3 1  
    3 1  
    1

(C) 9 7 5 3 1  
    7 5 3 1 -1  
    5 3 1 -1 -3  
    3 1 -1 -3 -5  
    1 -1 -3 -5 -7

(D) 1  
    1 3  
    1 3 5  
    1 3 5 7  
    1 3 5 7 9

(E) 1 3 5 7 9  
    1 3 5 7  
    1 3 5  
    1 3  
    1
24. Which of the following program fragments will produce this output? (Ignore spacing.)

```
2 - - - -
- 4 - - -
- - 6 - -
- - 8 - -
- - - 10 -
- - - - 12
```

I
```java
for (int i = 1; i <= 6; i++)
{
    for (int k = 1; k <= 6; k++)
        if (k == i)
            System.out.print(2 * k);
        else
            System.out.print("-");
    System.out.println();
}
```

II
```java
for (int i = 1; i <= 6; i++)
{
    for (int k = 1; k <= i - 1; k++)
        System.out.print("-");
    System.out.print(2 * i);
    for (int k = 1; k <= 6 - i; k++)
        System.out.print("-");
    System.out.println();
}
```

III
```java
for (int i = 1; i <= 6; i++)
{
    for (int k = 1; k <= i - 1; k++)
        System.out.print("-");
    System.out.print(2 * i);
    for (int k = i + 1; k <= 6; k++)
        System.out.print("-");
    System.out.println();
}
```

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
25. Consider this program segment:

```java
int newNum = 0, temp;
int num = k;          //k is some predefined integer value ≥ 0
while (num > 10)
{
    temp = num % 10;
    num /= 10;
    newNum = newNum * 10 + temp;
}
System.out.print(newNum);
```

Which is a true statement about the segment?

I If $100 \leq \text{num} \leq 1000$ initially, the final value of newNum must be in the range $10 \leq \text{newNum} \leq 100$.

II There is no initial value of num that will cause an infinite while loop.

III If num ≤ 10 initially, newNum will have a final value of 0.

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III
26. Consider the method `reverse`:

```java
/** Precondition: n > 0.
 * Postcondition:
 * - Returns n with its digits reversed.
 * - Example: If n = 234, method reverse returns 432.
 * @param n a positive integer
 * @return n with its digits reversed */
int reverse(int n)
{
    int rem, revNum = 0;

    /* code segment */
    return revNum;
}
```

Which of the following replacements for `/* code segment */` would cause the method to work as intended?

I for (int i = 0; i <= n; i++)
{
    rem = n % 10;
    revNum = revNum * 10 + rem;
    n /= 10;
}

II while (n != 0)
{
    rem = n % 10;
    revNum = revNum * 10 + rem;
    n /= 10;
}

III for (int i = n; i != 0; i /= 10)
{
    rem = i % 10;
    revNum = revNum * 10 + rem;
}

(A) I only
(B) II only
(C) I and II only
(D) II and III only
(E) I and III only
ANSWER KEY

2. E 11. C 20. D
9. D

ANSWERS EXPLAINED

1. (B) When x is converted to an integer, as in segment I, information is lost. Java requires that an explicit cast to an int be made, as in segment II. Note that segment II will cause x to be truncated: The value stored in y is 14. By requiring the explicit cast, Java doesn’t let you do this accidentally. In segment III y will contain the value 14.0. No explicit cast to a double is required since no information is lost.

2. (E) The string argument contains two escape sequences: ‘\’, which means print a backslash (\), and ‘\n’, which means go to a new line. Choice E is the only choice that does both of these.

3. (D) Short-circuit evaluation of the boolean expression will occur. The expression (n != 0) will evaluate to false, which makes the entire boolean expression false. Therefore the expression (x / n > 100) will not be evaluated. Hence no division by zero will occur, causing an ArithmeticException to be thrown. When the boolean expression has a value of false, only the else part of the statement, statement2, will be executed.

4. (E) For this choice, the integer division 13/5 will be evaluated to 2, which will then be cast to 2.0. The output will be 13/5 = 2.0. The compiler needs a way to recognize that real-valued division is required. All the other options provide a way.

5. (E) The operators *, /, and % have equal precedence, all higher than -, and must be performed first, from left to right.

\[
13 - 3 * 6 / 4 \% 3 \\
= 13 - 18 / 4 \% 3 \\
= 13 - 4 \% 3 \\
= 13 - 1 \\
= 12
\]

6. (C) The expression must be evaluated as if parenthesized like this:
\[(2 + 3) \times 12 / (7 - 4 + 8)\]

This becomes \(5 \times 12 / 11 = 60 / 11 = 5\).

7. (B) Although the expression is always algebraically true for nonzero \(x\), the expression may evaluate to false. This could occur because of round-off error in performing the division and multiplication operations. Whether the right-hand side of the expression evaluates to exactly 3.0 depends on the value of \(x\). Note that if \(x\) is zero, the expression will be evaluated to false because the right-hand side will be assigned a value of Infinity.

8. (D) Anytime arithmetic operations are done with floating-point numbers, round-off error occurs. The Math class methods (see p. 183) such as \(\text{pow}\) and \(\sqrt{\text{r}}\) use various approximations to generate their answers to the required accuracy. Since they do different internal arithmetic, however, the round-off will usually not result in exactly the same answers. Note that choice A is not correct because both Math.\(\text{pow}\) and Math.\(\sqrt{\text{r}}\) return type double. Choice B is wrong because no matter how \(x\) was previously calculated, the same \(x\) is input to \(\text{pow}\) and \(\sqrt{\text{r}}\). Choice C is wrong since round-off error occurs no matter how many bits are used to represent numbers. Choice E is wrong because if \(x\) is representable on the machine (i.e., hasn’t overflowed), then its square root, \(x^{1/2}\), will not overflow.

9. (D) Each else gets paired with the nearest unpaired if. Thus when the test \((22 \% 5 == 0)\) fails, the else part indicating that 22 is negative will be executed. This is clearly not the intent of the fragment, which can be fixed using delimiters:

```java
    int num = call to a method that reads an integer;
    if (num > 0)
    {
        if (num \% 5 == 0)
            System.out.println(num);
    }
    else
        System.out.println(num + " is negative");
```

10. (A) Since the first test \((x >= 0)\) is true, the matching else part, \(y = -x\), will not be executed. Since \((x <= 100)\) is true, the matching else part, \(y = x * 2\), will not be executed. The variable \(y\) will be set to \(x * 3\) (i.e., 90) and will now fail the test \(y < 50\). Thus, \(x\) will never be altered in this algorithm. Final values are \(x = 30\) and \(y = 90\).

11. (C) In order for \(! (A || B || C)\) to be true, \((A || B || C)\) must evaluate to false. This will happen only if \(A, B,\) and \(C\) are all false. Choice A evaluates to true when \(A\) and \(B\) are false and \(C\) is true. In choice B, if any one of \(A, B,\) or \(C\) is false, the boolean expression evaluates to true. In choice D, if any one of \(A, B,\) or \(C\) is false, the boolean expression evaluates to true since we have \(! (false)\). All that's required for choice E to evaluate to true is for \(A\) to be false. Since \(true || (any)\) evaluates to true, both \(B\) and \(C\) can be either true or false.

12. (D) To evaluate to true, the expression must reduce to true \&\& true. We therefore need \(! (false) \&\& true\). Choice D is the only condition that guarantees this: \(a > b\) provides \(! (false)\) for the left-hand expression, and \(a > b\) and \(b > 0\) implies both \(a\) and \(b\) positive, which leads to true for the right-hand expression. Choice E, for example, will provide true for the right-hand expression only if \(a < 0\). You have no information about \(a\) and can’t make assumptions about it.
13. (A) If \((c < a)\) is \textit{false}, \((((c == a*b) \&\& (c < a))\) evaluates to \textit{false} irrespective of the value of \(c == a*b\). In this case, \(!((c == a*b) \&\& c < a))\) evaluates to \textit{true}. Then \((a < b) \mid\mid \text{true}\) evaluates to \textit{true} irrespective of the value of the test \((a < b)\). In all the other choices, the given expression \textit{may} be \textit{true}. There is not enough information given to guarantee this, however.

14. (C) If \(a == b\) is \textit{false}, then \(a != b\) is \textit{true}. Thus, the second piece of the compound test must be evaluated before the value of the whole test is known. Since \(a == b\) is \textit{false}, \(a - b\) is not equal to zero. Thus, there is no division by zero, and no exception will be thrown. Also, since the relative values of \(a\), \(b\), and \(n\) are unknown, the value of the test \(n / (a - b) > 90\) is unknown, and there is insufficient information to determine whether the compound test is \textit{true} or \textit{false}. Thus, either \(/\ast\ \text{statement 1} \ast/\) or \(/\ast\ \text{statement 2} \ast/\) will be executed.

15. (A) If \(n \geq 1\), both segments will print out the integers from 1 through \(n\). If \(n \leq 0\), both segments will fail the test immediately and do nothing.

16. (D) The \((\text{value} != \text{SENTINEL})\) test occurs before a value has been read from the list. This will cause 0 to be processed, which may cause an error. The code must be fixed by reading the first value before doing the test:

```java
final int SENTINEL = -999;
int value = IO.readInt();
while (value != SENTINEL)
{
    //code to process value
    value = IO.readInt();
}
```

17. (A) Quick method: Convert each hex digit to binary.

\[
\begin{align*}
3 & \quad D_{\text{hex}} \\
0011 & \quad 1101 \\
& \quad = 111101_{\text{bin}} \\
\end{align*}
\]

Slow method: Convert \(3D_{\text{hex}}\) to base 10.

\[
3D_{\text{hex}} = (3)(16^1) + (D)(16^0) = 48 + 13 = 61_{\text{dec}}
\]

Now convert \(61_{\text{dec}}\) to binary. Write 61 as a sum of descending powers of 2:

\[
61 = 32 + 16 + 8 + 4 + 1 \\
= 1(2^5) + 1(2^4) + 1(2^3) + 1(2^2) + 0(2^1) + 1(2^0) \\
= 111101_{\text{bin}}
\]

18. (C) Start by converting each of the three numbers to hexadecimal:

\[
\begin{align*}
14 & \quad = (0)(16^1) + (14)(16^0) = \text{0E} \\
20 & \quad = (1)(16^1) + (4)(16^0) = 14 \\
255 & \quad = (15)(16^1) + (15)(16^0) = \text{FF}
\end{align*}
\]

Therefore \((14, 20, 255) = \#0E14FF\).
19. (D) Think of the integer as having 31 slots for storage. If there were just one slot, the maximum binary number would be \(1 = 2^1 - 1\). If there were just two slots, the maximum binary number would be \(11 = 2^2 - 1 = 3\). If there were just eight slots, the maximum binary number would be \(1111111 = 2^8 - 1\). So for 31 slots, the maximum value is \(2^{31} - 1\).

20. (D) Here is a trace of the values of \(x\) and \(y\) during execution. Note that the condition \((y \% x == 1)\) is never true in this example.

<table>
<thead>
<tr>
<th></th>
<th>x</th>
<th>10</th>
<th>7</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>3</td>
<td>6</td>
<td>12</td>
<td>3</td>
</tr>
</tbody>
</table>

The while loop terminates when \(x\) is 4 since the test while \((x > 5)\) fails.

21. (B) The algorithm finds the remainder when the sum of the first three digits of \(n\) is divided by 7. If this remainder is equal to the fourth digit, checkDigit, the method returns true, otherwise false. Note that \((6+1+4) \% 7\) equals 4. Thus, only choice B is a valid number.

22. (C) As \(n\) gets broken down into its digits, \(n\text{remaining}\) is the part of \(n\) that remains after each digit is stripped off. Thus, \(n\text{remaining}\) is a self-documenting name that helps describe what is happening. Choice A is false because every digit can be stripped off using some sequence of integer division and mod. Choice B is false because \(n\text{num}\) is passed by value and therefore will not be altered when the method is exited (see p. 104). Eliminate choice D: When the method is exited, all local variables are destroyed. Choice E is nonsense.

23. (B) The outer loop produces five rows of output. Each pass through the inner loop goes from \(i\) down to 1. Thus five odd numbers starting at 9 are printed in the first row, four odd numbers starting at 7 in the second row, and so on.

24. (E) All three algorithms produce the given output. The outer for (int \(i\) ...) loop produces six rows, and the inner for (int \(k\) ...) loops produce the symbols in each row.

25. (D) Statement I is false, since if \(100 \leq \text{num} \leq 109\), the body of the while loop will be executed just once. (After this single pass through the loop, the value of \(\text{num}\) will be 10, and the test if \((\text{num} > 10)\) will fail.) With just one pass, \(\text{newNum}\) will be a one-digit number, equal to \(\text{temp}\) (which was the original \(\text{num} \% 10\)). Note that statement II is true: There cannot be an infinite loop since \(\text{num} /= 10\) guarantees termination of the loop. Statement III is true because if \(\text{num} \leq 10\), the loop will be skipped, and \(\text{newNum}\) will keep its original value of 0.

26. (D) The algorithm works by stripping off the rightmost digit of \(n\) (stored in \(\text{rem}\), multiplying the current value of \(\text{revNum}\) by 10, and adding that rightmost digit. When \(n\) has been stripped down to no digits (i.e., \(n == 0\) is true), \(\text{revNum}\) is complete. Both segments II and III work. Segment I fails to produce the right output whenever the input value \(n\) has first digit less than \((\text{number of digits} - 1)\). For these cases the output has the first digit of the original number missing from the end of the returned number.
Classes and Objects

Chapter Goals

• Objects and classes
• Encapsulation
• References
• Keywords public, private, and static
• Methods
• Scope of variables

OBJECTS

Every program that you write involves at least one thing that is being created or manipulated by the program. This thing, together with the operations that manipulate it, is called an object.

Consider, for example, a program that must test the validity of a four-digit code number that a person will enter to be able to use a photocopy machine. Rules for validity are provided. The object is a four-digit code number. Some of the operations to manipulate the object could be readNumber, getSeparateDigits, testValidity, and writeNumber.

Any given program can have several different types of objects. For example, a program that maintains a database of all books in a library has at least two objects:

1. A Book object, with operations like getTitle, isOnShelf, isFiction, and goOutOfPrint.
2. A ListOfBooks object, with operations like search, addBook, removeBook, and sortByAuthor.

An object is characterized by its state and behavior. For example, a book has a state described by its title, author, whether it’s on the shelf, and so on. It also has behavior, like going out of print.

Notice that an object is an idea, separate from the concrete details of a programming language. It corresponds to some real-world object that is being represented by the program.
All object-oriented programming languages have a way to represent an object as a variable in a program. In Java, a variable that represents an object is called an object reference.

**CLASSES**

A *class* is a software blueprint for implementing objects of a given type. An object is a single *instance* of the class. In a program there will often be several different instances of a given class type.

The current state of a given object is maintained in its *data fields* or *instance variables*, provided by the class. The *methods* of the class provide both the behaviors exhibited by the object and the operations that manipulate the object. Combining an object’s data and methods into a single unit called a class is known as *encapsulation*.

Here is the framework for a simple bank account class:

```java
public class BankAccount {
    private String password;
    private double balance;
    public static final double OVERDRAWN_PENALTY = 20.00;

    // constructors
    /** Default constructor. */
    public BankAccount() { /* implementation code */ }

    /** Constructs bank account with specified password and balance. */
    public BankAccount(String acctPassword, double acctBalance) {
        /* implementation code */
    }

    // accessor
    /** @return balance of this account */
    public double getBalance() {
        /* implementation code */
    }

    // mutators
    /** Deposits amount in bank account with given password. */
    public void deposit(String acctPassword, double amount) {
        /* implementation code */
    }

    /** Withdraws amount from bank account with given password. */
    public void withdraw(String acctPassword, double amount) {
        /* implementation code */
    }
}
```
Chapter 2  Classes and Objects

PUBLIC, PRIVATE, AND STATIC

The keyword public preceding the class declaration signals that the class is usable by all client programs. If a class is not public, it can be used only by classes in its own package. In the AP Java subset, all classes are public.

Similarly, public methods are accessible to all client programs. Clients, however, are not privy to the class implementation and may not access the private instance variables and private methods of the class. Restriction of access is known as information hiding. In Java, this is implemented by using the keyword private. Private methods and variables in a class can be accessed only by methods of that class. Even though Java allows public instance variables, in the AP Java subset all instance variables are private.

A static variable (class variable) contains a value that is shared by all instances of the class. “Static” means that memory allocation happens once.

Typical uses of a static variable are to

- keep track of statistics for objects of the class.
- accumulate a total.
- provide a new identity number for each new object of the class.

For example:

```java
public class Employee {
    private String name;
    private static int employeeCount = 0; //number of employees

    public Employee( < parameter list > )
    {
        < initialization of private instance variables >
        employeeCount++; //increment count of all employees
    }

    ...
}
```

Notice that the static variable was initialized outside the constructor and that its value can be changed.

Static final variables (constants) in a class cannot be changed. They are often declared public (see some examples of Math class constants on p. 183). The variable OVERDRAWN_PENALTY is an example in the BankAccount class. Since the variable is public, it can be used in any client method. The keyword static indicates that there is a single value of the variable that applies to the whole class, rather than a new instance for each object of the class. A client method would refer to the variable as BankAccount.OVERDRAWN_PENALTY. In its own class it is referred to as simply OVERDRAWN_PENALTY.

See p. 97 for static methods.
## METHODS

### Headers

All method headers, with the exception of constructors (see below) and static methods (p. 97), look like this:

```java
public void withdraw (String password, double amount)
```

**access specifier**  **return type**  **method name**  **parameter list**

### NOTE

1. The *access specifier* tells which other methods can call this method (see *Public*, *Private*, and *Static* on the previous page).
2. A *return type* of *void* signals that the method does not return a value.
3. Items in the *parameter list* are separated by commas.

The implementation of the method directly follows the header, enclosed in a `{}` block.

### Types of Methods

#### CONSTRUCTORS

A *constructor* creates an object of the class. You can recognize a constructor by its name—always the same as the class. Also, a constructor has no return type.

Having several constructors provides different ways of initializing class objects. For example, there are two constructors in the `BankAccount` class.

1. The *default constructor* has no arguments. It provides reasonable initial values for an object. Here is its implementation:

   ```java
   /** Default constructor.
   * Constructs a bank account with default values. */
   public BankAccount()
   {
     password = "";
     balance = 0.0;
   }
   ```

   In a client method, the declaration

   ```java
   BankAccount b = new BankAccount();
   ```

   constructs a `BankAccount` object with a balance of zero and a password equal to the empty string. The `new` operator returns the address of this newly constructed object. The variable `b` is assigned the value of this address—we say "`b` is a *reference* to the object." Picture the setup like this:
2. The constructor with parameters sets the instance variables of a BankAccount object to the values of those parameters.

Here is the implementation:

```java
/** Constructor. Constructs a bank account with specified password and balance. */
public BankAccount(String acctPassword, double acctBalance) {
    password = acctPassword;
    balance = acctBalance;
}
```

In a client program a declaration that uses this constructor needs matching parameters:

```java
BankAccount c = new BankAccount("KevinC", 800.00);
```

**NOTE**

b and c are object variables that store the addresses of their respective BankAccount objects. They do not store the objects themselves (see References on p. 101).

**ACCESSORS**

An accessor method accesses a class object without altering the object. An accessor returns some information about the object.

The BankAccount class has a single accessor method, getBalance(). Here is its implementation:

```java
/** @return the balance of this account */
public double getBalance() {
    return balance;
}
```

A client program may use this method as follows:

```java
BankAccount b1 = new BankAccount("MattW", 500.00);
BankAccount b2 = new BankAccount("DannyB", 650.50);
if (b1.getBalance() > b2.getBalance())
...
```
NOTE

The . operator (dot operator) indicates that getBalance() is a method of the class to which b1 and b2 belong, namely the BankAccount class.

MUTATORS

A mutator method changes the state of an object by modifying at least one of its instance variables.

Here are the implementations of the deposit and withdraw methods, each of which alters the value of balance in the BankAccount class:

```java
/** Deposits amount in a bank account with the given password. *
* @param acctPassword the password of this bank account *
* @param amount the amount to be deposited *
*/
public void deposit(String acctPassword, double amount)
{
    if (!acctPassword.equals(password))
        /* throw an exception */
    else
        balance += amount;
}

/** Withdraws amount from bank account with given password. *
* Assesses penalty if balance is less than amount. *
* @param acctPassword the password of this bank account *
* @param amount the amount to be withdrawn *
*/
public void withdraw(String acctPassword, double amount)
{
    if (!acctPassword.equals(password))
        /* throw an exception */
    else
    {
        balance -= amount; //allows negative balance
        if (balance < 0)
            balance -= OVERDRAWN_PENALTY;
    }
}
```

A mutator method in a client program is invoked in the same way as an accessor: using an object variable with the dot operator. For example, assuming valid BankAccount declarations for b1 and b2:

```java
b1.withdraw("MattW", 200.00);
b2.deposit("DannyB", 35.68);
```

STATIC METHODS

Static Methods vs. Instance Methods  The methods discussed in the preceding sections—constructors, accessors, and mutators—all operate on individual objects of a class. They are called instance methods. A method that performs an operation for the entire class, not its individual objects, is called a static method (sometimes called a class method).
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The implementation of a static method uses the keyword static in its header. There is no implied object in the code (as there is in an instance method). Thus, if the code tries to call an instance method or invoke a private instance variable for this nonexistent object, a syntax error will occur. A static method can, however, use a static variable in its code. For example, in the Employee example on p. 94, you could add a static method that returns the employeeCount:

```java
public static int getEmployeeCount()
{ return employeeCount; }
```

Here’s an example of a static method that might be used in the BankAccount class. Suppose the class has a static variable intRate, declared as follows:

```java
private static double intRate;
```

The static method getInterestRate may be as follows:

```java
public static double getInterestRate()
{
    System.out.println("Enter interest rate for bank account");
    System.out.println("Enter in decimal form: ");
    intRate = IO.readDouble(); // read user input
    return intRate;
}
```

Since the rate that’s read in by this method applies to all bank accounts in the class, not to any particular BankAccount object, it’s appropriate that the method should be static.

Recall that an instance method is invoked in a client program by using an object variable followed by the dot operator followed by the method name:

```java
BankAccount b = new BankAccount(); // invokes the deposit method for
b.deposit(acctPassword, amount);  // BankAccount object b
```

A static method, by contrast, is invoked by using the class name with the dot operator:

```java
double interestRate = BankAccount.getInterestRate();
```

**Static Methods in a Driver Class**  Often a class that contains the main() method is used as a driver program to test other classes. Usually such a class creates no objects of the class. So all the methods in the class must be static. Note that at the start of program execution, no objects exist yet. So the main() method must always be static.

For example, here is a program that tests a class for reading integers entered at the keyboard.

```java
import java.util.*;
public class GetListTest
{
    /** @return a list of integers from the keyboard */
    public static List<Integer> getList()
    {
        List<Integer> a = new ArrayList<Integer>();
        <code to read integers into a>
        return a;
    }
}
```
/** Write contents of List a.  
* @param a the list  
*/
public static void writeList(List<Integer> a)  
{"  
    System.out.println("List is : " + a);  
"
public static void main(String[] args)  
{"  
    List<Integer> list = getList();  
    writeList(list);  
"

NOTE
1. The calls to writeList(list) and getList() do not need to be preceded by GetListTest plus a dot because main is not a client program: It is in the same class as getList and writeList.
2. If you omit the keyword static from the getList or writeList header, you get an error message like the following:

    Can't make static reference to method getList()  
in class GetListTest

The compiler has recognized that there was no object variable preceding the method call, which means that the methods were static and should have been declared as such.

Method Overloading

Overloaded methods are two or more methods in the same class that have the same name but different parameter lists. For example,

    public class DoOperations  
{"  
    public int product(int n) { return n * n; }  
    public double product(double x) { return x * x; }  
    public double product(int x, int y) { return x * y; }  
    ...  
"

The compiler figures out which method to call by examining the method's signature. The signature of a method consists of the method's name and a list of the parameter types. Thus, the signatures of the overloaded product methods are

    product(int)  
    product(double)  
    product(int, int)

Note that for overloading purposes, the return type of the method is irrelevant. You can't have two methods with identical signatures but different return types. The compiler will complain that the method call is ambiguous.

Having more than one constructor in the same class is an example of overloading. Overloaded constructors provide a choice of ways to initialize objects of the class.
SCOPE

The scope of a variable or method is the region in which that variable or method is visible and can be accessed.

The instance variables, static variables, and methods of a class belong to that class’s scope, which extends from the opening brace to the closing brace of the class definition. Within the class all instance variables and methods are accessible and can be referred to simply by name (no dot operator!).

A local variable is defined inside a method. It can even be defined inside a statement. Its scope extends from the point where it is declared to the end of the block in which its declaration occurs. A block is a piece of code enclosed in a {} pair. When a block is exited, the memory for a local variable is automatically recycled.

Local variables take precedence over instance variables with the same name. (Using the same name, however, creates ambiguity for the programmer, leading to errors. You should avoid the practice.)

The this Keyword

An instance method is always called for a particular object. This object is an implicit parameter for the method and is referred to with the keyword this. You are expected to know this vocabulary for the exam.

In the implementation of instance methods, all instance variables can be written with the prefix this followed by the dot operator.

Example 1

In the method call obj.doSomething("Mary",num), where obj is some class object and doSomething is a method of that class, "Mary" and num, the parameters in parentheses, are explicit parameters, whereas obj is an implicit parameter.

Example 2

Here’s an example where this is used as a parameter.

```java
public class Person
{
    private String name;
    private int age;

    public Person(String aName, int anAge)
    {
        name = aName;
        age = anAge;
    }

    /** @return the String form of this person */
    public String toString()
    { return name + " "+ age; }

    public void printPerson()
    { System.out.println(this); }

    //Other variables and methods are not shown.
}
```
Suppose a client class has these lines of code:

```java
Person p = new Person("Dan", 10);
p.printPerson();
```

The statement

```java
System.out.println(this);
```

in the printPerson method means “print the current Person object.” The output should be: Dan 10. Note that System.out.println invokes the toString method of the Person class.

**Example 3**

The deposit method of the BankAccount class can refer to balance as follows:

```java
public void deposit(String acctPassword, double amount)
{
    this.balance += amount;
}
```

The use of this is unnecessary in the above example.

**Example 4**

Consider a rational number class called Rational, which has two private instance variables:

```java
private int num;  // numerator
private int denom; // denominator
```

Now consider a constructor for the Rational class:

```java
public Rational(int num, int denom)
{
    this.num = num;
    this.denom = denom;
}
```

It is definitely not a good idea to use the same name for the explicit parameters and the private instance variables. But if you do, you can avoid errors by referring to this.num and this.denom for the current object that is being constructed. (This particular use of this will not be tested on the exam.)

---

**REFERENCES**

**Reference vs. Primitive Data Types**

All of the numerical data types, like `double` and `int`, as well as types `char` and `boolean`, are *primitive* data types. All objects are *reference* data types. The difference lies in the way they are stored.

Consider the statements
The variables \(\text{num1}\) and \(\text{num2}\) can be thought of as memory slots, labeled \(\text{num1}\) and \(\text{num2}\), respectively:

\[
\begin{array}{c|c|c}
\text{num1} & \text{num2} \\
3 & 3
\end{array}
\]

If either of the above variables is now changed, the other is not affected. Each has its own memory slot.

Contrast this with the declaration of a reference data type. Recall that an object is created using `new`:

```java
date = new Date(2, 17, 1948);
```

This declaration creates a reference variable \(d\) that refers to a `Date` object. The value of \(d\) is the address in memory of that object:

```
Date
d
month 2
day 17
year 1948
```

Suppose the following declaration is now made:

```java
date = d;
```

This statement creates the reference variable `birthday`, which contains the same address as `d`:

```
Date
d
birthday
month 2
day 17
year 1948
```

Having two references for the same object is known as aliasing. Aliasing can cause unintended problems for the programmer. The statement

```java
d.changeDate();
```

will automatically change the object referred to by `birthday` as well.

What the programmer probably intended was to create a second object called `birthday` whose attributes exactly matched those of `d`. This cannot be accomplished without using `new`. For example,

```java
date = new Date(d.getMonth(), d.getDay(), d.getYear());
```

The statement `d.changeDate()` will now leave the `birthday` object unchanged.
The Null Reference

The declaration

    BankAccount b;

defines a reference b that is uninitialized. (To construct the object that b refers to requires the new operator and a BankAccount constructor.) An uninitialized object variable is called a null reference or null pointer. You can test whether a variable refers to an object or is uninitialized by using the keyword null:

    if (b == null)

If a reference is not null, it can be set to null with the statement

    b = null;

An attempt to invoke an instance method with a null reference may cause your program to terminate with a NullPointerException. For example,

    public class PersonalFinances
    {
        BankAccount b;                     //b is a null reference
        ...
        b.withdraw(acctPassword, amt);     //throws a NullPointerException
        ...
        //if b not constructed with new

NOTE

If you fail to initialize a local variable in a method before you use it, you will get a compile-time error. If you make the same mistake with an instance variable of a class, the compiler provides reasonable default values for primitive variables (0 for numbers, false for booleans), and the code may run without error. However, if you don’t initialize reference instance variables in a class, as in the above example, the compiler will set them to null. Any method call for an object of the class that tries to access the null reference will cause a run-time error: The program will terminate with a NullPointerException.

Method Parameters

FORMAL VS. ACTUAL PARAMETERS

The header of a method defines the parameters of that method. For example, consider the withdraw method of the BankAccount class:

    public class BankAccount
    {
        ...
        public void withdraw(String acctPassword, double amount)
        ...
    }

This method has two explicit parameters, acctPassword and amount. These are dummy or formal parameters. Think of them as placeholders for the pair of actual parameters or arguments that will be supplied by a particular method call in a client program.

For example,
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BankAccount b = new BankAccount("TimB", 1000);
b.withdraw("TimB", 250);

Here "TimB" and 250 are the actual parameters that match up with acctPassword and amount for the withdraw method.

NOTE
1. The number of arguments in the method call must equal the number of parameters in the method header, and the type of each argument must be compatible with the type of each corresponding parameter.
2. In addition to its explicit parameters, the withdraw method has an implicit parameter, this, the BankAccount from which money will be withdrawn. In the method call
   b.withdraw("TimB", 250);
   the actual parameter that matches up with this is the object reference b.

PASSING PRIMITIVE TYPES AS PARAMETERS
Parameters are passed by value. For primitive types this means that when a method is called, a new memory slot is allocated for each parameter. The value of each argument is copied into the newly created memory slot corresponding to each parameter.

During execution of the method, the parameters are local to that method. Any changes made to the parameters will not affect the values of the arguments in the calling program. When the method is exited, the local memory slots for the parameters are erased.

Here's an example: What will the output be?

```java
public class ParamTest
{
    public static void foo(int x, double y)
    {
        x = 3;
        y = 2.5;
    }

    public static void main(String[] args)
    {
        int a = 7;
        double b = 6.5;
        foo(a, b);
        System.out.println(a + " " + b);
    }
}
```

The output will be

7 6.5

The arguments a and b remain unchanged, despite the method call!

This can be understood by picturing the state of the memory slots during execution of the program.
Just before the $f_00(a, b)$ method call:

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>6.5</td>
</tr>
</tbody>
</table>

At the time of the $f_00(a, b)$ method call:

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>6.5</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>6.5</td>
</tr>
</tbody>
</table>

Just before exiting the method: Note that the values of $x$ and $y$ have been changed.

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>6.5</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>2.5</td>
</tr>
</tbody>
</table>

After exiting the method: Note that the memory slots for $x$ and $y$ have been reclaimed. The values of $a$ and $b$ remain unchanged.

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>6.5</td>
</tr>
</tbody>
</table>

### PASSING OBJECTS AS PARAMETERS

In Java both primitive types and object references are passed by value. When an object’s reference is a parameter, the same mechanism of copying into local memory is used. The key difference is that the address (reference) is copied, not the values of the individual instance variables. As with primitive types, changes made to the parameters will not change the values of the matching arguments. What this means in practice is that it is not possible for a method to replace an object with another one—you can’t change the reference that was passed. It is, however, possible to change the state of the object to which the parameter refers through methods that act on the object.

#### Example 1

A method that changes the state of an object.

```java
/** Subtracts fee from balance in b if current balance too low. */
public static void chargeFee(BankAccount b, String password, double fee) {
    final double MIN_BALANCE = 10.00;
    if (b.getBalance() < MIN_BALANCE) {
        b.withdraw(password, fee);
    }
}
```

```java
public static void main(String[] args) {
    final double FEE = 5.00;
    BankAccount andysAccount = new BankAccount("AndyS", 7.00);
    chargeFee(andysAccount, "AndyS", FEE);
    ...
}
```
Here are the memory slots before the `chargeFee` method call:

At the time of the `chargeFee` method call, copies of the matching parameters are made:

Just before exiting the method: The `balance` field of the `BankAccount` object has been changed.

After exiting the method: All parameter memory slots have been erased, but the object remains altered.

**NOTE**

The `andysAccount` reference is unchanged throughout the program segment. The object to which it refers, however, has been changed. This is significant. Contrast this with Example 2 below in which an attempt is made to replace the object itself.
Example 2

A chooseBestAccount method attempts—erroneously—to set its betterFund parameter to the BankAccount with the higher balance:

```java
public static void chooseBestAccount(BankAccount better, 
    BankAccount b1, BankAccount b2)
{
    if (b1.getBalance() > b2.getBalance())
        better = b1;
    else
        better = b2;
}
```

```java
public static void main(String[] args)
{
    BankAccount briansFund = new BankAccount("BrianL", 10000); 
    BankAccount paulsFund = new BankAccount("PaulM", 90000); 
    BankAccount betterFund = null;

    chooseBestAccount(betterFund, briansFund, paulsFund);
    ... 
}
```

The intent is that betterFund will be a reference to the paulsFund object after execution of the chooseBestAccount statement. A look at the memory slots illustrates why this fails.

Before the chooseBestAccount method call:

```
<table>
<thead>
<tr>
<th>BankAccount</th>
<th>briansFund</th>
</tr>
</thead>
<tbody>
<tr>
<td>password</td>
<td>&quot;BrianL&quot;</td>
</tr>
<tr>
<td>balance</td>
<td>10000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>BankAccount</th>
<th>paulsFund</th>
</tr>
</thead>
<tbody>
<tr>
<td>password</td>
<td>&quot;PaulM&quot;</td>
</tr>
<tr>
<td>balance</td>
<td>90000</td>
</tr>
</tbody>
</table>
```

At the time of the chooseBestAccount method call: Copies of the matching references are made.
Just before exiting the method: The value of `better` has been changed; `betterFund`, however, remains unchanged.

After exiting the method: All parameter slots have been erased.
The way to fix the problem is to modify the method so that it returns the better account. Returning an object from a method means that you are returning the address of the object.

```java
public static BankAccount chooseBestAccount(BankAccount b1,
                                             BankAccount b2)
{
    BankAccount better;
    if (b1.getBalance() > b2.getBalance())
        better = b1;
    else
        better = b2;
    return better;
}
```

```java
public static void main(String[] args)
{
    BankAccount briansFund = new BankAccount("BrianL", 10000);
    BankAccount paulsFund = new BankAccount("PaulM", 90000);
    BankAccount betterFund = chooseBestAccount(briansFund, paulsFund);
    ...
}
```

**NOTE**

The effect of this is to create the betterFund reference, which refers to the same object as paulsFund:

![Diagram showing the creation of the betterFund reference](image-url)
What the method does not do is create a new object to which betterFund refers. To do that would require the keyword `new` and use of a `BankAccount` constructor. Assuming that a `getPassword()` accessor has been added to the `BankAccount` class, the code would look like this:

```java
public static BankAccount chooseBestAccount(BankAccount b1, BankAccount b2) {
    BankAccount better;
    if (b1.getBalance() > b2.getBalance())
        better = new BankAccount(b1.getPassword(), b1.getBalance());
    else
        better = new BankAccount(b2.getPassword(), b2.getBalance());
    return better;
}
```

Using this modified method with the same `main()` method above has the following effect:

![Diagram showing BankAccount objects with passwords and balances]

Modifying more than one object in a method can be accomplished using a *wrapper class* (see p. 180).

---

**Chapter Summary**

By now you should be able to write code for any given object, with its private data fields and methods encapsulated in a class. Be sure that you know the various types of methods—static, instance, and overloaded.

You should also understand the difference between storage of primitive types and the references used for objects.
MULTIPLE-CHOICE QUESTIONS ON CLASSES AND OBJECTS

Questions 1–3 refer to the Time class declared below:

```java
public class Time {
    private int hrs;
    private int mins;
    private int secs;

    public Time() {
        /* implementation not shown */
    }

    public Time(int h, int m, int s) {
        /* implementation not shown */
    }

    /** Resets time to hrs = h, mins = m, secs = s. */
    public void resetTime(int h, int m, int s) {
        /* implementation not shown */
    }

    /** Advances time by one second. */
    public void increment() {
        /* implementation not shown */
    }

    /** @return true if this time equals t, false otherwise */
    public boolean equals(Time t) {
        /* implementation not shown */
    }

    /** @return true if this time is earlier than t, false otherwise */
    public boolean lessThan(Time t) {
        /* implementation not shown */
    }

    /** @return a String with the time in the form hrs:mins:secs */
    public String toString() {
        /* implementation not shown */
    }
}
```

1. Which of the following is a false statement about the methods?
   (A) equals, lessThan, and toString are all accessor methods.
   (B) increment is a mutator method.
   (C) Time() is the default constructor.
   (D) The Time class has three constructors.
   (E) There are no static methods in this class.
2. Which of the following represents correct implementation code for the constructor with parameters?
   (A) hrs = 0;
       mins = 0;
       secs = 0;
   (B) hrs = h;
       mins = m;
       secs = s;
   (C) resetTime(hrs, mins, secs);
   (D) h = hrs;
       m = mins;
       s = secs;
   (E) Time = new Time(h, m, s);

3. A client class has a display method that writes the time represented by its parameter:

   /** Outputs time t in the form hrs:mins:secs. *
    * @param t the time *
    */
   public void display (Time t)
   {
   /* method body */
   }

Which of the following are correct replacements for /* method body */?
   I Time T = new Time(h, m, s);
       System.out.println(T);
   II System.out.println(t.hrs + ":" + t.mins + ":" + tsecs);
   III System.out.println(t);
   (A) I only
   (B) II only
   (C) III only
   (D) II and III only
   (E) I, II, and III

4. Which statement about parameters is false?
   (A) The scope of parameters is the method in which they are defined.
   (B) Static methods have no implicit parameter this.
   (C) Two overloaded methods in the same class must have parameters with different names.
   (D) All parameters in Java are passed by value.
   (E) Two different constructors in a given class can have the same number of parameters.
Questions 5–11 refer to the following Date class declaration:

```java
public class Date {
    private int day;
    private int month;
    private int year;

    public Date() //default constructor
    {
        ...
    }

    public Date(int mo, int da, int yr) //constructor
    {
        ...
    }

    public int month() //returns month of Date
    {
        ...
    }

    public int day() //returns day of Date
    {
        ...
    }

    public int year() //returns year of Date
    {
        ...
    }

    //Returns String representation of Date as "m/d/y", e.g. 4/18/1985.
    public String toString()
    {
        ...
    }
}
```

5. Which of the following correctly constructs a Date object in a client class?

(A) Date d = new (2, 13, 1947);

(B) Date d = new Date(2, 13, 1947);

(C) Date d;
    d = new (2, 13, 1947);

(D) Date d;
    d = Date(2, 13, 1947);

(E) Date d = Date(2, 13, 1947);
6. Which of the following will cause an error message?

I Date d1 = new Date(8, 2, 1947);
   Date d2 = d1;

II Date d1 = null;
   Date d2 = d1;

III Date d = null;
   int x = d.year();

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III

7. A client program creates a Date object as follows:

Date d = new Date(1, 13, 2002);

Which of the following subsequent code segments will cause an error?

(A) String s = d.toString();
(B) int x = d.day();
(C) Date e = d;
(D) Date e = new Date(1, 13, 2002);
(E) int y = d.year;

8. Consider the implementation of a write() method that is added to the Date class:

/** Write the date in the form m/d/y, for example 2/17/1948. */
public void write()
{
   /* implementation code */
}

Which of the following could be used as /* implementation code */?

I System.out.println(month + "/" + day + "/" + year);
II System.out.println(month() + "/" + day() + "/" + year());
III System.out.println(this);

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III
9. Here is a client program that uses `Date` objects:

```java
public class BirthdayStuff {
    public static Date findBirthdate()
    {
        /* code to get birthDate */
        return birthDate;
    }

    public static void main(String[] args)
    {
        Date d = findBirthdate();
        ...
    }
}
```

Which of the following is a correct replacement for /* code to get birthDate */?

I System.out.println("Enter birthdate: mo, day, yr: ");
int m = IO.readInt(); //read user input
int d = IO.readInt(); //read user input
int y = IO.readInt(); //read user input
Date birthDate = new Date(m, d, y);

II System.out.println("Enter birthdate: mo, day, yr: ");
int birthDate.month() = IO.readInt(); //read user input
int birthDate.day() = IO.readInt(); //read user input
int birthDate.year() = IO.readInt(); //read user input
Date birthDate = new Date(birthDate.month, birthDate.day, birthDate.year);

III System.out.println("Enter birthdate: mo, day, yr: ");
int birthDate.month = IO.readInt(); //read user input
int birthDate.day = IO.readInt(); //read user input
int birthDate.year = IO.readInt(); //read user input
Date birthDate = new Date(birthDate.month, birthDate.day, birthDate.year);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only
Chapter 2 Classes and Objects

10. A method in a client program for the Date class has this declaration:

\[
\text{Date } d1 = \text{new Date(mo, da, yr);}
\]

where mo, da, and yr are previously defined integer variables. The same method now creates a second Date object d2 that is an exact copy of the object d1 refers to. Which of the following code segments will not do this correctly?

I Date d2 = d1;
II Date d2 = new Date(mo, da, yr);
III Date d2 = new Date(d1.month(), d1.day(), d1.year());

(A) I only  
(B) II only  
(C) III only  
(D) II and III only  
(E) I, II, and III

11. The Date class is modified by adding the following mutator method:

\[
\text{public void addYears(int n) //add n years to date}
\]

Here is part of a poorly coded client program that uses the Date class:

\[
\text{public static void addCentury(Date recent, Date old) }
\{
\text{  old.addYears(100);}
\text{  recent = old;}
\}
\]

\[
\text{public static void main(String[] args) }
\{
\text{  Date oldDate = new Date(1, 13, 1900);}
\text{  Date recentDate = null;}
\text{  addCentury(recentDate, oldDate);}
\text{  ...}
\}
\]

Which will be true after executing this code?

(A) A NullPointerException is thrown.  
(B) The oldDate object remains unchanged.  
(C) recentDate is a null reference.  
(D) recentDate refers to the same object as oldDate.  
(E) recentDate refers to a separate object whose contents are the same as those of oldDate.
12. Here are the private instance variables for a Frog object:

```java
public class Frog {
    private String species;
    private int age;
    private double weight;
    private Position position; //position (x,y) in pond
    private boolean amAlive;
    ...
}
```

Which of the following methods in the Frog class is the best candidate for being a static method?

(A) swim //frog swims to new position in pond
(B) getPondTemperature //returns temperature of pond
(C) eat //frog eats and gains weight
(D) getWeight //returns weight of frog
(E) die //frog dies with some probability based on frog’s age and pond temperature

13. What output will be produced by this program?

```java
public class Mystery {
    public static void strangeMethod(int x, int y) {
        x += y;
        y *= x;
        System.out.println(x + " " + y);
    }

    public static void main(String[] args) {
        int a = 6, b = 3;
        strangeMethod(a, b);
        System.out.println(a + " " + b);
    }
}
```

(A) 36 9
(B) 3 6 9
(C) 9 27 9 27
(D) 6 3 9 27
(E) 9 27 6 3
Questions 14–17 refer to the following definition of the `Rational` class:

```java
public class Rational {
    private int numerator;
    private int denominator;

    /** default constructor */
    Rational() {
        /* implementation not shown */
    }

    /** Constructs a Rational with numerator n and
     * denominator 1. */
    Rational(int n) {
        /* implementation not shown */
    }

    /** Constructs a Rational with specified numerator and
     * denominator. */
    Rational(int numer, int denom) {
        /* implementation not shown */
    }

    /** @return numerator */
    int numerator() {
        /* implementation not shown */
    }

    /** @return denominator */
    int denominator() {
        /* implementation not shown */
    }

    /** Returns (this + r). Leaves this unchanged.
     * @return this rational number plus r
     * @param r a rational number to be added to this Rational */
    public Rational plus(Rational r) {
        /* implementation not shown */
    }

    //Similarly for times, minus, divide ...
    ...

    /** Ensures denominator > 0. */
    private void fixSigns() {
        /* implementation not shown */
    }

    /** Ensures lowest terms. */
    private void reduce() {
        /* implementation not shown */
    }
}
```

14. The method `reduce()` is not a public method because
   (A) methods whose return type is `void` cannot be public.
   (B) methods that change this cannot be public.
   (C) the `reduce()` method is not intended for use by clients of the `Rational` class.
   (D) the `reduce()` method is intended for use only by clients of the `Rational` class.
   (E) the `reduce()` method uses only the private data fields of the `Rational` class.
15. The constructors in the Rational class allow initialization of Rational objects in several different ways. Which of the following will cause an error?
(A) Rational r1 = new Rational();
(B) Rational r2 = r1;
(C) Rational r3 = new Rational(2, -3);
(D) Rational r4 = new Rational(3.5);
(E) Rational r5 = new Rational(10);

16. Here is the implementation code for the plus method:

```java
/** Returns (this + r). Leaves this unchanged.
 * @return this rational number plus r
 * @param r a rational number to be added to this Rational
 */
public Rational plus(Rational r)
{
    fixSigns();
    r.fixSigns();
    int denom = denominator * r.denominator;
    int numer = numerator * r.denominator + r.numerator * denominator;
    /* more code */
}
```

Which of the following is a correct replacement for /* more code */?
(A) Rational rat(numer, denom);
   rat.reduce();
   return rat;
(B) return new Rational(numer, denom);
(C) reduce();
   Rational rat = new Rational(numer, denom);
   return rat;
(D) Rational rat = new Rational(numer, denom);
   Rational.reduce();
   return rat;
(E) Rational rat = new Rational(numer, denom);
   rat.reduce();
   return rat;

17. Assume these declarations:

```java
Rational a = new Rational();
Rational r = new Rational(numer, denom);
int n = value;
// numer, denom, and value are valid integer values
```

Which of the following will cause a compile-time error?
(A) r = a.plus(r);
(B) a = r.plus(new Rational(n));
(C) r = r.plus(r);
(D) a = n.plus(r);
(E) r = r.plus(new Rational(n));
Questions 18–20 refer to the Temperature class shown below:

```java
public class Temperature {
    private String scale; //valid values are "F" or "C"
    private double degrees;

    /** constructor with specified degrees and scale */
    public Temperature(double tempDegrees, String tempScale) { /* implementation not shown */ }

    /** Mutator. Converts this Temperature to degrees Fahrenheit.
     * @return this temperature in degrees Fahrenheit
     */
    public Temperature toFahrenheit() { /* implementation not shown */ }

    /** Mutator. Converts this Temperature to degrees Celsius.
     * @return this temperature in degrees Celsius
     */
    public Temperature toCelsius() { /* implementation not shown */ }

    /** Mutator.
     * @param amt the number of degrees to raise this temperature
     * @return this temperature raised by amt degrees
     */
    public Temperature raise(double amt) { /* implementation not shown */ }

    /** Mutator.
     * @param amt the number of degrees to lower this temperature
     * @return this temperature lowered by amt degrees
     */
    public Temperature lower(double amt) { /* implementation not shown */ }

    /** @param tempDegrees the number of degrees
     * @param tempScale the temperature scale
     * @return true if tempDegrees is a valid temperature in the given temperature scale, false otherwise
     */
    public static boolean isValidTemp(double tempDegrees, String tempScale) { /* implementation not shown */ }

    //Other methods are not shown.
}
```
18. A client method contains this code segment:

```java
Temperature t1 = new Temperature(40, "C");
Temperature t2 = t1;
Temperature t3 = t2.lower(20);
Temperature t4 = t1.toFahrenheit();
```

Which statement is true following execution of this segment?
(A) t1, t2, t3, and t4 all represent the identical temperature, in degrees Celsius.
(B) t1, t2, t3, and t4 all represent the identical temperature, in degrees Fahrenheit.
(C) t4 represents a Fahrenheit temperature, while t1, t2, and t3 all represent degrees Celsius.
(D) t1 and t2 refer to the same Temperature object; t3 refers to a Temperature object that is 20 degrees lower than t1 and t2, while t4 refers to an object that is t1 converted to Fahrenheit.
(E) A NullPointerException was thrown.

19. Consider the following code:

```java
public class TempTest
{
    public static void main(String[] args)
    {
        System.out.println("Enter temperature scale: ");
        String tempScale = IO.readString(); //read user input
        System.out.println("Enter number of degrees: ");
        double tempDegrees = IO.readDouble(); //read user input
        /* code to construct a valid temperature from user input */
    }
}
```

Which is a correct replacement for /* code to construct... */?

I Temperature t = new Temperature(tempDegrees, tempScale);
if (!t.isValidTemp(tempDegrees, tempScale))
    /* error message and exit program */

II if (isValidTemp(tempDegrees, tempScale))
    Temperature t = new Temperature(tempDegrees, tempScale);
else
    /* error message and exit program */

III if (Temperature.isValidTemp(tempDegrees, tempScale))
    Temperature t = new Temperature(tempDegrees, tempScale);
else
    /* error message and exit program */

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only
20. The formula to convert degrees Celsius $C$ to Fahrenheit $F$ is

$$F = 1.8C + 32$$

For example, 30°C is equivalent to 86°F.

An `inFahrenheit()` accessor method is added to the `Temperature` class. Here is its implementation:

```java
/**
 * Precondition: The temperature is a valid temperature
 * in degrees Celsius.
 * Postcondition:
 * - An equivalent temperature in degrees Fahrenheit has been
 *   returned.
 * - Original temperature remains unchanged.
 * @return an equivalent temperature in degrees Fahrenheit
 */
public Temperature inFahrenheit()
{
    Temperature result;
    /* more code */
    return result;
}
```

Which of the following correctly replaces `/* more code */` so that the postcondition is achieved?

I. `result = new Temperature(degrees * 1.8 + 32, "F");`

II. `result = new Temperature(degrees * 1.8, "F");
    result = result.raise(32);`

III. `degrees *= 1.8;
     this = this.raise(32);
     result = new Temperature(degrees, "F");`

(A) I only  
(B) II only 
(C) III only  
(D) I and II only 
(E) I, II, and III
21. Consider this program:

```java
public class CountStuff {
    public static void doSomething() {
        int count = 0;
        ...
        // code to do something - no screen output produced
        count++;
    }

    public static void main(String[] args) {
        int count = 0;
        System.out.println("How many iterations?");
        int n = IO.readInt(); // read user input
        for (int i = 1; i <= n; i++) {
            doSomething();
            System.out.println(count);
        }
    }
}
```

If the input value for `n` is 3, what screen output will this program subsequently produce?

(A) 0
    0
    0

(B) 1
    2
    3

(C) 3
    3
    3

(D) ?
    ?
    ?
    where ? is some undefined value.

(E) No output will be produced.
22. This question refers to the following class:

```java
public class IntObject {
    private int num;

    public IntObject() //default constructor
    { num = 0; }

    public IntObject(int n) //constructor
    { num = n; }

    public void increment() //increment by 1
    { num++; }
}
```

Here is a client program that uses this class:

```java
public class IntObjectTest {
    public static IntObject someMethod(IntObject obj)
    {
        IntObject ans = obj;
        ans.increment();
        return ans;
    }

    public static void main(String[] args)
    {
        IntObject x = new IntObject(2);
        IntObject y = new IntObject(7);
        IntObject a = y;
        x = someMethod(y);
        a = someMethod(x);
    }
}
```

Just before exiting this program, what are the object values of x, y, and a, respectively?

(A) 9, 9, 9  
(B) 2, 9, 9  
(C) 2, 8, 9  
(D) 3, 8, 9  
(E) 7, 8, 9
23. Consider the following program:

```java
public class Tester
{
    public void someMethod(int a, int b)
    {
        int temp = a;
        a = b;
        b = temp;
    }
}

public class TesterMain
{
    public static void main(String[] args)
    {
        int x = 6, y = 8;
        Tester tester = new Tester();
        tester.someMethod(x, y);
    }
}
```

Just before the end of execution of this program, what are the values of \(x\), \(y\), and \(temp\), respectively?

(A) 6, 8, 6
(B) 8, 6, 6
(C) 6, 8, ?, where ? means undefined
(D) 8, 6, ?, where ? means undefined
(E) 8, 6, 8
## ANSWER KEY

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## ANSWERS EXPLAINED

1. (D) There are just two constructors. Constructors are recognizable by having the same name as the class, and no return type.

2. (B) Each of the private instance variables should be assigned the value of the matching parameter. Choice B is the only choice that does this. Choice D confuses the order of the assignment statements. Choice A gives the code for the default constructor, ignoring the parameters. Choice C would be correct if it were `resetTime(h, m, s)`. As written, it doesn't assign the parameter values `h`, `m`, and `s` to `hrs`, `mins`, and `secs`. Choice E is wrong because the keyword `new` should be used to create a new object, not to implement the constructor!

3. (C) Replacement III will automatically print time in the required form since a `toString` method was defined for the `Time` class. Replacement I is wrong because it doesn't refer to the parameter, `t`, of the method. Replacement II is wrong because a client program may not access private data of the class.

4. (C) The parameter names can be the same—the signatures must be different. For example,

   ```java
   public void print(int x) //prints x
   public void print(double x) //prints x
   ```

   The signatures (method name plus parameter types) here are `print(int)` and `print(double)`, respectively. The parameter name `x` is irrelevant. Choice A is true: All local variables and parameters go out of scope (are erased) when the method is exited. Choice B is true: Static methods apply to the whole class. Only instance methods have an implicit `this` parameter. Choice D is true even for object parameters: Their references are passed by value. Note that choice E is true because it's possible to have two different constructors with different signatures but the same number of parameters (e.g., one for an `int` argument and one for a `double`).

5. (B) Constructing an object requires the keyword `new` and a constructor of the `Date` class. Eliminate choices D and E since they omit `new`. The class name `Date` should appear on the right-hand side of the assignment statement, immediately following the keyword `new`. This eliminates choices A and C.
6. (C) Segment III will cause a NullPointerException to be thrown since d is a null reference. You cannot invoke a method for a null reference. Segment II has the effect of assigning null to both d1 and d2—obscure but not incorrect. Segment I creates the object reference d1 and then declares a second reference d2 that refers to the same object as d1.

7. (E) A client program cannot access a private instance variable.

8. (E) All are correct. Since write() is a Date instance method, it is OK to use the private data members in its implementation code. Segment III prints this, the current Date object. This usage is correct since write() is part of the Date class. The toString() method guarantees that the date will be printed in the required format (see p. 175).

9. (A) The idea here is to read in three separate variables for month, day, and year and then to construct the required date using new and the Date class constructor with three parameters. Code segment II won’t work because month(), day(), and year() are accessor methods that access existing values and may not be used to read new values into a Date. Segment III is wrong because it tries to access private instance variables from a client program.

10. (A) Segment I will not create a second object. It will simply cause d2 to refer to the same object as d1, which is not what was required. The keyword new must be used to create a new object.

11. (C) When recentDate is declared in main(), its value is null. Recall that a method is not able to replace an object reference, so recentDate remains null. Note that the intent of the program is to change recentDate to refer to the updated oldDate object. The code, however, doesn’t do this. Choice A is false: No methods are invoked with a null reference. Choice B is false because addYears() is a mutator method. Even though a method doesn’t change the address of its object parameter, it can change the contents of the object, which is what happens here. Choices D and E are wrong because the addCentury() method cannot change the value of its recentDate argument.

12. (B) The method getPondTemperature is the only method that applies to more than one frog. It should therefore be static. All of the other methods relate directly to one particular Frog object. So f.swim(), f.die(), f.getWeight(), and f.eat() are all reasonable methods for a single instance f of a Frog. On the other hand, it doesn’t make sense to say f.getPondTemperature(). It makes more sense to say Frog.getPondTemperature(), since the same value will apply to all frogs in the class.

13. (E) Here are the memory slots at the start of strangeMethod(a, b):

```
   a  b
  6  3
```

Before exiting strangeMethod(a, b):

```
   x  y
  6  3
```
Note that 9 27 is output before exiting. After exiting strangeMethod(a, b), the memory slots are

\[
\begin{array}{c|c|c|c}
\hline
a & b \\
6 & 3 \\
\hline
x & y \\
9 & 27 \\
\hline
\end{array}
\]

The next step outputs 6 3.

14. (C) The `reduce()` method will be used only in the implementation of the instance methods of the `Rational` class.

15. (D) None of the constructors in the `Rational` class takes a real-valued parameter. Thus, the real-valued parameter in choice D will need to be converted to an integer. Since in general truncating a real value to an integer involves a loss of precision, it is not done automatically—you have to do it explicitly with a cast. Omitting the cast causes a compile-time error.

16. (E) A new `Rational` object must be created using the newly calculated `numerator` and `denominator`. Then it must be reduced before being returned. Choice A is wrong because it doesn't correctly create the new object. Choice B returns a correctly constructed object, but one that has not been reduced. Choice C reduces the current object, `this`, instead of the new object, `rat`. Choice D is wrong because it invokes `reduce()` for the `Rational` class instead of the specific `rat` object.

17. (D) The `plus` method of the `Rational` class can only be invoked by `Rational` objects. Since `n` is an `int`, the statement in choice D will cause an error.

18. (B) This is an example of aliasing. The keyword `new` is used just once, which means that just one object is constructed. Here are the memory slots after each declaration:

```
After declaration for t1

Temperature
scale "C"
degrees 40

After declaration for t2

Temperature
scale "C"
degrees 40
```
19. (C) Notice that isValidTemp is a static method for the Temperature class, which means that it cannot be invoked with a Temperature object. Thus, segment I is incorrect: `t.isValidTemp` is wrong. Segment II fails because isValidTemp is not a method of the TempTest class. It therefore must be invoked with its class name, which is what happens (correctly) in segment III: `Temperature.isValidTemp`.

20. (D) A new Temperature object must be constructed to prevent the current Temperature from being changed. Segment I, which applies the conversion formula directly to degrees, is the best way to do this. Segment II, while not the best algorithm, does work. The statement

```java
result = result.raise(32);
```

has the effect of raising the result temperature by 32 degrees, and completing the conversion. Segment III fails because

```java
degrees *= 1.8;
```

alters the `degrees` instance variable of the current object, as does

```java
this = this.raise(32);
```

To be correct, these operations must be applied to the `result` object.

21. (A) This is a question about the scope of variables. The scope of the count variable that is declared in `main()` extends up to the closing brace of `main()`. In `doSomething()`, count is a local variable. After the method call in the `for` loop, the local variable count goes out of scope, and the value that’s being printed is the value of the count in `main()`, which is unchanged from 0.

22. (A) Here are the memory slots before the first `someMethod` call:

![Memory slots before first someMethod call](image)

Just before exiting `x = someMethod(y):`
Chapter 2  Classes and Objects

After exiting

```java
x = someMethod(y);
```

x has been reassigned, so the object with num = 2 has been recycled:

After exiting a = someMethod(x):

23. (C) Recall that when primitive types are passed as parameters, copies are made of the actual arguments. All manipulations in the method are performed on the copies, and the arguments remain unchanged. Thus x and y retain their values of 6 and 8. The local variable temp goes out of scope as soon as someMethod is exited and is therefore undefined just before the end of execution of the program.
Inheritance and Polymorphism

Chapter Goals
- Superclasses and subclasses
- Inheritance hierarchy
- Polymorphism
- Type compatibility
- Abstract classes
- Interfaces

INHERITANCE

Superclass and Subclass

Inheritance defines a relationship between objects that share characteristics. Specifically it is the mechanism whereby a new class, called a subclass, is created from an existing class, called a superclass, by absorbing its state and behavior and augmenting these with features unique to the new class. We say that the subclass inherits characteristics of its superclass.

Don’t get confused by the names: a subclass is bigger than a superclass—it contains more data and more methods!

Inheritance provides an effective mechanism for code reuse. Suppose the code for a superclass has been tested and debugged. Since a subclass object shares features of a superclass object, the only new code required is for the additional characteristics of the subclass.

Inheritance Hierarchy

A subclass can itself be a superclass for another subclass, leading to an inheritance hierarchy of classes.

For example, consider the relationship between these objects: Person, Employee, Student, GradStudent, and UnderGrad.
For any of these classes, an arrow points to its superclass. The arrow designates an inheritance relationship between classes, or, informally, an *is-a* relationship. Thus, an Employee *is-a* Person; a Student *is-a* Person; a GradStudent *is-a* Student; an UnderGrad *is-a* Student. Notice that the opposite is not necessarily true: A Person may not be a Student, nor is a Student necessarily an UnderGrad.

Note that the *is-a* relationship is transitive: If a GradStudent *is-a* Student and a Student *is-a* Person, then a GradStudent *is-a* Person.

Every subclass inherits the public or protected variables and methods of its superclass (see p. 135). Subclasses may have additional methods and instance variables that are not in the superclass. A subclass may redefine a method it inherits. For example, GradStudent and UnderGrad may use different algorithms for computing the course grade, and need to change a computeGrade method inherited from Student. This is called *method overriding*. If part of the original method implementation from the superclass is retained, we refer to the rewrite as *partial overriding* (see p. 135).

### Implementing Subclasses

**THE extends KEYWORD**

The inheritance relationship between a subclass and a superclass is specified in the declaration of the subclass, using the keyword extends. The general format looks like this:

```java
public class Superclass
{
    //private instance variables
    //other data members
    //constructors
    //public methods
    //private methods
}

public class Subclass extends Superclass
{
    //additional private instance variables
    //additional data members
    //constructors (Not inherited!)
    //additional public methods
    //inherited public methods whose implementation is overridden
    //additional private methods
}
```
Inheritance

For example, consider the following inheritance hierarchy:

```
Student
   \-
GradStudent  UnderGrad
```

The implementation of the classes may look something like this (discussion follows the code):

```java
public class Student
{
   //data members
   public final static int NUM_TESTS = 3;
   private String name;
   private int[] tests;
   private String grade;

   //constructor
   public Student()
   {
      name = "";
      tests = new int[NUM_TESTS];
      grade = "";
   }

   //constructor
   public Student(String studName, int[] studTests, String studGrade)
   {
      name = studName;
      tests = studTests;
      grade = studGrade;
   }

   public String getName()
   { return name; }

   public String getGrade()
   { return grade; }

   public void setGrade(String newGrade)
   { grade = newGrade; }

   public void computeGrade()
   {
      if (name.equals(""))
         grade = "No grade";
      else if (getTestAverage() >= 65)
         grade = "Pass";
      else
         grade = "Fail";
   }
```
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public double getTestAverage()
{
    double total = 0;
    for (int score : tests)
    {
        total += score;
    }
    return total/NUM_TESTS;
}

public class UnderGrad extends Student
{
    public UnderGrad() //default constructor
    {
        super();
    }

    public UnderGrad(String studName, int[] studTests, String studGrade)
    {
        super(studName, studTests, studGrade);
    }

    public void computeGrade()
    {
        if (getTestAverage() >= 70)
            setGrade("Pass");
        else
            setGrade("Fail");
    }

    public class GradStudent extends Student
    {
        private int gradID;
        public GradStudent() //default constructor
        {
            super();
            gradID = 0;
        }

        public GradStudent(String studName, int[] studTests, String studGrade, int gradStudID)
        {
            super(studName, studTests, studGrade);
            gradID = gradStudID;
        }

        public int getID()
        {
            return gradID;
        }

        public void computeGrade()
        {
            super.computeGrade();
            if (getTestAverage() >= 90)
                setGrade("Pass with distinction");
        }
    }
INHERITING INSTANCE METHODS AND VARIABLES

The semantics of talking about inheritance is tricky. Subclasses do not inherit the private instance variables or private methods of their superclasses. However, objects of subclasses contain memory for those private instance variables, even though they can’t directly access them. A subclass inherits all the public and protected data members of its parent.

In the Student example, the UnderGrad and GradStudent subclasses inherit all of the methods of the Student superclass. Notice, however, that the Student instance variables name, tests, and grade are private and are therefore not inherited or directly accessible to the methods in the UnderGrad and GradStudent subclasses. A subclass can, however, directly invoke the public accessor and mutator methods of the superclass. Thus, both UnderGrad and GradStudent use getTestAverage. Additionally, both UnderGrad and GradStudent use setGrade to access indirectly—and modify—grade.

If, instead of private, the access specifier for the instance variables in Student were public or protected, then the subclasses could directly access these variables. The keyword protected is not part of the AP Java subset.

Classes on the same level in a hierarchy diagram do not inherit anything from each other (for example, UnderGrad and GradStudent). All they have in common is the identical code they inherit from their superclass.

METHOD OVERRIDING AND THE super KEYWORD

Any public method in a superclass can be overridden in a subclass by defining a method with the same return type and signature (name and parameter types). For example, the computeGrade method in the UnderGrad subclass overrides the computeGrade method in the Student superclass.

Sometimes the code for overriding a method includes a call to the superclass method. This is called partial overriding. Typically this occurs when the subclass method wants to do what the superclass does, plus something extra. This is achieved by using the keyword super in the implementation. The computeGrade method in the GradStudent subclass partially overrides the matching method in the Student class. The statement

    super.computeGrade();

signals that the computeGrade method in the superclass should be invoked here. The additional test

    if (getTestAverage() >= 90)
    ...

allows a GradStudent to have a grade Pass with distinction. Note that this option is open to GradStudents only.

NOTE

Private methods cannot be overridden.

CONSTRUCTORS AND super

Constructors are never inherited! If no constructor is written for a subclass, the superclass default constructor with no parameters is generated. If the superclass does
not have a default (zero-parameter) constructor, but only a constructor with parameters, a compiler error will occur. If there is a default constructor in the superclass, inherited data members will be initialized as for the superclass. Additional instance variables in the subclass will get a default initialization—0 for primitive types and null for reference types.

A subclass constructor can be implemented with a call to the super method, which invokes the superclass constructor. For example, the default constructor in the UnderGrad class is identical to that of the Student class. This is implemented with the statement

```java
super();
```

The second constructor in the UnderGrad class is called with parameters that match those in the constructor of the Student superclass.

```java
public UnderGrad(String studName, int[] studTests, String studGrade)
{ super(studName, studTests, studGrade); }
```

For each constructor, the call to super has the effect of initializing the instance variables name, tests, and grade exactly as they are initialized in the Student class. Contrast this with the constructors in GradStudent. In each case, the instance variables name, tests, and grade are initialized as for the Student class. Then the new instance variable, gradID, must be explicitly initialized.

```java
public GradStudent()
{
    super();
    gradID = 0;
}
```

```java
public GradStudent(String studName, int[] studTests, String studGrade, int gradStudID)
{
    super(studName, studTests, studGrade);
    gradID = gradStudID;
}
```

**NOTE**

1. If super is used in the implementation of a subclass constructor, it must be used in the first line of the constructor body.
2. If no constructor is provided in a subclass, the compiler provides the following default constructor:

```java
public SubClass()
{
    super(); //calls default constructor of superclass
}
```
Inheritance

Rules for Subclasses

- A subclass can add new private instance variables.
- A subclass can add new public, private, or static methods.
- A subclass can override inherited methods.
- A subclass may not redefine a public method as private.
- A subclass may not override static methods of the superclass.
- A subclass should define its own constructors.
- A subclass cannot directly access the private members of its superclass. It must use accessor or mutator methods.

Declaring Subclass Objects

When a superclass object is declared in a client program, that reference can refer not only to an object of the superclass, but also to objects of any of its subclasses. Thus, each of the following is legal:

Student \( s = \) new Student();
Student \( g = \) new GradStudent();
Student \( u = \) new UnderGrad();

This works because a GradStudent is-a Student, and an UnderGrad is-a Student.

Note that since a Student is not necessarily a GradStudent nor an UnderGrad, the following declarations are not valid:

GradStudent \( g = \) new Student();
UnderGrad \( u = \) new Student();

Consider these valid declarations:

Student \( s = \) new Student("Brian Lorenzen", new int[] {90,94,99}, "none");
Student \( u = \) new UnderGrad("Tim Broder", new int[] {90,90,100}, "none");
Student \( g = \) new GradStudent("Kevin Cristella", new int[] {85,70,90}, "none", 1234);

Suppose you make the method call

\[ s.setGrade("Pass"); \]

The appropriate method in Student is found and the new grade assigned. The method calls

\[ g.setGrade("Pass"); \]

and

\[ u.setGrade("Pass"); \]

achieve the same effect on \( g \) and \( u \) since GradStudent and UnderGrad both inherit the setGrade method from Student. The following method calls, however, won’t work:

\[ \text{int studentNum} = s.getID(); \]
\[ \text{int underGradNum} = u.getID(); \]

Neither Student nor UnderGrad \( u \) inherit the getID method from the GradStudent class: A superclass does not inherit from a subclass.

Now consider the following valid method calls:
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Since s, g, and u have all been declared to be of type Student, will the appropriate method be executed in each case? That is the topic of the next section, polymorphism.

NOTE
The initializer list syntax used in constructing the array parameters—for example, new int[] {90,90,100}—will not be tested on the AP exam.

POLYMORPHISM

A method that has been overridden in at least one subclass is said to be polymorphic. An example is computeGrade, which is redefined for both GradStudent and UnderGrad.

Polymorphism is the mechanism of selecting the appropriate method for a particular object in a class hierarchy. The correct method is chosen because, in Java, method calls are always determined by the type of the actual object, not the type of the object reference. For example, even though s, g, and u are all declared as type Student, s.computeGrade(), g.computeGrade(), and u.computeGrade() will all perform the correct operations for their particular instances. In Java, the selection of the correct method occurs during the run of the program.

Dynamic Binding (Late Binding)

Making a run-time decision about which instance method to call is known as dynamic binding or late binding. Contrast this with selecting the correct method when methods are overloaded (see p. 99) rather than overridden. The compiler selects the correct overloaded method at compile time by comparing the methods’ signatures. This is known as static binding, or early binding. In polymorphism, the actual method that will be called is not determined by the compiler. Think of it this way: The compiler determines if a method can be called (i.e., is it legal?), while the run-time environment determines how it will be called (i.e., which overridden form should be used?).

Example 1

Student s = null;
Student u = new UnderGrad("Tim Broder", new int[] {90,90,100}, "none");
Student g = new GradStudent("Kevin Cristella",  
new int[] {85,70,90}, "none", 1234);
System.out.print("Enter student status: ");
System.out.println("Grad (G), Undergrad (U), Neither (N)");
String str = IO.readString(); //read user input
if (str.equals("G"))
    s = g;
else if (str.equals("U"))
    s = u;
else
    s = new Student();
s.computeGrade();
When this code fragment is run, the `computeGrade` method used will depend on the type of the actual object `s` refers to, which in turn depends on the user input.

**Example 2**

```java
public class StudentTest {
    public static void computeAllGrades(Student[] studentList) {
        for (Student s : studentList)
            if (s != null)
                s.computeGrade();
    }

    public static void main(String[] args) {
        Student[] stu = new Student[5];
        stu[0] = new Student("Brian Lorenzen", new int[] {90,94,99}, "none");
        stu[1] = new UnderGrad("Tim Broder", new int[] {90,90,100}, "none");
        stu[2] = new GradStudent("Kevin Cristella", new int[] {85,70,90}, "none", 1234);
        computeAllGrades(stu);
    }
}
```

Here an array of five `Student` references is created, all of them initially null. Three of these references, `stu[0]`, `stu[1]`, and `stu[2]`, are then assigned to actual objects. The `computeAllGrades` method steps through the array invoking for each of the objects the appropriate `computeGrade` method, using dynamic binding in each case. The null test in `computeAllGrades` is necessary because some of the array references could be null.

### Using `super` in a Subclass

A subclass can call a method in its superclass by using `super`. Suppose that the superclass method then calls another method that has been overridden in the subclass. By polymorphism, the method that is executed is the one in the subclass. The computer keeps track and executes any pending statements in either method.

**Example**

```java
public class Dancer {
    public void act() {
        System.out.print(" spin");
        doTrick();
    }

    public void doTrick() {
        System.out.print(" float");
    }
}
```
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public class Acrobat extends Dancer
{
    public void act()
    {
        super.act();
        System.out.print(" flip");
    }

    public void doTrick()
    {
        System.out.print(" somersault");
    }
}

Suppose the following declaration appears in a class other than Dancer or Acrobat:

Dancer a = new Acrobat();

What is printed as a result of the call a.act()?

When a.act() is called, the act method of Acrobat is executed. This is an example of polymorphism. The first line, super.act(), goes to the act method of Dancer, the superclass. This prints spin, then calls doTrick(). Again, using polymorphism, the doTrick method in Acrobat is called, printing somersault. Now, completing the act method of Acrobat, flip is printed. So what all got printed?

spin somersault flip

NOTE

Even though there are no constructors in either the Dancer or Acrobat classes, the declaration

Dancer a = new Acrobat();

compiles without error. This is because Dancer, while not having an explicit superclass, has an implicit superclass, Object, and gets its default (no-argument) constructor slotted into its code. Similarly the Acrobat class gets this constructor slotted into its code.

The statement Dancer a = new Acrobat(); will not compile, however, if the Dancer class has at least one constructor with parameters but no default constructor.

TYPE COMPATIBILITY

Downcasting

Consider the statements

Student s = new GradStudent();
GradStudent g = new GradStudent();
int x = s.getID(); //compile-time error
int y = g.getID(); //legal

Both s and g represent GradStudent objects, so why does s.getID() cause an error? The reason is that s is of type Student, and the Student class doesn’t have a getID method. At compile time, only nonprivate methods of the Student class can appear
to the right of the dot operator when applied to s. Don’t confuse this with polymorphism: `getID` is not a polymorphic method. It occurs in just the `GradStudent` class and can therefore be called only by a `GradStudent` object.

The error shown above can be fixed by casting s to the correct type:

```java
int x = ((GradStudent) s).getID();
```

Since s (of type `Student`) is actually representing a `GradStudent` object, such a cast can be carried out. Casting a superclass to a subclass type is called a downcast.

**NOTE**

1. The outer parentheses are necessary:

   ```java
   int x = (GradStudent) s.getID();
   ```

   will still cause an error, despite the cast. This is because the dot operator has higher precedence than casting, so `s.getID()` is invoked before s is cast to `GradStudent`.

2. The statement

   ```java
   int y = g.getID();
   ```

   compiles without problem because g is declared to be of type `GradStudent`, and this is the class that contains `getID`. No cast is required.

---

**Type Rules for Polymorphic Method Calls**

- For a declaration like

  ```java
  Superclass a = new Subclass();
  ```

  the type of a at compile time is `Superclass`; at run time it is `Subclass`.

- At compile time, method must be found in the class of a, that is, in `Superclass`. (This is true whether the method is polymorphic or not.) If method cannot be found in the class of a, you need to do an explicit cast on a to its actual type.

- For a polymorphic method, at run time the actual type of a is determined—`Subclass` in this example—and method is selected from `Subclass`. This could be an inherited method if there is no overriding method.

- The type of parameter b is checked at compile time. You may need to do an explicit cast to the subclass type to make this correct.
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The `ClassCastException`

The `ClassCastException` is a run-time exception thrown to signal an attempt to cast an object to a class of which it is not an instance.

```java
Student u = new UnderGrad();
System.out.println((String) u);  // ClassCastException
// u is not an instance of String
int x = ((GradStudent) u).getID();  // ClassCastException
// u is not an instance of GradStudent
```

ABSTRACT CLASSES

Abstract Class

An abstract class is a superclass that represents an abstract concept, and therefore should not be instantiated. For example, a maze program could have several different maze components—paths, walls, entrances, and exits. All of these share certain features (e.g., location, and a way of displaying). They can therefore all be declared as subclasses of the abstract class `MazeComponent`. The program will create path objects, wall objects, and so on, but no instances of `MazeComponent`.

An abstract class may contain abstract methods. An abstract method has no implementation code, just a header. The rationale for an abstract method is that there is no good default code for the method. Every subclass will need to override this method, so why bother with a meaningless implementation in the superclass? The method appears in the abstract class as a placeholder. The implementation for the method occurs in the subclasses. If a class contains any abstract methods, it must be declared an abstract class.

The `abstract` Keyword

An abstract class is declared with the keyword `abstract` in the header:

```java
public abstract class AbstractClass
{
    ...
}
```

The keyword `extends` is used as before to declare a subclass:

```java
public class SubClass extends AbstractClass
{
    ...
}
```

If a subclass of an abstract class does not provide implementation code for all the abstract methods of its superclass, it too becomes an abstract class and must be declared as such to avoid a compile-time error:

```java
public abstract class SubClass extends AbstractClass
{
    ...
}
```

Here is an example of an abstract class, with two concrete (nonabstract) subclasses:
public abstract class Shape
{
    private String name;

    //constructor
    public Shape(String shapeName)
    { name = shapeName; }

    public String getName()
    { return name; }

    public abstract double area();
    public abstract double perimeter();

    public double semiPerimeter()
    { return perimeter() / 2; }
}

public class Circle extends Shape
{
    private double radius;

    //constructor
    public Circle(double circleRadius, String circleName)
    { super(circleName);
        radius = circleRadius;
    }

    public double perimeter()
    { return 2 * Math.PI * radius; }

    public double area()
    { return Math.PI * radius * radius; }
}

public class Square extends Shape
{
    private double side;

    //constructor
    public Square(double squareSide, String squareName)
    { super(squareName);
        side = squareSide;
    }

    public double perimeter()
    { return 4 * side; }

    public double area()
    { return side * side; }
}
NOTE

1. It is meaningless to define `perimeter` and `area` methods for `Shape`—thus, these are declared as abstract methods.
2. An abstract class can have both instance variables and concrete (nonabstract) methods. See, for example, `name`, `getName`, and `semiPerimeter` in the `Shape` class.
3. Abstract methods are declared with the keyword `abstract`. There is no method body. The header is terminated with a semicolon.
4. A concrete (non-abstract) subclass of an abstract superclass must provide implementation code for all abstract methods of the superclass. Therefore both the `Circle` and `Square` classes implement both the `perimeter` and `area` methods.
5. It is possible for an abstract class to have no abstract methods. (An abstract subclass of an abstract superclass inherits the abstract methods without explicitly declaring them.)
6. An abstract class may or may not have constructors.
7. No instances can be created for an abstract class:

   ```java
   Shape a = new Shape("blob"); //Illegal.
   //Can't create instance of abstract class.
   Shape c = new Circle(1.5, "small circle"); //legal
   ```

8. Polymorphism works with abstract classes as it does with concrete classes:

   ```java
   Shape circ = new Circle(10, "circle");
   Shape sq = new Square(9.4, "square");
   Shape s = null;
   System.out.println("Which shape?");
   String str = IO.readString(); //read user input
   if (str.equals("circle"))
       s = circ;
   else
       s = sq;
   System.out.println("Area of " + s.getName() + " is " + s.area());
   ```

INTERFACES

Interface

An `interface` is a collection of related methods, either abstract (headers only) or default (implementation provided in the interface). Default methods are new in Java 8, and will not be tested on the AP exam. Non-default (i.e., abstract) methods will be tested on the exam and are discussed below.

Students may be required to design, create, or modify classes that implement interfaces with abstract methods.

The non-default methods are both public and abstract—no need to explicitly include these keywords. As such, they provide a framework of behavior for any class.

The classes that implement a given interface may represent objects that are vastly different. They all, however, have in common a capability or feature expressed in the methods of the interface. An interface called `FlyingObject`, for example, may have the methods `fly` and `isFlying`. Some classes that implement `FlyingObject` could be `Bird`,
Airplane, Missile, Butterfly, and Witch. A class called Turtle would be unlikely to implement FlyingObject because turtles don’t fly.

An interface called Computable may have just three methods: add, subtract, and multiply. Classes that implement Computable could be Fraction, Matrix, LongInteger, and ComplexNumber. It would not be meaningful, however, for a TelevisionSet to implement Computable—what does it mean, for example, to multiply two TelevisionSet objects?

A class that implements an interface can define any number of methods. In particular, it contracts to provide implementations for all the non-default (i.e., abstract) methods declared in the interface. If it fails to implement any of the methods, the class must be declared abstract.

Defining an Interface

An interface is declared with the interface keyword. For example,

```java
public interface FlyingObject
{
    void fly(); //method that simulates flight of object
    boolean isFlying(); //true if object is in flight, false otherwise
}
```

The implements Keyword

Interfaces are implemented using the implements keyword. For example,

```java
public class Bird implements FlyingObject
{
    ...
}
```

This declaration means that two of the methods in the Bird class must be fly and isFlying. Note that any subclass of Bird will automatically implement the interface FlyingObject, since fly and isFlying will be inherited by the subclass.

A class that extends a superclass can also directly implement an interface. For example,

```java
public class Mosquito extends Insect implements FlyingObject
{
    ...
}
```

NOTE

1. The extends clause must precede the implements clause.
2. A class can have just one superclass, but it can implement any number of interfaces:

```java
public class SubClass extends SuperClass
    implements Interface1, Interface2, ...
```

The Comparable Interface

Starting in 2015, this will not be tested on the AP exam. Students will, however, be required to use compareTo for comparison of strings (p. 178). The standard java.lang package contains the Comparable interface, which provides a useful method for comparing objects.
public interface Comparable
{
    int compareTo(Object obj);
}

Any class that implements Comparable must provide a compareTo method. This method compares the implicit object (this) with the parameter object (obj) and returns a negative integer, zero, or a positive integer depending on whether the implicit object is less than, equal to, or greater than the parameter. If the two objects being compared are not type compatible, a ClassCastException is thrown by the method.

Example

The abstract Shape class defined previously (p. 143) is modified to implement the Comparable interface:

```java
public abstract class Shape implements Comparable {
    private String name;

    //constructor
    public Shape(String shapeName)
    { name = shapeName; }

    public String getName()
    { return name; }

    public abstract double area();
    public abstract double perimeter();

    public double semiPerimeter()
    { return perimeter() / 2; }

    public int compareTo(Object obj)
    {
        final double EPSILON = 1.0e-15;  //slightly bigger than
        //machine precision
        Shape rhs = (Shape) obj;
        double diff = area() - rhs.area();
        if (Math.abs(diff) <= EPSILON * Math.abs(area()))
            return 0;  //area of this shape equals area of obj
        else if (diff < 0)
            return -1;  //area of this shape less than area of obj
        else
            return 1;  //area of this shape greater than area of obj
    }
}
```

NOTE

1. The Circle, Square, and other subclasses of Shape will all automatically implement Comparable and inherit the compareTo method.
2. It is tempting to use a simpler test for equality of areas, namely

   ```java
   if (diff == 0)
       return 0;
   ```
But recall that real numbers can have round-off errors in their storage (Box p. 65). This means that the simple test may return false even though the two areas are essentially equal. A more robust test is implemented in the code given, namely to test if the relative error in diff is small enough to be considered zero.

3. The Object class is a universal superclass (see p. 174). This means that the compareTo method can take as a parameter any object reference that implements Comparable.

4. One of the first steps of a compareTo method must cast the Object argument to the class type, in this case Shape. If this is not done, the compiler won’t find the area method—remember, an Object is not necessarily a Shape.

5. The algorithm one chooses in compareTo should in general be consistent with the equals method (see p. 176): Whenever object1.equals(object2) returns true, object1.compareTo(object2) returns 0.

Here is a program that finds the larger of two Comparable objects.

```java
public class FindMaxTest
{
    /** Return the larger of two objects a and b. */
    public static Comparable max(Comparable a, Comparable b)
    {
        if (a.compareTo(b) > 0) //if a > b ...
            return a;
        else
            return b;
    }

    /** Test max on two Shape objects. */
    public static void main(String[] args)
    {
        Shape s1 = new Circle(3.0, "circle");
        Shape s2 = new Square(4.5, "square");
        System.out.println("Area of " + s1.getName() + " is " +
            s1.area());
        System.out.println("Area of " + s2.getName() + " is " +
            s2.area());
        Shape s3 = (Shape) max(s1, s2);
        System.out.println("The larger shape is the " +
            s3.getName());
    }
}
```

Here is the output:

```
Area of circle is 28.27
Area of square is 20.25
The larger shape is the circle
```

NOTE

1. The max method takes parameters of type Comparable. Since s1 is a Comparable object and s2 is a Comparable object, no casting is necessary in the method call.
2. The max method can be called with any two Comparable objects, for example, two String objects or two Integer objects (see Chapter 4).
3. The objects must be type compatible (i.e., it must make sense to compare them). For example, in the program shown, if \( s1 \) is-a \textit{Shape} and \( s2 \) is-a \textit{String}, the \texttt{compareTo} method will throw a \texttt{ClassCastException} at the line

\[
\text{Shape rhs = (Shape) obj;}
\]

4. The cast is needed in the line

\[
\text{Shape s3 = (Shape) max(s1, s2);}
\]

since \texttt{max(s1, s2)} returns a \texttt{Comparable}.

5. A primitive type is not an object and therefore cannot be passed as \texttt{Comparable}. You can, however, use a wrapper class and in this way convert a primitive type to a \texttt{Comparable} (see p. 180).

**ABSTRACT CLASS VS. INTERFACE**

Consider writing a program that simulates a game of Battleships. The program may have a \texttt{Ship} class with subclasses \texttt{Submarine}, \texttt{Cruiser}, \texttt{Destroyer}, and so on. The various ships will be placed in a two-dimensional grid that represents a part of the ocean.

An abstract class \texttt{Ship} is a good design choice. There will not be any instances of \texttt{Ship} objects because the specific features of the subclasses must be known in order to place these ships in the grid. A \texttt{Grid} interface that manipulates objects in a two-dimensional setting suggests itself for the two-dimensional grid.

Notice that the abstract \texttt{Ship} class is specific to the Battleships application, whereas the \texttt{Grid} interface is not. You could use the \texttt{Grid} interface in any program that has a two-dimensional grid.

**Interface vs. Abstract Class**

- Use an abstract class for an object that is application-specific but incomplete without its subclasses.
- Consider using an interface when its methods are suitable for your program but could be equally applicable in a variety of programs.
- An interface typically doesn’t provide implementations for any of its methods, whereas an abstract class does. (In Java 8, implementation of default methods is allowed in interfaces.)
- An interface cannot contain instance variables, whereas an abstract class can.
- It is not possible to create an instance of an interface object or an abstract class object.
Chapter Summary

You should be able to write your own subclasses, given any superclass, and also design, create, or modify a class that implements an interface.

Be sure you understand the use of the keyword `super`, both in writing constructors and calling methods of the superclass.

You should understand what polymorphism is: Recall that it only operates when methods have been overridden in at least one subclass. You should also be able to explain the difference between the following concepts:

- An abstract class and an interface.
- An overloaded method and an overridden method.
- Dynamic binding (late binding) and static binding (early binding).
MULTIPLE-CHOICE QUESTIONS ON INHERITANCE AND POLYMORPHISM

Questions 1–10 refer to the BankAccount, SavingsAccount, and CheckingAccount classes defined below:

```java
public class BankAccount
{
    private double balance;
    
    public BankAccount()
    { balance = 0; }
    
    public BankAccount(double acctBalance)
    { balance = acctBalance; }
    
    public void deposit(double amount)
    { balance += amount; }
    
    public void withdraw(double amount)
    { balance -= amount; }
    
    public double getBalance()
    { return balance; }
}

public class SavingsAccount extends BankAccount
{
    private double interestRate;
    
    public SavingsAccount()
    { /* implementation not shown */ }
    
    public SavingsAccount(double acctBalance, double rate)
    { /* implementation not shown */ }
    
    public void addInterest() //Add interest to balance
    { /* implementation not shown */ }
}

public class CheckingAccount extends BankAccount
{
    private static final double FEE = 2.0;
    private static final double MIN_BALANCE = 50.0;
    
    public CheckingAccount(double acctBalance)
    { /* implementation not shown */ }
    
    /** FEE of $2 deducted if withdrawal leaves balance less
     * than MIN_BALANCE. Allows for negative balance. */
    public void withdraw(double amount)
    { /* implementation not shown */ }
}
```
Multiple-Choice Questions on Inheritance and Polymorphism

1. Of the methods shown, how many different nonconstructor methods can be invoked by a SavingsAccount object?
   (A) 1
   (B) 2
   (C) 3
   (D) 4
   (E) 5

2. Which of the following correctly implements the default constructor of the SavingsAccount class?
   I
   ```java
   interestRate = 0;
   super();
   ```
   II
   ```java
   super();
   interestRate = 0;
   ```
   III
   ```java
   super();
   ```
   (A) II only
   (B) I and II only
   (C) II and III only
   (D) III only
   (E) I, II, and III

3. Which is a correct implementation of the constructor with parameters in the SavingsAccount class?
   (A)
   ```java
   balance = acctBalance;
   interestRate = rate;
   ```
   (B)
   ```java
   getBalance() = acctBalance;
   interestRate = rate;
   ```
   (C)
   ```java
   super();
   interestRate = rate;
   ```
   (D)
   ```java
   super(acctBalance);
   interestRate = rate;
   ```
   (E)
   ```java
   super(acctBalance, rate);
   ```

4. Which is a correct implementation of the CheckingAccount constructor?
   I
   ```java
   super(acctBalance);
   ```
   II
   ```java
   super();
   deposit(acctBalance);
   ```
   III
   ```java
   deposit(acctBalance);
   ```
   (A) I only
   (B) II only
   (C) III only
   (D) II and III only
   (E) I, II, and III
5. Which is correct implementation code for the withdraw method in the CheckingAccount class?

(A) super.withdraw(amount);
    if (balance < MIN_BALANCE)
        super.withdraw(FEE);

(B) withdraw(amount);
    if (balance < MIN_BALANCE)
        withdraw(FEE);

(C) super.withdraw(amount);
    if (getBalance() < MIN_BALANCE)
        super.withdraw(FEE);

(D) withdraw(amount);
    if (getBalance() < MIN_BALANCE)
        withdraw(FEE);

(E) balance -= amount;
    if (balance < MIN_BALANCE)
        balance -= FEE;

6. Redefining the withdraw method in the CheckingAccount class is an example of
   (A) method overloading.
   (B) method overriding.
   (C) downcasting.
   (D) dynamic binding (late binding).
   (E) static binding (early binding).

Use the following for Questions 7–9.
A program to test the BankAccount, SavingsAccount, and CheckingAccount classes has these declarations:

BankAccount b = new BankAccount(1400);
BankAccount s = new SavingsAccount(1000, 0.04);
BankAccount c = new CheckingAccount(500);

7. Which method call will cause an error?
   (A) b.deposit(200);
   (B) s.withdraw(500);
   (C) c.withdraw(500);
   (D) s.deposit(10000);
   (E) s.addInterest();

8. In order to test polymorphism, which method must be used in the program?
   (A) Either a SavingsAccount constructor or a CheckingAccount constructor
   (B) addInterest
   (C) deposit
   (D) withdraw
   (E) getBalance
9. Which of the following will not cause a ClassCastException to be thrown?
(A) ((SavingsAccount) b).addInterest();
(B) ((CheckingAccount) b).withdraw(200);
(C) ((CheckingAccount) c).deposit(800);
(D) ((CheckingAccount) s).withdraw(150);
(E) ((SavingsAccount) c).addInterest();

10. A new method is added to the BankAccount class.

```java
/** Transfer amount from this BankAccount to another BankAccount. 
 * Precondition: balance > amount 
 * @param another a different BankAccount object 
 * @param amount the amount to be transferred 
 */
public void transfer(BankAccount another, double amount) {
    withdraw(amount);
    another.deposit(amount);
}
```

A program has these declarations:

```java
BankAccount b = new BankAccount(650);
SavingsAccount timsSavings = new SavingsAccount(1500, 0.03);
CheckingAccount daynasChecking = new CheckingAccount(2000);
```

Which of the following will transfer money from one account to another without error?

I b.transfer(timsSavings, 50);
II timsSavings.transfer(daynasChecking, 30);
III daynasChecking.transfer(b, 55);

(A) I only
(B) II only
(C) III only
(D) I, II, and III
(E) None
Chapter 3  Inheritance and Polymorphism

11. Consider these class declarations:

```java
public class Person {
    ...
}

public class Teacher extends Person {
    ...
}
```

Which is a true statement?

I Teacher inherits the constructors of Person.
II Teacher can add new methods and private instance variables.
III Teacher can override existing private methods of Person.

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) II and III only

12. Which statement about abstract classes and interfaces is false?

(A) An interface cannot implement any non-default instance methods, whereas an abstract class can.
(B) A class can implement many interfaces but can have only one superclass.
(C) An unlimited number of unrelated classes can implement the same interface.
(D) It is not possible to construct either an abstract class object or an interface object.
(E) All of the methods in both an abstract class and an interface are public.
13. Consider the following hierarchy of classes:

![Class Hierarchy Diagram]

A program is written to print data about various birds:

```java
public class BirdStuff {
    public static void printName(Bird b) {
        /* implementation not shown */
    }
    public static void printBirdCall(Parrot p) {
        /* implementation not shown */
    }
    //several more Bird methods
    public static void main(String[] args) {
        Bird bird1 = new Bird();
        Bird bird2 = new Parrot();
        Parrot parrot1 = new Parrot();
        Parrot parrot2 = new Parakeet();
        /* more code */
    }
}
```

Assuming that none of the given classes is abstract and all have default constructors, which of the following segments of /* more code */ will not cause an error?

(A) printName(parrot2);
    printBirdCall((Parrot) bird2);

(B) printName((Parrot) bird1);
    printBirdCall(bird2);

(C) printName(bird2);
    printBirdCall(bird2);

(D) printName((Parakeet) parrot1);
    printBirdCall(parrot2);

(E) printName((Owl) parrot2);
    printBirdCall((Parakeet) parrot2);
Chapter 3  Inheritance and Polymorphism

Refer to the classes below for Questions 14 and 15.

```java
public class ClassA {
    //default constructor not shown ...
    public void method1() {
        /* implementation of method1 */
    }
}

public class ClassB extends ClassA {
    //default constructor not shown ...
    public void method1() {
        /* different implementation from method1 in ClassA*/
    }
    public void method2() {
        /* implementation of method2 */
    }
}
```

14. The `method1` method in `ClassB` is an example of
(A) method overloading.
(B) method overriding.
(C) polymorphism.
(D) information hiding.
(E) procedural abstraction.

15. Consider the following declarations in a client class.

```java
ClassA ob1 = new ClassA();
ClassA ob2 = new ClassB();
```

Which of the following method calls will cause an error?

I  `ob1.method2();`
II `ob2.method2();`
III `((ClassB) ob1).method2();`

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III
Multiple-Choice Questions on Inheritance and Polymorphism

Use the declarations below for Questions 16–18.

```java
public abstract class Solid
{
    private String name;

    //constructor
    public Solid(String solidName)
    { name = solidName; }

    public String getName()
    { return name; }

    public abstract double volume();
}

public class Sphere extends Solid
{
    private double radius;

    //constructor
    public Sphere(String sphereName, double sphereRadius)
    {
        super(sphereName);
        radius = sphereRadius;
    }

    public double volume()
    { return (4.0/3.0) * Math.PI * radius * radius * radius; }
}

public class RectangularPrism extends Solid
{
    private double length;
    private double width;
    private double height;

    //constructor
    public RectangularPrism(String prismName, double l, double w, double h)
    {
        super(prismName);
        length = l;
        width = w;
        height = h;
    }

    public double volume()
    { return length * width * height; }
}
```
Chapter 3 Inheritance and Polymorphism

16. A program that tests these classes has the following declarations and assignments:

```java
Solid s1, s2, s3, s4;
s1 = new Solid("blob");
s2 = new Sphere("sphere", 3.8);
s3 = new RectangularPrism("box", 2, 4, 6.5);
s4 = null;
```

How many of the above lines of code are incorrect?

(A) 0
(B) 1
(C) 2
(D) 3
(E) 4

17. Which is false?

(A) If a program has several objects declared as type Solid, the decision about which volume method to call will be resolved at run time.
(B) If the Solid class were modified to provide a default implementation for the volume method, it would no longer need to be an abstract class.
(C) If the Sphere and RectangularPrism classes failed to provide an implementation for the volume method, they would need to be declared as abstract classes.
(D) The fact that there is no reasonable default implementation for the volume method in the Solid class suggests that it should be an abstract method.
(E) Since Solid is abstract and its subclasses are nonabstract, polymorphism no longer applies when these classes are used in a program.
18. Here is a program that prints the volume of a solid:

```java
public class SolidMain {
    /** Output volume of Solid s. */
    public static void printVolume(Solid s) {
        System.out.println("Volume = " + s.volume() + " cubic units");
    }

    public static void main(String[] args) {
        Solid sol;
        Solid sph = new Sphere("sphere", 4);
        Solid rec = new RectangularPrism("box", 3, 6, 9);
        int flipCoin = (int) (Math.random() * 2); // 0 or 1
        if (flipCoin == 0)
            sol = sph;
        else
            sol = rec;
        printVolume(sol);
    }
}
```

Which is a true statement about this program?
(A) It will output the volume of the sphere or box, as intended.
(B) It will output the volume of the default Solid s, which is neither a sphere nor a box.
(C) A ClassCastException will be thrown.
(D) A compile-time error will occur because there is no implementation code for volume in the Solid class.
(E) A run-time error will occur because of parameter type mismatch in the method call `printVolume(sol)`.
19. Consider the Computable interface below for performing simple calculator operations:

```java
public interface Computable {
    /** Return this Object + y. */
    Object add(Object y);

    /** Return this Object - y. */
    Object subtract(Object y);

    /** Return this Object * y. */
    Object multiply(Object y);
}
```

Which of the following is the least suitable class for implementing Computable?

(A) LargeInteger //integers with 100 digits or more
(B) Fraction //implemented with numerator and
    //denominator of type int
(C) IrrationalNumber //nonrepeating, nonterminating decimal
(D) Length //implemented with different units, such
    //as inches, centimeters, etc.
(E) BankAccount //implemented with balance

Refer to the Player interface shown below for Questions 20–23.

```java
public interface Player {
    /** Return an integer that represents a move in a game. */
    int getMove();

    /** Display the status of the game for this Player after
     * implementing the next move. */
    void updateDisplay();
}
```

20. HumanPlayer is a class that implements the Player interface. Another class,
    SmartPlayer, is a subclass of HumanPlayer. Which statement is false?
(A) SmartPlayer automatically implements the Player interface.
(B) HumanPlayer must contain implementations of both the updateDisplay and
    getMove methods, or be declared as abstract.
(C) It is not possible to declare a reference of type Player.
(D) The SmartPlayer class can override the methods updateDisplay and
    getMove of the HumanPlayer class.
(E) A method in a client program can have Player as a parameter type.
21. A programmer plans to write programs that simulate various games. In each case he will have several classes, each representing a different kind of competitor in the game, such as ExpertPlayer, ComputerPlayer, RecklessPlayer, CheatingPlayer, Beginner, IntermediatePlayer, and so on. It may or may not be suitable for these classes to implement the Player interface, depending on the particular game being simulated. In the games described below, which is the least suitable for having the competitor classes implement the given Player interface?

(A) High-Low Guessing Game: The computer thinks of a number and the competitor who guesses it with the least number of guesses wins. After each guess, the computer tells whether its number is higher or lower than the guess.

(B) Chips: Start with a pile of chips. Each player in turn removes some number of chips. The winner is the one who removes the final chip. The first player may remove any number of chips, but not all of them. Each subsequent player must remove at least one chip and at most twice the number removed by the preceding player.

(C) Chess: Played on a square board of 64 squares of alternating colors. There are just two players, called White and Black, the colors of their respective pieces. The players each have a set of pieces on the board that can move according to a set of rules. The players alternate moves, where a move consists of moving any one piece to another square. If that square is occupied by an opponent’s piece, the piece is captured and removed from the board.

(D) Tic-Tac-Toe: Two players alternate placing “X” or “O” on a 3 × 3 grid. The first player to get three in a row, where a row can be vertical, horizontal, or diagonal, wins.

(E) Battleships: There are two players, each with a 10 × 10 grid hidden from his opponent. Various “ships” are placed on the grid. A move consists of calling out a grid location, trying to “hit” an opponent’s ship. Players alternate moves. The first player to sink his opponent’s fleet wins.
Consider these declarations for Questions 22 and 23:

```java
public class HumanPlayer implements Player {
    private String name;
    //Constructors not shown ...
    //Code to implement getMove and updateDisplay not shown ...

    public String getName()
    { /* implementation not shown */ }
}

public class ExpertPlayer extends HumanPlayer {
    private int rating;
    //Constructors not shown ...

    public int compareTo(ExpertPlayer expert)
    { /* implementation not shown */ }
}
```

22. Which code segment in a client program will cause an error?

```java
I Player p1 = new HumanPlayer();
    Player p2 = new ExpertPlayer();
    int x1 = p1.getMove();
    int x2 = p2.getMove();

II int x;
    Player c1 = new ExpertPlayer(/* correct parameter list */);
    Player c2 = new ExpertPlayer(/* correct parameter list */);
    if (c1.compareTo(c2) < 0)
        x = c1.getMove();
    else
        x = c2.getMove();

III int x;
    HumanPlayer h1 = new HumanPlayer(/* correct parameter list */);
    HumanPlayer h2 = new HumanPlayer(/* correct parameter list */);
    if (h1.compareTo(h2) < 0)
        x = h1.getMove();
    else
        x = h2.getMove();
```

(A) II only 
(B) III only 
(C) II and III only 
(D) I, II, and III 
(E) None
23. Which of the following is correct implementation code for the `compareTo` method in the `ExpertPlayer` class?

I if (rating == expert.rating)
   return 0;
else if (rating < expert.rating)
   return -1;
else
   return 1;

II return rating - expert.rating;

III if (getName().equals(expert.getName()))
   return 0;
else if (getName().compareTo(expert.getName()) < 0)
   return -1;
else
   return 1;

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
24. Which of the following classes is the least suitable candidate for containing a `compareTo` method?

(A) public class Point
{
    private double x;
    private double y;

    // various methods follow

}

(B) public class Name
{
    private String firstName;
    private String lastName;

    // various methods follow

}

(C) public class Car
{
    private int modelNumber;
    private int year;
    private double price;

    // various methods follow

}

(D) public class Student
{
    private String name;
    private double gpa;

    // various methods follow

}

(E) public class Employee
{
    private String name;
    private int hireDate;
    private double salary;

    // various methods follow

}
25. A programmer has the task of maintaining a database of students of a large university. There are two types of students, undergraduates and graduate students. About a third of the graduate students are doctoral candidates.

All of the students have the same personal information stored, like name, address, and phone number, and also student information like courses taken and grades. Each student’s GPA is computed, but differently for undergraduates and graduates. The doctoral candidates have information about their dissertations and faculty advisors.

The programmer will write a Java program to handle all the student information. Which of the following is the best design, in terms of programmer efficiency and code reusability? Note: { ... } denotes class code.

(A) public interface Student {
    ...
    public class Undergraduate implements Student {
        ...
    }
    public class Graduate implements Student {
        ...
    }
    public class DocStudent extends Graduate {
        ...
    }
}

(B) public abstract class Student {
    ...
    public class Undergraduate extends Student {
        ...
    }
    public class Graduate extends Student {
        ...
    }
    public class DocStudent extends Graduate {
        ...
    }
}

(C) public class Student {
    ...
    public class Undergraduate extends Student {
        ...
    }
    public class Graduate extends Student {
        ...
    }
    public class DocStudent extends Graduate {
        ...
    }
}

(D) public abstract class Student {
    ...
    public class Undergraduate extends Student {
        ...
    }
    public class Graduate extends Student {
        ...
    }
    public class DocStudent extends Student {
        ...
    }
}

(E) public interface PersonalInformation {
    ...
    public class Student implements PersonalInformation {
        ...
    }
    public class Undergraduate extends Student {
        ...
    }
    public abstract class Graduate extends Student {
        ...
    }
    public class DocStudent extends Graduate {
        ...
    }
}
26. Consider the `Orderable` interface and the partial implementation of the `Temperature` class defined below:

```java
public interface Orderable
{
    /** Returns -1, 0, or 1 depending on whether the implicit object is less than, equal to, or greater than other. */
    int compareTo (Object other);
}

public class Temperature implements Orderable
{
    private String scale;
    private double degrees;

    //default constructor
    public Temperature () { /* implementation not shown */ }

    //constructor
    public Temperature(String tempScale, double tempDegrees) { /* implementation not shown */ }

    public int compareTo(Object obj) { /* implementation not shown */ }

    public String toString() { /* implementation not shown */ }

    //Other methods are not shown.
}
```

Here is a program that finds the lowest of three temperatures:

```java
public class TemperatureMain
{
    /** Find smaller of objects a and b. */
    public static Orderable min(Orderable a, Orderable b)
    {
        if (a.compareTo(b) < 0)
            return a;
        else
            return b;
    }

    /** Find smallest of objects a, b, and c. */
    public static Orderable minThree(Orderable a, Orderable b, Orderable c)
    {
        return min(min(a, b), c);
    }

    public static void main(String[] args)
    {
        /* code to test minThree method */
    }
}
```
Multiple-Choice Questions on Inheritance and Polymorphism

Which are correct replacements for `/* code to test minThree method */`?

I. `Temperature t1 = new Temperature("C", 85);`  
   `Temperature t2 = new Temperature("F", 45);`  
   `Temperature t3 = new Temperature("F", 120);`  
   `System.out.println("The lowest temperature is " + minThree(t1, t2, t3));`

II. `Orderable c1 = new Temperature("C", 85);`  
    `Orderable c2 = new Temperature("F", 45);`  
    `Orderable c3 = new Temperature("F", 120);`  
    `System.out.println("The lowest temperature is " + minThree(c1, c2, c3));`

III. `Orderable c1 = new Orderable("C", 85);`  
     `Orderable c2 = new Orderable("F", 45);`  
     `Orderable c3 = new Orderable("F", 120);`  
     `System.out.println("The lowest temperature is " + minThree(c1, c2, c3));`

(A) II only  
(B) I and II only  
(C) II and III only  
(D) I and III only  
(E) I, II, and III
27. A certain interface provided by a Java package contains just a single method:

```java
public interface SomeName
{
    int method1(Object o);
}
```

A programmer adds some functionality to this interface by adding another abstract method to it, `method2`:

```java
public interface SomeName
{
    int method1(Object ob1);
    void method2(Object ob2);
}
```

As a result of this addition, which of the following is true?

(A) A `ClassCastException` will occur if `ob1` and `ob2` are not compatible.
(B) All classes that implement the original `SomeName` interface will need to be rewritten because they no longer implement `SomeName`.
(C) A class that implements the original `SomeName` interface will need to modify its declaration as follows:

```java
public class ClassName implements SomeName extends method2
{
    ...
}
```

(D) `SomeName` will need to be changed to an abstract class and provide implementation code for `method2`, so that the original and upgraded versions of `SomeName` are compatible.

(E) Any new class that implements the upgraded version of `SomeName` will not compile.
ANSWER KEY

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ANSWERS EXPLAINED

1. (D) The methods are deposit, withdraw, and getBalance, all inherited from the BankAccount class, plus addInterest, which was defined just for the class SavingsAccount.

2. (C) Implementation I fails because super() must be the first line of the implementation whenever it is used in a constructor. Implementation III may appear to be incorrect because it doesn’t initialize interestRate. Since interestRate, however, is a primitive type—double—the compiler will provide a default initialization of 0, which was required.

3. (D) First, the statement super(acctBalance) initializes the inherited private variable balance as for the BankAccount superclass. Then the statement interestRate = rate initializes interestRate, which belongs uniquely to the SavingsAccount class. Choice E fails because interestRate does not belong to the BankAccount class and therefore cannot be initialized by a super method. Choice A is wrong because the SavingsAccount class cannot directly access the private instance variables of its superclass. Choice B assigns a value to an accessor method, which is meaningless. Choice C is incorrect because super() invokes the default constructor of the superclass. This will cause balance of the SavingsAccount object to be initialized to 0, rather than acctBalance, the parameter value.

4. (E) The constructor must initialize the inherited instance variable balance to the value of the acctBalance parameter. All three segments achieve this. Implementation I does it by invoking super(acctBalance), the constructor in the superclass. Implementation II first initializes balance to 0 by invoking the default constructor of the superclass. Then it calls the inherited deposit method of the superclass to add acctBalance to the account. Implementation III works because super() is automatically called as the first line of the constructor code if there is no explicit call to super.

5. (C) First the withdraw method of the BankAccount superclass is used to withdraw amount. A prefix of super must be used to invoke this method, which eliminates
choices B and D. Then the balance must be tested using the accessor method `getBalance`, which is inherited. You can't test `balance` directly since it is private to the `BankAccount` class. This eliminates choices A and E, and provides another reason for eliminating choice B.

6. (B) When a superclass method is redefined in a subclass, the process is called `method overriding`. Which method to call is determined at run time. This is called `dynamic binding` (p. 138). `Method overloading` is two or more methods with different signatures in the same class (p. 99). The compiler recognizes at compile time which method to call. This is `early binding`. The process of `downcasting` is unrelated to these principles (p. 140).

7. (E) The `addInterest` method is defined only in the `SavingsAccount` class. It therefore cannot be invoked by a `BankAccount` object. The error can be fixed by casting `s` to the correct type:

```java
((SavingsAccount) s).addInterest();
```

The other method calls do not cause a problem because `withdraw` and `deposit` are both methods of the `BankAccount` class.

8. (D) The `withdraw` method is the only method that has one implementation in the superclass and a `different` implementation in a subclass. Polymorphism is the mechanism of selecting the correct method from the different possibilities in the class hierarchy. Notice that the `deposit` method, for example, is available to objects of all three bank account classes, but it's the `same` code in all three cases. So polymorphism isn't tested.

9. (C) You will get a `ClassCastException` whenever you try to cast an object to a class of which it is not an instance. Choice C is the only statement that doesn't attempt to do this. Look at the other choices: In choice A, `b` is not an instance of `SavingsAccount`. In choice B, `b` is not an instance of `CheckingAccount`. In choice D, `s` is not an instance of `CheckingAccount`. In choice E, `c` is not an instance of `SavingsAccount`.

10. (D) It is OK to use `timsSavings` and `daynasChecking` as parameters since each of these is a `BankAccount` object. It is also OK for `timsSavings` and `daynasChecking` to call the `transfer` method (statements II and III), since they inherit this method from the `BankAccount` superclass.

11. (B) Statement I is false: A subclass must specify its own constructors. Otherwise the default constructor of the superclass will automatically be invoked. Note that statement III is false: Private instance methods cannot be overridden.

12. (E) All of the methods in an interface are by default public (the `public` keyword isn't needed). An abstract class can have both private and public methods. Note that choice A would be false if it simply stated “An interface cannot implement any methods, whereas an abstract class can.” Java 8 allows an interface to implement default methods.

13. (A) There are two quick tests you can do to find the answer to this question:

1. Test the `is-a` relationship, namely the parameter for `printName` is a `Bird` and the parameter for `printBirdCall` is a `Parrot`?
2. A reference cannot be cast to something it's not an instance of.

Choice A passes both of these tests: `parrot2` is a `Bird`, and (Parrot) `bird2`
is a Parrot. Also bird2 is an instance of a Parrot (as you can see by looking at the right-hand side of the assignment), so the casting is correct. In choice B, printBirdCall(bird2) is wrong because bird2 is a Bird and the printBirdCall method is expecting a Parrot. Therefore bird2 must be downcast to a Parrot. Also, the method call printName((Parrot) bird1) fails because bird1 is an instance of a Bird and therefore cannot be cast to a Parrot. In choice C, printName(bird2) is correct: bird2 is a Bird. However, printBirdCall(bird2) fails as already discussed. In choice D, (Parakeet) parrot1 is an incorrect cast: parrot1 is an instance of a Parrot. Note that printBirdCall(parrot2) is OK since parrot2 is a Parrot. In choice E, (Owl) parrot2 is an incorrect cast: parrot2 is an instance of Parakeet. Note that printBirdCall((Parakeet) parrot2) is correct: A Parakeet is a Parrot, and parrot2 is an instance of a Parakeet.

14. (B) Method overriding occurs whenever a method in a superclass is redefined in a subclass. Method overloading is a method in the same class that has the same name but different parameter types. Polymorphism is when the correct overridden method is called for a particular subclass object during run time. Information hiding is the use of private to restrict access. Procedural abstraction is the use of helper methods.

15. (E) All will cause an error!

I: An object of a superclass does not have access to a new method of its subclass.
II: ob2 is declared to be of type ClassA, so a compile-time error will occur with a message indicating that there is no method2 in ClassA. Casting ob2 to ClassB would correct the problem.
III: A ClassCastException will be thrown, since ob1 is of type ClassA, and therefore cannot be cast to ClassB.

16. (B) The only incorrect line is s1 = new Solid("blob"): You can’t create an instance of an abstract class. Abstract class references can, however, refer to objects of concrete (nonabstract) subclasses. Thus, the assignments for s2 and s3 are OK. Note that an abstract class reference can also be null, so the final assignment, though redundant, is correct.

17. (E) The point of having an abstract method is to postpone until run time the decision about which subclass version to call. This is what polymorphism is—calling the appropriate method at run time based on the type of the object.

18. (A) This is an example of polymorphism: The correct volume method is selected at run time. The parameter expected for printVolume is a Solid reference, which is what it gets in main(). The reference s1 will refer either to a Sphere or a RectangularPrism object depending on the outcome of the coin flip. Since a Sphere is a Solid and a RectangularPrism is a Solid, there will be no type mismatch when these are the actual parameters in the printVolume method. (Note: The Math.random method is discussed in Chapter 4.)

19. (E) Each of choices A though D represent Computable objects: It makes sense to add, subtract, or multiply two large integers, two fractions, two irrational numbers, and two lengths. (One can multiply lengths to get an area, for example.) While it may make sense under certain circumstances to add or subtract two bank accounts, it does not make sense to multiply them!

20. (C) You can declare a reference of type Player. What you cannot do is construct an object of type Player. The following declarations are therefore legal:
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```java
SmartPlayer s = new SmartPlayer();
Player p1 = s;
Player p2 = new HumanPlayer();
```

21. (C) Remember, to implement the `Player` interface a class must provide implementations for `getMove` and `updateDisplay`. The `updateDisplay` method is suitable for all five games described. The `getMove` method returns a single integer, which works well for the High-Low game of choice A and the Chips game of choice B. In Tic-Tac-Toe (choice D) and Battleships (choice E) a move consists of giving a grid location. This can be provided by a single integer if the grid locations are numbered in a unique way. It’s not ideal, but certainly doable. In the Chess game, however, it’s neither easy nor intuitive to describe a move with a single integer. The player needs to specify both the grid location he is moving the piece to and which piece he is moving. The `getMove` method would need to be altered in a way that changes its return type. This makes the `Player` interface unsuitable.

22. (C) Segments II and III have errors in the `compareTo` calls. References `c1` and `c2` are of type `Player`, which doesn’t have a `compareTo` method, and references `h1` and `h2` are of type `HumanPlayer`, which also doesn’t have a `compareTo` method. Note that Segment II can be fixed by downcasting `c1` and `c2` to `ExpertPlayer`:

```java
if (((ExpertPlayer) c1).compareTo((ExpertPlayer) c2) < 0)
```

A cast won’t work in Segment III, because you can’t cast a `HumanPlayer` to an `ExpertPlayer`. In Segments I, II, and III, the `getMove` calls are all correct, because `p1`, `p2`, `c1`, and `c2` are all of type `Player` which has a `getMove` method; and `h1` and `h2` are of type `HumanPlayer` which implements `Player` and therefore has a `getMove` method.

23. (E) All implementations are correct. This is not a question about whether it is better to compare `ExpertPlayers` based on their ratings or their names! One might need an alphabetized list of players, or one might need a list according to ranking. In practice, the program specification will instruct the programmer which to use. Note that segment II is correct because `compareTo` doesn’t need to return 1 or -1. Any positive or negative integer is OK. Note also that in segments I and II it is OK to use `expert.rating`, since `expert` is of type `ExpertPlayer`, the current class being written. Normally, a parameter of some class type cannot access the private instance variables of another class.

24. (A) While it is certainly possible to write a `compareTo` method for a `Point` class, there’s no good intuitive way to compare points. Two points `(x₁, y₁)` and `(x₂, y₂)` are equal if and only if `x₁ = x₂` and `y₁ = y₂`. But if points `P₁` and `P₂` are not equal, what will determine if `P₁ < P₂` or `P₁ > P₂`? You could try using the distance from the origin. Define `P₁ > P₂` if and only if `OP₁ > OP₂`, and `P₁ < P₂` if and only if `OP₁ < OP₂`, where `O` is `(0,0)`. This definition means that points `(a, b)` and `(b, a)` are equal, which violates the definition of equals! The problem is that there is no way to map the two-dimensional set of points to a one-dimensional distance function and still be consistent with the definition of equals. The objects in each of the other classes can be compared without a problem. In choice B, two `Name` objects can be ordered alphabetically. In choice C, two `Car` objects can be ordered by year or by price. In choice D, two `Student` objects can be ordered by name or GPA. In choice E, two `Employee` objects can be ordered by name or seniority (date of hire).
25. (B) Here is the hierarchy of classes:

```
Student
  /   \                     /   \         
Undergraduate Graduate DocStudent
```

Eliminate choice D which fails to make DocStudent a subclass of Graduate. This is a poor design choice since a DocStudent is a Graduate. Making Student an abstract class is desirable since the methods that are common to all students can go in there with implementations provided. The method to calculate the GPA, which differs among student types, will be declared in Student as an abstract method. Then unique implementations will be provided in both the Graduate and Undergraduate classes. Choice A is a poor design because making Student an interface means that all of its methods will need to be implemented in both the Undergraduate and Graduate classes. Many of these methods will have the same implementations. As far as possible, you want to arrange for classes to inherit common methods and to avoid repeated code. Choice C is slightly inferior to choice B because you are told that all students are either graduates or undergraduates. Having the Student class abstract guarantees that you won’t create an instance of a Student (who is neither a graduate nor an undergraduate). Choice E has a major design flaw: making Graduate an abstract class means that you can’t create any instances of Graduate objects. Disaster! If the keyword abstract is removed from choice E, it becomes a fine design, as good as that in choice B. Once Student has implemented all the common PersonalInformation methods, these are inherited by each of the subclasses.

26. (B) Segment III is wrong because you can’t construct an interface object. Segments I and II both work because the minThree method is expecting three parameters, each of which is an Orderable. Since Temperature implements Orderable, each of the Temperature objects is an Orderable and can be used as a parameter in this method. Note that the program assumes that the compareTo method is able to compare Temperature objects with different scales. This is an internal detail that would be dealt with in the compareTo method, and hidden from the client. When a class implements Orderable there is an assumption that the compareTo method will be implemented in a reasonable way.

27. (B) Classes that implement an interface must provide implementation code for all non-default (i.e., abstract) methods in the interface. Adding method2 to the SomeName interface means that all of those classes need to be rewritten with implementation code for method2. (This is not good—it violates the sacred principle of code reusability, and programmers relying on the interface will squeal.) Choices A, C, and D are all meaningless garbage. Choice E may be true if there is some other error in the new class. Otherwise, as long as the new class provides implementation code for both method1 and method2, the class will compile.
T H E  O b j e c t  C L A S S

The Universal Superclass

Think of Object as the superclass of the universe. Every class automatically extends Object, which means that Object is a direct or indirect superclass of every other class. In a class hierarchy tree, Object is at the top:

Methods in Object

There are many methods in Object, all of them inherited by every other class. Since Object is not an abstract class, all of its methods have implementations. The expectation is that these methods will be overridden in any class where the default implementation is not suitable. The methods of Object in the AP Java subset are toString and equals.
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THE toString METHOD
public String toString()
This method returns a version of your object in String form.
When you attempt to print an object, the inherited default toString method is
invoked, and what you will see is the class name followed by an @ followed by a meaningless number (the address in memory of the object). For example,
SavingsAccount s = new SavingsAccount(500);
System.out.println(s);

produces something like
SavingsAccount@fea485c4

To have more meaningful output, you need to override the toString method for
your own classes. Even if your final program doesn’t need to output any objects, you
should define a toString method for each class to help in debugging.
Example 1
public class OrderedPair
{
private double x;
private double y;
//constructors and other methods ...
/** @return this OrderedPair in String form */
public String toString()
{
return "(" + x + "," + y + ")";
}
}

Now the statements
OrderedPair p = new OrderedPair(7,10);
System.out.println(p);

will invoke the overridden toString method and produce output that looks like an
ordered pair:
(7,10)
Example 2

For a BankAccount class the overridden toString method may look something like
this:
/** @return this BankAccount in String form */
public String toString()
{
return "Bank Account: balance = $" + balance;
}

The statements

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BankAccount b = new BankAccount(600);
System.out.println(b);

will produce output that looks like this:

Bank Account: balance = $600

NOTE

1. The + sign is a concatenation operator for strings (see p. 178).
2. Array objects are unusual in that they do not have a toString method. To print the elements of an array, the array must be traversed and each element must explicitly be printed.

THE equals METHOD

```java
public boolean equals(Object other)
```

All classes inherit this method from the Object class. It returns true if this object and other are the same object, false otherwise. Being the same object means referencing the same memory slot. For example,

```java
Date d1 = new Date("January", 14, 2001);
Date d2 = d1;
Date d3 = new Date("January", 14, 2001);
```

The test if (d1.equals(d2)) returns true, but the test if (d1==d3) returns false, since d1 and d3 do not refer to the same object. Often, as in this example, you may want two objects to be considered equal if their contents are the same. In that case, you have to override the equals method in your class to achieve this. Some of the standard classes described later in this chapter have overridden equals in this way. You will not be required to write code that overrides equals on the AP exam.

NOTE

1. The default implementation of equals is equivalent to the == relation for objects: In the Date example above, the test if (d1 == d2) returns true; the test if (d1 == d3) returns false.
2. The operators <, >, and so on, are not overloaded in Java. To compare objects, one must use either the equals method or define a compareTo method for the class.

Optional topic

THE hashCode METHOD

Every class inherits the hashCode method from Object. The value returned by hashCode is an integer produced by some formula that maps your object to an address in a hash table. A given object must always produce the same hash code. Also, two objects that are equal should produce the same hash code; that is, if obj1.equals(obj2) is true, then obj1 and obj2 should have the same hash code. Note that the opposite is not necessarily true. Hash codes do not have to be unique—two objects with the same hash code are not necessarily equal.

To maintain the condition that obj1.equals(obj2) is true implies that obj1 and obj2 have the same hash code, overriding equals means that you should override hashCode at the same time. You will not be required to do this on the AP exam.
You should, however, understand that every object is associated with an integer value called its hash code, and that objects that are equal have the same hash code.

THE String CLASS

String Objects
An object of type String is a sequence of characters. All string literals, such as "yikes!", are implemented as instances of this class. A string literal consists of zero or more characters, including escape sequences, surrounded by double quotes. (The quotes are not part of the String object.) Thus, each of the following is a valid string literal:

```
"" //empty string
"2468"
"I must\n go home"
```

String objects are immutable, which means that there are no methods to change them after they've been constructed. You can, however, always create a new String that is a mutated form of an existing String.

Constructing String Objects
A String object is unusual in that it can be initialized like a primitive type:

```java
String s = "abc";
```

This is equivalent to

```java
String s = new String("abc");
```

in the sense that in both cases `s` is a reference to a String object with contents "abc" (see Box on p. 179).

It is possible to reassign a String reference:

```java
String s = "John";
s = "Harry";
```

This is equivalent to

```java
String s = new String("John");
s = new String("Harry");
```

Notice that this is consistent with the immutable feature of String objects. "John" has not been changed; he has merely been discarded! The fickle reference `s` now refers to a new String, "Harry". It is also OK to reassign `s` as follows:

```java
s = s + " Windsor";
```

`s` now refers to the object "Harry Windsor".

Here are other ways to initialize String objects:

```java
String s1 = null;       //s1 is a null reference
String s2 = new String(); //s2 is an empty character sequence

String state = "Alaska";
String dessert = "baked " + state; //dessert has value "baked Alaska"
```
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The Concatenation Operator

The dessert declaration above uses the concatenation operator, +, which operates on String objects. Given two String operands lhs and rhs, lhs + rhs produces a single String consisting of lhs followed by rhs. If either lhs or rhs is an object other than a String, the toString method of the object is invoked, and lhs and rhs are concatenated as before. If one of the operands is a String and the other is a primitive type, then the non-String operand method is invoked, and concatenation occurs as before. If neither lhs nor rhs is a String object, an error occurs. Here are some examples:

```java
int five = 5;
String state = "Hawaii-";
String tvShow = state + five + "-0";  //tvShow has value
               //"Hawaii-5-0"

int x = 3, y = 4;
String sum = x + y;   //error: can't assign int 7 to String
```

Suppose a Date class has a toString method that outputs dates that look like this: 2/17/1948.

```java
Date d1 = new Date(8, 2, 1947);
Date d2 = new Date(2, 17, 1948);
String s = "My birthday is " + d2; //s has value
               //"My birthday is 2/17/1948"

String s2 = d1 + d2;    //error: + not defined for objects
String s3 = d1.toString() + d2.toString(); //s3 has value
               //8/2/19472/17/1948
```

Comparison of String Objects

There are two ways to compare String objects:

1. Use the equals method that is inherited from the Object class and overridden
to do the correct thing:

   ```java
   if (string1.equals(string2)) ...
   ```

   This returns true if string1 and string2 are identical strings, false otherwise.

2. Use the compareTo method. The String class has a compareTo method:

   ```java
   int compareTo(String otherString)
   ```

   It compares strings in dictionary (lexicographical) order:

   - If string1.compareTo(string2) < 0, then string1 precedes string2 in
     the dictionary.
   - If string1.compareTo(string2) > 0, then string1 follows string2 in
     the dictionary.
   - If string1.compareTo(string2) == 0, then string1 and string2 are iden-
     tical. (This test is an alternative to string1.equals(string2).)

   Be aware that Java is case-sensitive. Thus, if s1 is "cat" and s2 is "Cat", s1.equals(s2)
   will return false.
Characters are compared according to their position in the ASCII chart. All you need to know is that all digits precede all capital letters, which precede all lowercase letters. Thus "5" comes before "R", which comes before "a". Two strings are compared as follows: Start at the left end of each string and do a character-by-character comparison until you reach the first character in which the strings differ, the kth character, say. If the kth character of s1 comes before the kth character of s2, then s1 will come before s2, and vice versa. If the strings have identical characters, except that s1 terminates before s2, then s1 comes before s2. Here are some examples:

```java
String s1 = "HOT", s2 = "HOTEL", s3 = "dog";
if (s1.compareTo(s2) < 0)) //true, s1 terminates first
...
if (s1.compareTo(s3) > 0)) //false, "H" comes before "d"
```

Don't Use == to Test Strings!

The expression if(string1 == string2) tests whether string1 and string2 are the same reference. It does not test the actual strings. Using == to compare strings may lead to unexpected results.

**Example 1**

```java
String s = "oh no!";
String t = "oh no!";
if (s == t) ... 
```

The test returns true even though it appears that s and t are different references. The reason is that for efficiency Java makes only one String object for equivalent string literals. This is safe in that a String cannot be altered.

**Example 2**

```java
String s = "oh no!";
String t = new String("oh no!");
if (s == t) ... 
```

The test returns false because use of new creates a new object, and s and t are different references in this example!

The moral of the story? Use equals not == to test strings. It always does the right thing.

**Other String Methods**

The Java String class provides many methods, only a small number of which are in the AP Java subset. In addition to the constructors, comparison methods, and concatenation operator + discussed so far, you should know the following methods:
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```java
int length()
```

Returns the length of this string.

```java
String substring(int startIndex)
```

Returns a new string that is a substring of this string. The substring starts with the character at `startIndex` and extends to the end of the string. The first character is at index zero. The method throws an `IndexOutOfBoundsException` if `startIndex` is negative or larger than the length of the string. Note that if you're using Java 7 or above, you will see the error `StringIndexOutOfBoundsException`. However, the APstartIndex if `startIndex` is negative, or `endIndex` is larger than the length of the string, or `startIndex` is larger than `endIndex`.

```java
int indexOf(String str)
```

Returns the index of the first occurrence of `str` within this string. If `str` is not a substring of this string, -1 is returned. The method throws a `NullPointerException` if `str` is null.

Here are some examples:

```
"unhappy".substring(2)       //returns "happy"
"cold".substring(4)          //returns "" (empty string)
"cold".substring(6)          //StringIndexOutOfBoundsException
"strawberry".substring(5,7)  //returns "be"
"crayfish".substring(4,8)    //returns "fish"
"crayfish".substring(4,9)    //StringIndexOutOfBoundsException
"crayfish".substring(5,4)    //StringIndexOutOfBoundsException
```

```java
String s = "funnyfarm";
int x = s.indexOf("farm"); //x has value 5
x = s.indexOf("farmer");   //x has value -1
int y = s.length();        //y has value 9
```

**WRAPPER CLASSES**

A *wrapper class* takes either an existing object or a value of primitive type, “wraps” or “boxes” it in an object, and provides a new set of methods for that type. The point of a wrapper class is to provide extended capabilities for the boxed quantity:

- It can be used in generic Java methods that require objects as parameters.
- It can be used in Java container classes that require the items be objects (see p. 242).
In each case, the wrapper class allows

1. Construction of an object from a single value (wrapping or boxing the primitive in a wrapper object).
2. Retrieval of the primitive value (unwrapping or unboxing from the wrapper object).

Java provides a wrapper class for each of its primitive types. The two that you should know for the AP exam are the `Integer` and `Double` classes.

The Integer Class

The `Integer` class wraps a value of type `int` in an object. An object of type `Integer` contains just one instance variable whose type is `int`.

Here are the `Integer` methods you should know for the AP exam:

```java
Integer(int value)
```

Constructs an `Integer` object from an int. (Boxing.)

```java
int compareTo(Integer other)
```

Returns 0 if the value of this `Integer` is equal to the value of `other`, a negative integer if it is less than the value of `other`, and a positive integer if it is greater than the value of `other`.

```java
int intValue()
```

Returns the value of this `Integer` as an int. (Unboxing.)

```java
boolean equals(Object obj)
```

Returns true if and only if this `Integer` has the same `int` value as `obj`.

NOTE

1. This method overrides `equals` in class `Object`.
2. This method throws a `ClassCastException` if `obj` is not an `Integer`.

```java
String toString()
```

Returns a String representing the value of this `Integer`.

Here are some examples to illustrate the `Integer` methods:

```java
Integer intObj = new Integer(6); // boxes 6 in Integer object
int j = intObj.intValue(); // unboxes 6 from Integer object
System.out.println("Integer value is "+ intObj); // calls toString() for intObj
// output is
// Integer value is 6
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Object object = new Integer(5);  //Integer is a subclass of Object

Integer intObj2 = new Integer(3);
int k = intObj2.intValue();
if (intObj.equals(intObj2))  //OK, evaluates to false
...
if (intObj.intValue() == intObj2.intValue())
...  //OK, since comparing primitive types

if (k.equals(j))  //error, k and j not objects
...
if ((intObj.intValue()).compareTo(intObj2.intValue()) < 0)
...  //error, can't use compareTo on primitive types

if (intObj.compareTo(object) < 0)  //Error. Parameter needs Integer cast
if (intObj.compareTo((Integer) object) < 0)  //OK
...
if (object.compareTo(intObj) < 0)  //error, no compareTo in Object
...
if (((Integer) object).compareTo(intObj) < 0)  //OK
...

The Double Class

The Double class wraps a value of type double in an object. An object of type Double contains just one instance variable whose type is double.

The methods you should know for the AP exam are analogous to those for type Integer.

**Double(double value)**
Constructs a Double object from a double. (Boxing.)

**double doubleValue()**
Returns the value of this Double as a double. (Unboxing.)

**int compareTo(Double other)**
Returns 0 if the value of this Double is equal to the value of other, a negative integer if it is less than the value of other, and a positive integer if it is greater than the value of other.

**boolean equals(Object obj)**
This method overrides equals in class Object and throws a ClassCastException if obj is not a Double. Otherwise it returns true if and only if this Double has the same double value as obj.

**String toString()**
Returns a String representing the value of this Double.
Here are some examples:

```java
Double dObj = new Double(2.5);  //boxes 2.5 in Double object
double d = dObj.doubleValue();  //unboxes 2.5 from Double object

Object object = new Double(7.3);  //Double is a subclass of Object
Object intObj = new Integer(4);
if (dObj.compareTo(object) > 0)  //Error. Parameter needs cast to Double
  if (dObj.compareTo((Double) object) > 0)  //OK
    ...  
  if (dObj.compareTo(intObj) > 0)  //ClassCastException
    ...
  //can't compare Integer to Double
```

**NOTE**

1. Integer and Double objects are immutable: There are no mutator methods in the classes.
2. See p. 242 for a discussion of auto-boxing and -unboxing. This useful feature will *not* be tested on the AP exam.

---

**THE Math CLASS**

This class implements standard mathematical functions such as absolute value, square root, trigonometric functions, the log function, the power function, and so on. It also contains mathematical constants such as π and e.

Here are the functions you should know for the AP exam:

```java
static int abs(int x)
```

Returns the absolute value of integer x.

```java
static double abs(double x)
```

Returns the absolute value of real number x.

```java
static double pow(double base, double exp)
```

Returns base<sup>exp</sup>. Assumes base > 0, or base = 0 and exp > 0, or base < 0 and exp is an integer.

```java
static double sqrt(double x)
```

Returns √x, x ≥ 0.

```java
static double random()
```

Returns a random number r, where 0.0 ≤ r < 1.0. (See the next section, Random Numbers.)

All of the functions and constants are implemented as static methods and variables, which means that there are no instances of `Math` objects. The methods are invoked using the class name, `Math`, followed by the dot operator.
Chapter 4  Some Standard Classes

Here are some examples of mathematical formulas and the equivalent Java statements.

1. The relationship between the radius and area of a circle:

   \[ r = \sqrt{\frac{A}{\pi}} \]

   In code:
   ```java
   radius = Math.sqrt(area / Math.PI);
   ```

2. The amount of money \( A \) in an account after ten years, given an original deposit of \( P \) and an interest rate of 5% compounded annually, is

   \[ A = P(1.05)^{10} \]

   In code:
   ```java
   a = p * Math.pow(1.05, 10);
   ```

3. The distance \( D \) between two points \( P(x_P, y) \) and \( Q(x_Q, y) \) on the same horizontal line is

   \[ D = |x_P - x_Q| \]

   In code:
   ```java
   d = Math.abs(xp - xq);
   ```

**NOTE**

The static import construct allows you to use the static members of a class without the class name prefix. For example, the statement

```java
import static java.lang.Math.*;
```

allows use of all \( \text{Math} \) methods and constants without the \( \text{Math} \) prefix. Thus, the statement in formula 1 above could be written

```java
radius = sqrt(area / PI);
```

Static imports are not part of the AP subset.

**Random Numbers**

**RANDOM REALS**

The statement

```java
double r = Math.random();
```

produces a random real number in the range 0.0 to 1.0, where 0.0 is included and 1.0 is not.

This range can be scaled and shifted. On the AP exam you will be expected to write algebraic expressions involving \( \text{Math.random()} \) that represent linear transformations of the original interval \( 0.0 \leq x < 1.0 \).
Example 1
Produce a random real value \( x \) in the range \( 0.0 \leq x < 6.0 \).
\[
\text{double } x = 6 * \text{Math.random();}
\]

Example 2
Produce a random real value \( x \) in the range \( 2.0 \leq x < 3.0 \).
\[
\text{double } x = \text{Math.random()} + 2;
\]

Example 3
Produce a random real value \( x \) in the range \( 4.0 \leq x < 6.0 \).
\[
\text{double } x = 2 * \text{Math.random()} + 4;
\]

In general, to produce a random real value in the range \( \text{lowValue} \leq x < \text{highValue} \):
\[
\text{double } x = (\text{highValue} - \text{lowValue}) * \text{Math.random()} + \text{lowValue};
\]

RANDOM INTEGERS
Using a cast to \text{int}, a scaling factor, and a shifting value, \text{Math.random()} can be used to produce random integers in any range.

Example 1
Produce a random integer, from 0 to 99.
\[
\text{int } \text{num} = (\text{int}) (\text{Math.random()} * 100);
\]

In general, the expression
\[
(\text{int}) (\text{Math.random()} * k)
\]
produces a random \text{int} in the range \( 0,1,\ldots,k-1 \), where \( k \) is called the scaling factor. Note that the cast to \text{int} truncates the real number \text{Math.random()} * \( k \).

Example 2
Produce a random integer, from 1 to 100.
\[
\text{int } \text{num} = (\text{int}) (\text{Math.random()} * 100) + 1;
\]

In general, if \( k \) is a scaling factor, and \( p \) is a shifting value, the statement
\[
\text{int } \text{n} = (\text{int}) (\text{Math.random()} * k) + p;
\]
produces a random integer \( n \) in the range \( p, p+1,\ldots,p+(k-1) \).

Example 3
Produce a random integer from 5 to 24.
\[
\text{int } \text{num} = (\text{int}) (\text{Math.random()} * 20) + 5;
\]

Note that there are 20 possible integers from 5 to 24, inclusive.

NOTE
There is further discussion of strings and random numbers, plus additional questions, in Chapter 9 (The AP Computer Science Labs).
Chapter 4  Some Standard Classes

Chapter Summary

All students should know about overriding the equals and toString methods of the Object class and should be familiar with the Integer and Double wrapper classes.

Know the AP subset methods of the Math class, especially the use of Math.random() for generating random integers. Know the String methods substring and indexOf like the back of your hand, including knowing where exceptions are thrown in the String methods.
MULTIPLE-CHOICE QUESTIONS ON STANDARD CLASSES

1. Here is a program segment to find the quantity $base^{exp}$. Both base and exp are entered at the keyboard.

```java
System.out.println("Enter base and exponent: ");
double base = IO.readDouble(); // read user input
double exp = IO.readDouble(); // read user input
/* code to find power, which equals $base^{exp}$ */
System.out.print(base + " raised to the power " + exp);
System.out.println(" equals " + power);
```

Which is a correct replacement for
/* code to find power, which equals $base^{exp}$ */?

I double power;
    Math m = new Math();
    power = m.pow(base, exp);

II double power;
    power = Math.pow(base, exp);

III int power;
    power = Math.pow(base, exp);

(A) I only 
(B) II only 
(C) III only 
(D) I and II only 
(E) I and III only
Chapter 4  Some Standard Classes

2. Consider the squareRoot method defined below:

```java
/** @param d a real number such that d >= 0  *
 * Postcondition: Returns a Double whose value is the square
 * root of the value represented by d.  */
public Double squareRoot(Double d)
{
   /* implementation code */
}
```

Which /* implementation code */ satisfies the postcondition?

I. `double x = d.doubleValue();
   x = Math.sqrt(x);
   return new Double(x);`

II. `return new Double(Math.sqrt(d.doubleValue()));`

III. `return (Double) Math.sqrt(d.doubleValue());`

(A) I only  
(B) I and II only  
(C) I and III only  
(D) II and III only  
(E) I, II, and III

3. Here are some examples of negative numbers rounded to the nearest integer.

<table>
<thead>
<tr>
<th>Negative real number</th>
<th>Rounded to nearest integer</th>
</tr>
</thead>
<tbody>
<tr>
<td>-3.5</td>
<td>-4</td>
</tr>
<tr>
<td>-8.97</td>
<td>-9</td>
</tr>
<tr>
<td>-5.0</td>
<td>-5</td>
</tr>
<tr>
<td>-2.487</td>
<td>-2</td>
</tr>
<tr>
<td>-0.2</td>
<td>0</td>
</tr>
</tbody>
</table>

Refer to the declaration

double d = -4.67;

Which of the following correctly rounds d to the nearest integer?

(A) int rounded = Math.abs(d);
(B) int rounded = (int) (Math.random() * d);
(C) int rounded = (int) (d - 0.5);
(D) int rounded = (int) (d + 0.5);
(E) int rounded = Math.abs((int) (d - 0.5));
Multiple-Choice Questions on Standard Classes

4. A program is to simulate plant life under harsh conditions. In the program, plants die randomly according to some probability. Here is part of a `Plant` class defined in the program.

```java
public class Plant {
    /** probability that plant dies, a real number between 0 and 1 */
    private double probDeath;

    public Plant(double plantProbDeath, <other parameters>)
    {
        probDeath = plantProbDeath;
        <initialization of other instance variables >
    }

    /** Plant lives or dies. */
    public void liveOrDie()
    {
        /* statement to generate random number */
        if (/* test to determine if plant dies */)
            <code to implement plant's death >
        else
            <code to make plant continue living >
    }

    //Other variables and methods are not shown.
}
```

Which of the following are correct replacements for
(1) /* statement to generate random number */ and
(2) /* test to determine if plant dies */?

(A) (1) double x = Math.random();
    (2) x == probDeath

(B) (1) double x = (int) (Math.random());
    (2) x > probDeath

(C) (1) double x = Math.random();
    (2) x < probDeath

(D) (1) int x = (int) (Math.random() * 100);
    (2) x < (int) probDeath

(E) (1) int x = (int) (Math.random() * 100) + 1;
    (2) x == (int) probDeath

5. A program simulates fifty slips of paper, numbered 1 through 50, placed in a bowl for a raffle drawing. Which of the following statements stores in `winner` a random integer from 1 to 50?

(A) int winner = (int) (Math.random() * 50) + 1;

(B) int winner = (int) (Math.random() * 50);

(C) int winner = (int) (Math.random() * 51);

(D) int winner = (int) (Math.random() * 51) + 1;

(E) int winner = (int) (1 + Math.random() * 49);
6. Consider the code segment

```java
Integer i = new Integer(20);
/* more code */
```

Which of the following replacements for /* more code */ correctly sets `i` to have an integer value of 25?

I  `i = new Integer(25);`

II `i.intValue() = 25;`

III `Integer j = new Integer(25);
    i = j;`

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) II and III only

7. Consider these declarations:

```java
Integer intOb = new Integer(3);
Object ob = new Integer(4);
Double doubOb = new Double(3.0);
```

Which of the following will not cause an error?

(A) if ((Integer) ob.compareTo(intOb) < 0) ...
(B) if (ob.compareTo(intOb) < 0) ...
(C) if (intOb.compareTo(doubOb) < 0) ...
(D) if (intOb.compareTo(ob) < 0) ...
(E) if (intOb.compareTo((Integer) ob) < 0) ...

8. Refer to these declarations:

```java
Integer k = new Integer(8);
Integer m = new Integer(4);
```

Which test will not generate an error?

I  `if (k.intValue() == m.intValue())...`

II `if ((k.intValue()).equals(m.intValue()))...`

III `if ((k.toString()).equals(m.toString()))...`

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III
9. Consider the code fragment

```java
Object intObj = new Integer(9);
System.out.println((String) intObj);
```

What will be output as a result of running the fragment?
(A) No output. A ClassCastException will be thrown.
(B) No output. An ArithmeticException will be thrown.
(C) 9
(D) "9"
(E) nine

10. Consider these declarations:

```java
String s1 = "crab";
String s2 = new String("crab");
String s3 = s1;
```

Which expression involving these strings evaluates to true?
(I) s1 == s2
(II) s1.equals(s2)
(III) s3.equals(s2)
(A) I only
(B) II only
(C) II and III only
(D) I and II only
(E) I, II, and III

11. Suppose that strA = "TOMATO", strB = "tomato", and strC = "tom". Given that "A" comes before "a" in dictionary order, which is true?
(A) strA.compareTo(strB) < 0 && strB.compareTo(strC) < 0
(B) strB.compareTo(strA) < 0 || strC.compareTo(strA) < 0
(C) strC.compareTo(strA) < 0 && strA.compareTo(strB) < 0
(D) !(strA.equals(strB)) && strC.compareTo(strB) < 0
(E) !(strA.equals(strB)) && strC.compareTo(strA) < 0

12. This question refers to the following declaration:

```java
String line = "Some more silly stuff on strings!";
//the words are separated by a single space
```

What string will str refer to after execution of the following?
```java
int x = line.indexOf("m");
String str = line.substring(10, 10 + x) + line.substring(25, 25 + x);
```

(A) "sillyst"
(B) "sillystr"
(C) "silly st"
(D) "silly str"
(E) "sillystrin"
13. A program has a String variable `fullName` that stores a first name, followed by a space, followed by a last name. There are no spaces in either the first or last names. Here are some examples of `fullName` values: "Anthony Coppola", "Jimmy Carroll", and "Tom DeWire". Consider this code segment that extracts the last name from a `fullName` variable, and stores it in `lastName` with no surrounding blanks:

```
int k = fullName.indexOf(" "); //find index of blank
String lastName = /* expression */
```

Which is a correct replacement for /* expression */?

I  fullName.substring(k);
II  fullName.substring(k + 1);
III  fullName.substring(k + 1, fullName.length());

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I and III only

14. One of the rules for converting English to Pig Latin states: If a word begins with a consonant, move the consonant to the end of the word and add "ay". Thus "dog" becomes "ogday," and "crisp" becomes "rispcay". Suppose `s` is a String containing an English word that begins with a consonant. Which of the following creates the correct corresponding word in Pig Latin? Assume the declarations

```
String ayString = "ay";
String pigString;
```

(A) pigString = s.substring(0, s.length()) + s.substring(0,1) + ayString;
(B) pigString = s.substring(1, s.length()) + s.substring(0,0) + ayString;
(C) pigString = s.substring(0, s.length()-1) + s.substring(0,1) + ayString;
(D) pigString = s.substring(1, s.length()-1) + s.substring(0,0) + ayString;
(E) pigString = s.substring(1, s.length()) + s.substring(0,1) + ayString;
15. This question refers to the `getString` method shown below:

```java
public static String getString(String s1, String s2) {
    int index = s1.indexOf(s2);
    return s1.substring(index, index + s2.length());
}
```

Which is true about `getString`? It may return a string that

I Is equal to `s2`.
II Has no characters in common with `s2`.
III Is equal to `s1`.

(A) I and III only  
(B) II and III only  
(C) I and II only  
(D) I, II, and III  
(E) None is true.

16. Consider this method:

```java
public static String doSomething(String s) {
    final String BLANK = " "; //BLANK contains a single space
    String str = " "; //empty string
    String temp;
    for (int i = 0; i < s.length(); i++) {
        temp = s.substring(i, i + 1);
        if (!(temp.equals(BLANK)))
            str += temp;
    }
    return str;
}
```

Which of the following is the most precise description of what `doSomething` does?

(A) It returns `s` unchanged.  
(B) It returns `s` with all its blanks removed.  
(C) It returns a `String` that is equivalent to `s` with all its blanks removed.  
(D) It returns a `String` that is an exact copy of `s`.  
(E) It returns a `String` that contains `s.length()` blanks.
Chapter 4 Some Standard Classes

Questions 17 and 18 refer to the classes Position and PositionTest below.

```java
public class Position {
    /** row and col are both >= 0 except in the default 
     * constructor where they are initialized to -1. */
    private int row, col;

    public Position() //constructor
    {
        row = -1;
        col = -1;
    }

    public Position(int r, int c) //constructor
    {
        row = r;
        col = c;
    }

    /** @return row of Position */
    public int getRow()
    { return row; }

    /** @return column of Position */
    public int getCol()
    { return col; }

    /** @return Position north of (up from) this position */
    public Position north()
    { return new Position(row - 1, col); }

    //Similar methods south, east, and west
    ...

    /** Compares this Position to another Position object. 
     * @param p a Position object 
     * @return -1 (less than), 0 (equals), or 1 (greater than) 
     */
    public int compareTo(Position p)
    {
        if (this.getRow() < p.getRow() || this.getRow() == p.getRow()
            && this.getCol() < p.getCol())
            return -1;
        if (this.getRow() > p.getRow() || this.getRow() == p.getRow()
            && this.getCol() > p.getCol())
            return 1;
        return 0; //row and col both equal
    }

    /** @return string form of Position */
    public String toString()
    { return "(" + row + "," + col + ")"; }
}
```
Multiple-Choice Questions on Standard Classes  195

public class PositionTest
{
    public static void main(String[] args)
    {
        Position p1 = new Position(2, 3);
        Position p2 = new Position(4, 1);
        Position p3 = new Position(2, 3);

        //tests to compare positions
        ...
    }
}

17. Which is true about the value of p1.compareTo(p2)?
   (A) It equals true.
   (B) It equals false.
   (C) It equals 0.
   (D) It equals 1.
   (E) It equals -1.

18. Which boolean expression about p1 and p3 is true?
   I  p1 == p3
   II p1.equals(p3)
   III p1.compareTo(p3) == 0
   (A) I only
   (B) II only
   (C) III only
   (D) II and III only
   (E) I, II, and III
Chapter 4 Some Standard Classes

Questions 19 and 20 deal with the problem of swapping two integer values. Three methods are proposed to solve the problem, using primitive int types, Integer objects, and IntPair objects, where IntPair is defined as follows:

```java
public class IntPair {
    private int firstValue;
    private int secondValue;

    public IntPair(int first, int second) {
        firstValue = first;
        secondValue = second;
    }

    public int getFirst() { return firstValue; }
    public int getSecond() { return secondValue; }
    public void setFirst(int a) { firstValue = a; }
    public void setSecond(int b) { secondValue = b; }
}
```

19. Here are three different swap methods, each intended for use in a client program.

I public static void swap(int a, int b) {
    int temp = a;
    a = b;
    b = temp;
}

II public static void swap(Integer obj_a, Integer obj_b) {
    Integer temp = new Integer(obj_a.intValue());
    obj_a = obj_b;
    obj_b = temp;
}

III public static void swap(IntPair pair) {
    int temp = pair.getFirst();
    pair.setFirst(pair.getSecond());
    pair.setSecond(temp);
}

When correctly used in a client program with appropriate parameters, which method will swap two integers, as intended?

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III
20. Consider the following program that uses the `IntPair` class:

```java
public class TestSwap {
    public static void swap(IntPair pair) {
        int temp = pair.getFirst();
        pair.setFirst(pair.getSecond());
        pair.setSecond(temp);
    }

    public static void main(String[] args) {
        int x = 8, y = 6;
        /* code to swap x and y */
    }
}
```

Which is a correct replacement for `/* code to swap x and y */`?

I IntPair iPair = new IntPair(x, y);
    swap(x, y);
    x = iPair.getFirst();
    y = iPair.getSecond();

II IntPair iPair = new IntPair(x, y);
    swap(iPair);
    x = iPair.getFirst();
    y = iPair.getSecond();

III IntPair iPair = new IntPair(x, y);
    swap(iPair);
    x = iPair.setFirst();
    y = iPair.setSecond();

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) None is correct.
Chapter 4  Some Standard Classes

Refer to the Name class below for Questions 21 and 22.

```java
public class Name {
    private String firstName;
    private String lastName;

    public Name(String first, String last) // constructor
    {
        firstName = first;
        lastName = last;
    }

    public String toString()
    {
        return firstName + " " + lastName;
    }

    public boolean equals(Object obj)
    {
        Name n = (Name) obj;
        return n.firstName.equals(firstName) &&
               n.lastName.equals(lastName);
    }

    public int hashCode()
    {
        /* implementation not shown */
    }

    public int compareTo(Name n)
    {
        /* more code */
    }
}
```
21. The `compareTo` method implements the standard name-ordering algorithm where last names take precedence over first names. Lexicographic or dictionary ordering of `String` objects is used. For example, the name Scott Dentes comes before Nick Elser, and Adam Cooper comes before Sara Cooper.

Which of the following is a correct replacement for /* more code */?

I  
```
int lastComp = lastName.compareTo(n.lastName);
if (lastComp != 0)
    return lastComp;
else
    return firstName.compareTo(n.firstName);
```

II  
```
if (lastName.equals(n.lastName))
    return firstName.compareTo(n.firstName);
else
    return 0;
```

III  
```
if (!(lastName.equals(n.lastName)))
    return firstName.compareTo(n.firstName);
else
    return lastName.compareTo(n.lastName);
```

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) I, II, and III

22. Which statement about the `Name` class is false?

(A) `Name` objects are immutable.  
(B) It is possible for the methods in `Name` to throw a `NullPointerException`.  
(C) If `n1` and `n2` are `Name` objects in a client class, then the expressions `n1.equals(n2)` and `n1.compareTo(n2) == 0` must have the same value.  
(D) The `compareTo` method throws a run-time exception if the parameter is null.  
(E) Since the `Name` class has a `compareTo` method, it must provide an implementation for an `equals` method.
ANSWER KEY

7. E  15. A  

ANSWERS EXPLAINED

1. (B) All the Math class methods are static methods, which means you can’t use a Math object that calls the method. The method is invoked using the class name, Math, followed by the dot operator. Thus segment II is correct, and segment I is incorrect. Segment III will cause an error: Since the parameters of pow are of type double, the result should be stored in a double.

2. (B) The Math.sqrt method must be invoked on a primitive type double, which is the reason d.doubleValue() is used. (Note that auto-unboxing would apply if you failed to use d.doubleValue(), and used just d instead.) A correct segment must create a Double object using new, which eliminates segment III.

3. (C) The value –4.67 must be rounded to –5. Subtracting 0.5 gives a value of –5.17. Casting to int truncates the number (chops off the decimal part) and leaves a value of –5. None of the other choices produces –5. Choice A gives the absolute value of d: 4.67. Choice B is an incorrect use of Random. The parameter for nextInt should be an integer n, n ≥ 2. The method then returns a random int k, where 0 ≤ k < n. Choice D is the way to round a positive real number to the nearest integer. In the actual case it produces –4. Choice E gives the absolute value of –5, namely 5.

4. (C) The statement double x = Math.random(); generates a random double in the range 0 ≤ x < 1. Suppose probDeath is 0.67, or 67%. Assuming that random doubles are uniformly distributed in the interval, one can expect that 67% of the time x will be in the range 0 ≤ x < 0.67. You can therefore simulate the probability of death by testing if x is between 0 and 0.67, that is, if x < 0.67. Thus, x < probDeath is the desired condition for plant death, eliminating choices A and B. Choices D and E fail because (int) probDeath truncates probDeath to 0. The test x < 0 will always be false, and the test x == 0 will only be true if the random number generator returned exactly 0, an extremely unlikely occurrence! Neither of these choices correctly simulates the probability of death.

5. (A) The expression

    (int) (Math.random() * 50);


returns an int from 0 to 49. Therefore, adding 1 shifts the range to be 1 to 50, which was required.

6. (D) The Integer class has no methods that can change the contents of i. However, i can be reassigned so that it refers to another object. This happens in both segments I and III. Segment II is wrong because intValue is an accessor—it cannot be used to change the value of object i.

7. (E) Choice D fails because you can’t compare an Integer to an Object. You need to cast ob to Integer, as is done in choice E, the correct answer. Choice D will give the error message

```java
compareTo(java.lang.Integer) in java.lang.Integer cannot be applied to (java.lang.Object)
```

Choice C will cause a ClassCastException since the calling and parameter objects are incompatible types. The compareTo method will try erroneously to cast its parameter to the type of the object calling the method. Choice A almost works: It fails because the dot operator has higher precedence than casting, which means that ob.compareTo is parsed before ob is cast to Integer, generating a message that the compareTo method is not in class Object. Choice A can be fixed with an extra pair of parentheses:

```java
if (((Integer) ob).compareTo(intOb) < 0) ...
```

Choice B causes the same error message as choice A: no compareTo method in class Object.

8. (D) Test I is correct because it’s OK to compare primitive types (in this case int values) using ==. Test III works because k.toString() and m.toString() are Strings, which should be compared with equals. Test II is wrong because you can’t invoke a method (in this case equals) on an int.

9. (A) An Integer cannot be cast to a String. Don’t confuse this with

```java
System.out.println(intObj.toString()); //outputs 9
```

Note that if the first line of the code fragment were

```java
Integer intObj = new Integer(9);
```

then the error would be detected at compile time.

10. (C) Here are the memory slots:

![Memory Slots Diagram](image)

Statements II and III are true because the contents of s1 and s2 are the same, and the contents of s3 and s2 are the same. Statement I is false because s1 and s2 are not the same reference. Note that the expression s1 == s3 would be true since s1 and s3 are the same reference.

11. (D) Note that "TOMATO" precedes both "tomato" and "tom", since "T" precedes "t". Also, "tom" precedes "tomato" since the length of "tom" is less than the length of "tomato". Therefore each of the following is true:
Chapter 4  Some Standard Classes

strA.compareTo(strB) < 0
strA.compareTo(strC) < 0
strC.compareTo(strB) < 0

So
Choice A is T and F which evaluates to F
Choice B is F or F which evaluates to F
Choice C is F and T which evaluates to F
Choice D is T and T which evaluates to T
Choice E is T and F which evaluates to F

12. (A) x contains the index of the first occurrence of "m" in line, namely 2. (Remember that "a" is at index 0.) The method call line.substring(10,15) returns "silly", the substring starting at index 10 and extending though index 14. The method call line.substring(25,27) returns "st" (don't include the character at index 27!). The concatenation operator, +, joins these.

13. (D) The first character of the last name starts at the first character after the space. Thus, startIndex for substring must be k+1. This eliminates expression I. Expression II takes all the characters from position k+1 to the end of the fullName string, which is correct. Expression III takes all the characters from position k+1 to position fullName.length()-1, which is also correct.

14. (E) Suppose s contains "cat". You want pigString = "at" + "c" + "ay". Now the string "at" is the substring of s starting at position 1 and ending at position s.length()-1. The correct substring call for this piece of the word is s.substring(1,s.length()), which eliminates choices A, C, and D. (Recall that the first parameter is the starting position, and the second parameter is one position past the last index of the substring.) The first letter of the word—"c" in the example—starts at position 0 and ends at position 0. The correct expression is s.substring(0,1), which eliminates choice B.

15. (A) Statement I is true whenever s2 occurs in s1. For example, if strings s1 = "catastrophe" and s2 = "cat", then getString returns "cat". Statement II will never happen. If s2 is not contained in s1, the indexOf call will return -1. Using a negative integer as the first parameter of substring will cause a StringIndexOutOfBoundsException. Statement III will be true whenever s1 equals s2.

16. (C) The String temp represents a single-character substring of s. The method examines each character in s and, if it is a nonblank, appends it to str, which is initially empty. Each assignment str += temp assigns a new reference to str. Thus, str ends up as a copy of s but without the blanks. A reference to the final str object is returned. Choice A is correct in that s is left unchanged, but it is not the best characterization of what the method does. Choice B is not precise because an object parameter is never modified: Changes, if any, are performed on a copy. Choices D and E are wrong because the method removes blanks.

17. (E) The compareTo method returns an int, so eliminate choices A and B. In the implementation of compareTo, the code segment that applies to the particular example is

if (this.getRow() < p.getRow()) || ... return -1;

Since 2 < 4, the value -1 is returned.
18. (C) Expression III is true: The `compareTo` method is implemented to return 0 if two `Position` objects have the same row and column. Expression I is false because `object1 == object2` returns true only if `object1` and `object2` are the same reference. Expression II is tricky. One would like `p1` and `p3` to be equal since they have the same row and column values. This is not going to happen automatically, however. The `equals` method must explicitly be overridden for the `Position` class. If this hasn’t been done, the default `equals` method, which is inherited from class `Object`, will return true only if `p1` and `p3` are the same reference, which is not true.

19. (C) Recall that primitive types and object references are passed by value. This means that copies are made of the actual arguments. Any changes that are made are made to the copies. The actual parameters remain unchanged. Thus, in methods I and II, the parameters will retain their original values and remain unswapped.

To illustrate, for example, why method II fails, consider this piece of code that tests it:

```java
public static void main(String[] args) {
    int x = 8, y = 6;
    Integer xObject = new Integer(x);
    Integer yObject = new Integer(y);
    swap(xObject, yObject);
    x = xObject.intValue(); //surprise! still has value 8
    y = yObject.intValue(); //surprise! still has value 6
    
    ...
}
```

Here are the memory slots before `swap` is called:

```
x     y     xObject
  8     6
```

Here they are when `swap` is invoked:

```
x     y     xObject
  8     6
```

```
yObject
  6
```

```
xObject
  8
```

```
Integer
  8
```

```
Integer
  6
```

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The reason method III works is that instead of the object references being changed, the object contents are changed. Thus, after exiting the method, the IntPair reference is as it was, but the first and second values have been interchanged. (See explanation to next question for diagrams of the memory slots.) In this question, IntPair is used as a wrapper class for a pair of integers whose values need to be swapped.

20. (B) The swap method has just a single IntPair parameter, which eliminates segment I. Segment III fails because setFirst and setSecond are used incorrectly. These are mutator methods that change an IntPair object. What is desired is to return the (newly swapped) first and second values of the pair: Accessor methods
getFirst and getSecond do the trick. To see why this swap method works, look at the memory slots.

Before the swap method is called:

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>iPair</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>6</td>
<td></td>
</tr>
</tbody>
</table>

Just after the swap method is called:

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>temp</th>
<th>iPair</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>6</td>
<td>8</td>
<td></td>
</tr>
</tbody>
</table>

Just before exiting the swap method:

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>temp</th>
<th>iPair</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>6</td>
<td>8</td>
<td></td>
</tr>
</tbody>
</table>

Just after exiting the swap method:

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>iPair</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>8</td>
<td></td>
</tr>
</tbody>
</table>

After the statements:

```java
x = iPair.getFirst();
y = iPair.getSecond();
```

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>iPair</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>8</td>
<td></td>
</tr>
</tbody>
</table>

Notice that x and y have been swapped!
21. (A) The first statement of segment I compares last names. If these are different, the method returns the int value lastComp, which is negative if lastName precedes n.lastName, positive otherwise. If last names are the same, the method returns the int result of comparing first names. Segments II and III use incorrect algorithms for comparing names. Segment II would be correct if the else part were

```
return lastName.compareTo(n.lastName);
```

Segment III would be correct if the two return statements were interchanged.

22. (E) It is wise to have an equals method that is compatible with the compareTo method, namely, n1.equals(n2) and n1.compareTo(n2)==0 have the same value if n1 and n2 are Name objects. However, nothing in the Java language mandates that if a class has a compareTo method, it must also have an equals method. Choice A is true. You know this because the Name class has no mutator methods. Thus, Name objects can never be changed. Choice B is true: If a Name is initialized with null references, each of the methods will throw a NullPointerException. Choice C is true: If n1.equals(n2) is true, then n1.compareTo(n2) == 0 is true, because both are conditions for equality of n1 and n2 and should therefore be consistent. Choice D is true: If the parameter is null, the compareTo method will throw a NullPointerException.
Program Design and Analysis

Weeks of coding can save you hours of planning.
—Anonymous

### Chapter Goals
- Program development, including design and testing
- Object-oriented program design
- Relationships between classes
- Program analysis
- Efficiency

Students of introductory computer science typically see themselves as programmers. They no sooner have a new programming project in their heads than they’re at the computer, typing madly to get some code up and running. (Is this you?)

To succeed as a programmer, however, you have to combine the practical skills of a software engineer with the analytical mindset of a computer scientist. A software engineer oversees the life cycle of software development: initiation of the project, analysis of the specification, and design of the program, as well as implementation, testing, and maintenance of the final product. A computer scientist (among other things!) analyzes the implementation, correctness, and efficiency of algorithms. All these topics are tested on the APCS exam.

### THE SOFTWARE DEVELOPMENT LIFE CYCLE

#### The Waterfall Model

The waterfall model of software development came about in the 1960s in order to bring structure and efficiency into the process of creating large programs.

Each step in the process flows into the next: The picture resembles a waterfall.
Program Specification

The specification is a written description of the project. Typically it is based on a customer’s requirements. The first step in writing a program is to analyze the specification, make sure you understand it, and clarify with the customer anything that is unclear.

Program Design

Even for a small-scale program a good design can save programming time and enhance the reliability of the final program. The design is a fairly detailed plan for solving the problem outlined in the specification. It should include all objects that will be used in the solution, the data structures that will implement them, plus a detailed list of the tasks to be performed by the program.

A good design provides a fairly detailed overall plan at a glance, without including the minutiae of Java code.

Program Implementation

Program implementation is the coding phase. Design and implementation are discussed in more detail on p. 210.

Testing and Debugging

TEST DATA

Not every possible input value can be tested, so a programmer should be diligent in selecting a representative set of test data. Typical values in each part of a domain of the program should be selected, as well as endpoint values and out-of-range values. If only positive input is required, your test data should include a negative value just to check that your program handles it appropriately.
Example

A program must be written to insert a value into its correct position in this sorted list:

\[
2 \hspace{1em} 5 \hspace{1em} 9
\]

Test data should include

- A value less than 2
- A value between 2 and 5
- A value between 5 and 9
- A value greater than 9
- 2, 5, and 9
- A negative value

TYPES OF ERRORS (BUGS)

- A \textit{compile-time error} occurs during compilation of the program. The compiler is unable to translate the program into bytecode and prints an appropriate error message. A \textit{syntax error} is a compile-time error caused by violating the rules of the programming language. Some examples are omitting semicolons or braces, using undeclared identifiers, using keywords inappropriately, having parameters that don't match in type and number, and invoking a method for an object whose class definition doesn't contain that method.

- A \textit{run-time error} occurs during execution of the program. The Java run-time environment throws an exception, which means that it stops execution and prints an error message. Typical causes of run-time errors include attempting to divide an integer by zero, using an array index that is out of bounds, attempting to open a file that cannot be found, and so on. An error that causes a program to run forever ("infinite loop") can also be regarded as a run-time error. (See also Errors and Exceptions, p. 74.)

- An \textit{intent or logic error} is one that fails to carry out the specification of the program. The program compiles and runs but does not do the job. These are sometimes the hardest types of errors to fix.

ROBUSTNESS

Always assume that any user of your program is not as smart as you are. You must therefore aim to write a \textit{robust} program, namely one that

- Won't give inaccurate answers for some input data.
- Won't crash if the input data are invalid.
- Won't allow execution to proceed if invalid data are entered.

Examples of bad input data include out-of-range numbers, characters instead of numerical data, and a response of "maybe" when "yes" or "no" was asked for.

Note that bad input data that invalidates a computation won't be detected by Java. Your program should include code that catches the error, allows the error to be fixed, and allows program execution to resume.
Program Maintenance

Program maintenance involves upgrading the code as circumstances change. New features may be added. New programmers may come on board. To make their task easier, the original program must have clear and precise documentation.

OBJECT-ORIENTED PROGRAM DESIGN

Object-oriented programming has been the dominant programming methodology since the mid 1990s. It uses an approach that blurs the lines of the waterfall model. Analysis of the problem, development of the design, and pieces of the implementation all overlap and influence one another.

Here are the steps in object-oriented design:

- Identify classes to be written.
- Identify behaviors (i.e., methods) for each class.
- Determine the relationships between classes.
- Write the interface (public method headers) for each class.
- Implement the methods.

Identifying Classes

Identify the objects in the program by picking out the nouns in the program specification. Ignore pronouns and nouns that refer to the user. Select those nouns that seem suitable as classes, the “big-picture” nouns that describe the major objects in the application. Some of the other nouns may end up as attributes of the classes.

Many applications have similar object types: a low-level basic component; a collection of low-level components; a controlling object that puts everything together; and a display object that could be a GUI (graphical user interface) but doesn’t have to be.

Example 1

Write a program that maintains an inventory of stock items for a small store.

Nouns to consider: inventory, item, store.

Basic Object: StockItem
Collection: Inventory (a list of StockItems)
Controller: Store (has an Inventory, uses a StoreDisplay)
Display: StoreDisplay (could be a GUI)

Example 2

Write a program that simulates a game of bingo. There should be at least two players, each of whom has a bingo card, and a caller who calls the numbers.

Nouns to consider: game, players, bingo card, caller.

Basic Objects: BingoCard, Caller
Collection: Players (each has a BingoCard)
Controller: GameMaster (sets up the Players and Caller)
Display: BingoDisplay (shows each player’s card and displays winners, etc.)
Example 3

Write a program that creates random bridge deals and displays them in a specified format. (The specification defines a “deal” as consisting of four hands. It also describes a deck of cards, and shows how each card should be displayed.)

Nouns to consider: deal, hand, format, deck, card.

Basic Object: Card
Collection: Deck (has an array of Cards)
Hand (has an array of Cards)
Deal (has an array of Hands)
Dealer (has a Deck, or several Decks)
Controller: Formatter (has a Deal and a TableDisplay)
Display: TableDisplay (could be a GUI)

Identifying Behaviors

Find all verbs in the program description that help lead to the solution of the programming task. These are likely behaviors that will probably become the methods of the classes. Now decide which methods belong in which classes. Recall that the process of bundling a group of methods and data fields into a class is called encapsulation.

Think carefully about who should do what. Do not ask a basic object to perform operations for the group. For example, a StockItem should keep track of its own details (price, description, how many on the shelf, etc.) but should not be required to search for another item. A Card should know its value and suit but should not be responsible for keeping track of how many cards are left in a deck. A Caller in a bingo game should be responsible for keeping track of the numbers called so far and for producing the next number but not for checking whether a player has bingo: That is the job of an individual player (element of Players) and his BingoCard.

You will also need to decide which data fields each class will need and which data structures should store them. For example, if an object represents a list of items, consider an array or ArrayList as the data structure.

Determining Relationships Between Classes

INHERITANCE RELATIONSHIPS

Look for classes with common behaviors. This will help identify inheritance relationships. Recall the is-a relationship—if object1 is-a object2, then object2 is a candidate for a superclass.

COMPOSITION RELATIONSHIPS

Composition relationships are defined by the has-a relationship. For example, a Nurse has-a Uniform. Typically, if two classes have a composition relationship, one of them contains an instance variable whose type is the other class.

Note that a wrapper class always implements a has-a relationship with any objects that it wraps.
Chapter 5  Program Design and Analysis

UML Diagrams

An excellent way to keep track of the relationships between classes and show the inheritance hierarchy in your programs is with a UML (Unified Modeling Language) diagram. This is a standard graphical scheme used by object-oriented programmers. Although it is not part of the AP subset, on the AP exam you may be expected to interpret simple UML diagrams and inheritance hierarchies.

Here is a simplified version of the UML rules:

- Represent classes with rectangles.
- Use angle brackets with the word “abstract” or “interface” to indicate either an abstract class or interface.
- Show the is-a relationship between classes with an open up-arrow.
- Show the is-a relationship that involves an interface with an open, dotted up-arrow.
- Show the has-a relationship with a down arrow or sideways arrow (indicates composition).

Example

From this diagram you can see at a glance that GoodPlayer and BadPlayer are subclasses of an abstract class Player, and that each Player implements the Rankable interface. Every Player has a Board and a ScoreCard, while only the BadPlayer has a Tutor.

Implementing Classes

BOTTOM-UP DEVELOPMENT

For each method in a class, list all of the other classes needed to implement that particular method. These classes are called collaborators. A class that has no collaborators is independent.

To implement the classes, often an incremental, bottom-up approach is used. This means that independent classes are fully implemented and tested before being incorporated into the overall project. Typically, these are the basic objects of the program, like StockItem, Card, and BingoCard. Unrelated classes in a programming project can be implemented by different programmers.
Object-Oriented Program Design 213

Note that a class can be tested using a dummy Tester class that will be discarded when the methods of the class are working. Constructors, then methods, should be added, and tested, one at a time. A driver class that contains a main method can be used to test the program as you go. The purpose of the driver is to test the class fully before incorporating it as an object in a new class.

When each of the independent classes is working, classes that depend on just one other class are implemented and tested, and so on. This may lead to a working, bare bones version of the project. New features and enhancements can be added later.

Design flaws can be corrected at each stage of development. Remember, a design is never set in stone: It simply guides the implementation.

TOP-DOWN DEVELOPMENT

In a top-down design, the programmer starts with an overview of the program, selecting the highest-level controlling object and the tasks needed. During development of the program, subsidiary classes may be added to simplify existing classes.

Implementing Methods

PROCEDURAL ABSTRACTION

A good programmer avoids chunks of repeated code wherever possible. To this end, if several methods in a class require the same task, like a search or a swap, you should use helper methods. The reduce method in the Rational class on p. 118 is an example of such a method. Also, wherever possible you should enhance the readability of your code by using helper methods to break long methods into smaller tasks. The use of helper methods within a class is known as procedural abstraction and is an example of top-down development within a class. This process of breaking a long method into a sequence of smaller tasks is sometimes called stepwise refinement.

INFORMATION HIDING

Instance variables and helper methods are generally declared as private, which prevents client classes from accessing them. This strategy is called information hiding.

STUB METHOD

Sometimes it makes more sense in the development of a class to test a calling method before testing a method it invokes. A stub is a dummy method that stands in for a method until the actual method has been written and tested. A stub typically has an output statement to show that it was called in the correct place, or it may return some reasonable values if necessary.

ALGORITHM

An algorithm is a precise step-by-step procedure that solves a problem or achieves a goal. Don’t write any code for an algorithm in a method until the steps are completely clear to you.

Example 1

A program must test the validity of a four-digit code number that a person will enter to be able to use a photocopy machine. The number is valid if the fourth digit equals the remainder when the sum of the first three digits is divided by seven.
Classes in the program may include an IDNumber, the four-digit code; Display, which would handle input and output; and IDMain, the driver for the program. The data structure used to implement an IDNumber could be an instance variable of type int, or an instance variable of type String, or four instance variables of type int—one per digit, and so on.

A top-down design for the program that tests the validity of the number is reflected in the steps of the main method of IDMain:

Create Display
Read in IDNumber
Check validity
Print message

Each method in this design is tested before the next method is added to main. If the display will be handled in a GUI (graphical user interface), stepwise refinement of the design might look like this:

Create Display
   Construct a Display
   Create window panels
   Set up text fields
   Add panels and fields to window

Read in IDNumber
   Prompt and read

Check validity of IDNumber
   Check input
      Check characters
      Check range
   Separate into digits
   Check validity property

Print message
   Write number
   State if valid

NOTE

1. The IDNumber class, which contains the four-digit code, is responsible for the following operations:
   Split value into separate digits
   Check condition for validity

The Display class, which contains objects to read and display, must also contain an IDNumber object. It is responsible for the following operations:
   Set up display
   Read in code number
   Display validity message

Creating these two classes with their data fields (instance variables) and operations (methods) is an example of encapsulation.
2. The `Display` method `readCodeNumber` needs private helper methods to check the input: `checkCharacters` and `checkRange`. This is an example of procedural abstraction (use of helper methods) and information hiding (making them private).

3. Initially the programmer had just an `IDNumber` class and a driver class. The `Display` class was added as a refinement, when it was realized that handling the input and message display was separate from checking the validity of the `IDNumber`. This is an example of top-down development (adding an auxiliary class to clarify the code).

4. The `IDNumber` class contains no data fields that are objects. It is therefore an independent class. The `Display` class, which contains an `IDNumber` data member, has a composition relationship with `IDNumber` (`Display has a IDNumber`).

5. When testing the final program, the programmer should be sure to include each of the following as a user-entered code number: a valid four-digit number, an invalid four-digit number, an $n$-digit number, where $n \neq 4$, and a “number” that contains a nondigit character. A robust program should be able to deal with all these cases.

**Example 2**

A program must create a teacher’s grade book. The program should maintain a class list of students for any number of classes in the teacher’s schedule. A menu should be provided that allows the teacher to

- Create a new class of students.
- Enter a set of scores for any class.
- Correct any data that’s been entered.
- Display the record of any student.
- Calculate the final average and grade for all students in a class.
- Print a class list, with or without grades.
- Add a student, delete a student, or transfer a student to another class.
- Save all the data in a file.

**IDENTIFYING CLASSES**

Use the nouns in the specification as a starting point for identifying classes in the program. The nouns are: program, teacher, grade book, class list, class, student, schedule, menu, set of scores, data, record, average, grade, and file.

Eliminate each of the following:

- `program` (Always eliminate “program” when used in this context.)
- `teacher` (Eliminate, because he or she is the user.)
- `schedule` (This will be reflected in the name of the external file for each class, e.g., `apcs_period3.dat`.)
- `data, record` (These are synonymous with student name, scores, grades, etc., and will be covered by these features.)
- `class` (This is synonymous with class list.)
The following seem to be excellent candidates for classes: GradeBook, ClassList, Student, and FileHandler. Other possibilities are Menu, ScoreList, and a GUI_Display.

On further thought: Basic independent objects are Student, Menu, Score, and FileHandler. Group objects are ClassList (collection of students), ScoreList (collection of scores), and AllClasses (collection of ClassLists). The controlling class is the GradeBook. A Display class is essential for many of the grade book operations, like showing a class list or displaying information for a single student.

RELATIONSHIPS BETWEEN CLASSES

There are no inheritance relationships. There are many composition relationships between objects, however. The GradeBook has-a Menu, the ClassList has-a Student (several, in fact!), a Student has-a name, average, grade, list_of_scores, etc. The programmer must decide whether to code these attributes as classes or data fields.

IDENTIFYING BEHAVIORS

Use the verbs in the specification to identify required operations in the program. The verbs are: maintain <list>, provide <menu>, allow <user>, create <list>, enter <scores>, correct <data>, display <record>, calculate <average>, calculate <grade>, print <list>, add <student>, delete <student>, transfer <student>, and save <data>.

You must make some design decisions about which class is responsible for which behavior. For example, will a ClassList display the record of a single Student, or will a Student display his or her own record? Who will enter scores—the GradeBook, a ClassList, or a Student? Is it desirable for a Student to enter scores of other Students? Probably not!

DECISIONS

Here are some preliminary decisions. The GradeBook will provideMenu. The menu selection will send execution to the relevant object.

The ClassList will maintain an updated list of each class. It will have these public methods: addStudent, deleteStudent, transferStudent, createNewClass, printClassList, printScores, and updateList. A good candidate for a helper method in this class is search for a given student.

Each Student will have complete personal and grade information. Public methods will include setName, getName, enterScore, correctData, findAverage, getAverage, getGrade, and displayRecord.

Saving and retrieving information is crucial to this program. The FileHandler will take care of openFileForReading, openFileForWriting, closeFile, loadClass, and saveClass. The FileHandler class should be written and tested right at the beginning, using a small dummy class list.

Score, ScoreList, and Student are easy classes to implement. When these are working, the programmer can go on to ClassList. Finally the Display GUI class, which will have the GradeBook, can be developed. This is an example of bottom-up development.

Example 3

A program simulates a game of Battleships, which is a game between two players,
each of whom has a grid where ships are placed. Each player has five ships:

```
battleship o o o o o
  cruiser    o o o o
  submarine  o o o
  destroyer  o o
  frigate    o
```

The grids of the players’ fleets may look like this. Any two adjacent squares that are taken must belong to the same ship, i.e., different ships shouldn’t “touch.”

```
  0 1 2 3 4 5 6 7
 0
 1 o o o o o
 2
 3 o
 4 o o
 5 o
 6 o o
 7 o
```

Player 1

```
  0 1 2 3 4 5 6 7
 0 o o o o
 1 o
 2
 3 o
 4 o o
 5
 6 o o o
 7
```

Player 2

Each player’s grid is hidden from the other player. Players alternate “shooting” at each other’s ships by calling out a position, a row and column number. A player must make an honest response, “hit” or “miss.” If it’s a hit, a player gets another turn. If the whole ship has been hit, the owner must say something like, “You sank my cruiser.” Each player must keep track of hits and misses. The first player to sink his opponent’s fleet is the winner.

IDENTIFYING CLASSES

The nouns in the specification are program, game, players, grid, ship, battleship, cruiser, submarine, destroyer, frigate, square, position, opponent, row, column, turn, hits, misses, fleet, winner.

Eliminate each of the following:

- program Always eliminate.
- row, col These are parts of a given position or square, more suitable as instance variables for a position or square object.
- hits, misses These are simply marked positions and probably don’t need their own class.
- turn Taking a turn is an action and will be described by a method rather than a class.
- opponent This is another word for player.

The following seem to be good candidates for classes: Player, Grid, Position, Ship, Battleship, Cruiser, Submarine, Destroyer, and Frigate. Additionally, it seems there should be a GameManager and Display.
RELATIONSHIP BETWEEN CLASSES

This program provides two examples of inheritance relationships. Each of the five ships is a Ship, and shares common features, like isHit, isSunk, and array of positions. However, each has a unique name, length, and position in the grid. This means that Ship is a good candidate for an abstract class with abstract methods like getLength, getName, and getPositions, which depend on the kind of ship.

The second inheritance relationship is between the grids. There are two types of grids for each player: his own FleetGrid (the current state of his own ships) and his opponent's HitGrid, which keeps track of his hits and misses. Each of these grids is a Grid. A grid is a candidate for an interface, with a list of methods like getAdjacentNeighbors, getRightNeighbor, etc. Each of FleetGrid and HitGrid would implement Grid.

There are several composition relationships in this program. A Player has a HitGrid and a FleetGrid and also has five ships. The GameManager has each of the two Player objects and also has a Display. The Display has each of the grids.

IDENTIFYING BEHAVIORS

Use the verbs to identify key methods in the program: simulate <game>, place <ships>, shoot <at position>, call out <position>, respond <hit or miss>, sink <ship>, inform that <ship was sunk>, keep track of <hits or misses>, sink <opponent's fleet>, win <game>.

You need to decide who will do what. There's no definitive way of implementing the program, but it seems clear that the GameManager should run the game and declare the winner. Should the GameManager also be in charge of announcing if a ship is sunk? It makes sense because the game manager can see both players' grids. Each player should keep track of his calls, so that he can make an intelligent next call and also respond "hit" or "miss." Will each player have a display? Or will the Display have both players? You have to set it up so that a player can't see his opponent's FleetGrid, but he can see his own and also a grid showing the state of the calls he has made. Should each player have a list of his ships, so he can keep track of the state of his fleet? And what about each ship in the fleet? Should a ship have a list of its positions, and should it keep track of if it's hit or sunk?

Saving and retrieving updated information is crucial to this program. It seems a bit overwhelming. Where should you start? The Ship classes are low-level classes, independent of the players and grids. Start with these and test that you can get accurate information about each ship. In your driver program create an ArrayList<Ship>. Have a loop that prints information about each ship. Polymorphism will take care of getting the correct information about each ship.

Now try the Grid classes. This is a complicated program where each small piece should be coded and tested with simple output. For example, a Grid can be displayed with a two-dimensional array of 0's and 1's to show the positions of ships. Other symbols can be used to show what's been hit and what's been sunk.

When everything is working with the grids, you could add a Display class that has Grid variables and a display method.

Try a Player. Give him a list of ships, two grids and a Display.

Then create a GameManager. Give her two Player variables and be sure she has a playGame method.

The program development shown above is an example of bottom-up development.
Vocabulary Summary

Know these terms for the AP exam:

<table>
<thead>
<tr>
<th>Vocabulary</th>
<th>Meaning</th>
</tr>
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<tbody>
<tr>
<td>software development</td>
<td>Writing a program</td>
</tr>
<tr>
<td>object-oriented program</td>
<td>Uses interacting objects</td>
</tr>
<tr>
<td>program specification</td>
<td>Description of a task</td>
</tr>
<tr>
<td>program design</td>
<td>A written plan, an overview of the solution</td>
</tr>
<tr>
<td>program implementation</td>
<td>The code</td>
</tr>
<tr>
<td>test data</td>
<td>Input to test the program</td>
</tr>
<tr>
<td>program maintenance</td>
<td>Keeping the program working and up to date</td>
</tr>
<tr>
<td>top-down development</td>
<td>Implement main classes first, subsidiary classes later</td>
</tr>
<tr>
<td>independent class</td>
<td>Doesn’t use other classes of the program in its code</td>
</tr>
<tr>
<td>bottom-up development</td>
<td>Implement lowest level, independent classes first</td>
</tr>
<tr>
<td>driver class</td>
<td>Used to test other classes; contains main method</td>
</tr>
<tr>
<td>inheritance relationship</td>
<td>is-a relationship between classes</td>
</tr>
<tr>
<td>composition relationship</td>
<td>has-a relationship between classes</td>
</tr>
<tr>
<td>inheritance hierarchy</td>
<td>Inheritance relationship shown in a tree-like diagram</td>
</tr>
<tr>
<td>UML diagram</td>
<td>Tree-like representation of relationship between classes</td>
</tr>
<tr>
<td>data structure</td>
<td>Java construct for storing a data field (e.g., array)</td>
</tr>
<tr>
<td>encapsulation</td>
<td>Combining data fields and methods in a class</td>
</tr>
<tr>
<td>information hiding</td>
<td>Using private to restrict access</td>
</tr>
<tr>
<td>stepwise refinement</td>
<td>Breaking methods into smaller methods</td>
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<tr>
<td>procedural abstraction</td>
<td>Using helper methods</td>
</tr>
<tr>
<td>algorithm</td>
<td>Step-by-step process that solves a problem</td>
</tr>
<tr>
<td>stub method</td>
<td>Dummy method called by another method being tested</td>
</tr>
<tr>
<td>debugging</td>
<td>Fixing errors</td>
</tr>
<tr>
<td>robust program</td>
<td>Screens out bad input</td>
</tr>
<tr>
<td>compile-time error</td>
<td>Usually a syntax error; prevents program from compiling</td>
</tr>
<tr>
<td>syntax error</td>
<td>Bad language usage (e.g., missing brace)</td>
</tr>
<tr>
<td>run-time error</td>
<td>Occurs during execution (e.g., int division by 0)</td>
</tr>
<tr>
<td>exception</td>
<td>Run-time error thrown by Java method</td>
</tr>
<tr>
<td>logic error</td>
<td>Program runs but does the wrong thing</td>
</tr>
</tbody>
</table>

PROGRAM ANALYSIS

Program Correctness

Testing that a program works does not prove that the program is correct. After all, you can hardly expect to test programs for every conceivable set of input data. Computer scientists have developed mathematical techniques to prove correctness in certain cases, but these are beyond the scope of the APCS course. Nevertheless, you are expected to be able to make assertions about the state of a program at various points during its execution.

Assertions

An assertion is a precise statement about a program at any given point. The idea is that if an assertion is proved to be true, then the program is working correctly at that point.
An informal step on the way to writing correct algorithms is to be able to make different kinds of assertions about your code.

**PRECONDITION**
The *precondition* for any piece of code, whether it is a method, loop, or block, is a statement of what is true immediately before execution of that code.

**POSTCONDITION**
The *postcondition* for a piece of code is a statement of what is true immediately after execution of that code.

**Efficiency**
An efficient algorithm is one that is economical in the use of

- CPU time. This refers to the number of machine operations required to carry out the algorithm (arithmetic operations, comparisons, data movements, etc.).
- Memory. This refers to the number and complexity of the variables used.

Some factors that affect run-time efficiency include unnecessary tests, excessive movement of data elements, and redundant computations, especially in loops.

Always aim for early detection of output conditions: Your sorting algorithm should halt when the list is sorted; your search should stop if the key element has been found.

In discussing efficiency of an algorithm, we refer to the *best case*, *worst case*, and *average case*. The best case is a configuration of the data that causes the algorithm to run in the least possible amount of time. The worst case is a configuration that leads to the greatest possible run time. Typical configurations (i.e., not specially chosen data) give the average case. It is possible that best, worst, and average cases don’t differ much in their run times.

For example, suppose that a list of distinct random numbers must be searched for a given key value. The algorithm used is a sequential search starting at the beginning of the list. In the best case, the key will be found in the first position examined. In the worst case, it will be in the last position or not in the list at all. On average, the key will be somewhere in the middle of the list.

---

**Chapter Summary**

There’s a lot of vocabulary that you are expected to know in this chapter. Learn the words!

Never make assumptions about a program specification, and always write a design before starting to write code. Even if you don’t do this for your own programs, these are the answers you will be expected to give on the AP exam. You are certain to get questions about program design. Know the procedures and terminology involved in developing an object-oriented program.

Be sure you understand what is meant by best case, worst case, and average case for an algorithm. There will be questions about efficiency on the AP exam.

By now you should know what a precondition and postcondition are.
MULTIPLE-CHOICE QUESTIONS ON PROGRAM DESIGN AND ANALYSIS

1. A program that reads in a five-digit identification number is to be written. The specification does not state whether zero can be entered as a first digit. The programmer should
   (A) write the code to accept zero as a first digit since zero is a valid digit.
   (B) write the code to reject zero as a first digit since five-digit integers do not start with zero.
   (C) eliminate zero as a possibility for any of the digits.
   (D) treat the identification number as a four-digit number if the user enters a number starting with zero.
   (E) check with the writer of the specification whether zero is acceptable as a first digit.

2. Refer to the following three program descriptions:
   
   I Test whether there exists at least one three-digit integer whose value equals the sum of the squares of its digits.
   II Read in a three-digit code number and check if it is valid according to some given formula.
   III Passwords consist of three digits and three capital letters in any order. Read in a password, and check if there are any repeated characters.

   For which of the preceding program descriptions would a ThreeDigitNumber class be suitable?
   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) I, II, and III

3. Top-down programming is illustrated by which of the following?
   (A) Writing a program from top to bottom in Java
   (B) Writing an essay describing how the program will work, without including any Java code
   (C) Using driver programs to test all methods in the order that they’re called in the program
   (D) Writing and testing the lowest level methods first and then combining them to form appropriate abstract operations
   (E) Writing the program in terms of the operations to be performed and then refining these operations by adding more detail
4. Which of the following should influence your choice of a particular algorithm?

   I  The run time of the algorithm
   II The memory requirements of the algorithm
   III The ease with which the logic of the algorithm can be understood

   (A) I only
   (B) III only
   (C) I and III only
   (D) I and II only
   (E) I, II, and III

5. A list of numbers is stored in a sorted array. It is required that the list be maintained in sorted order. This requirement leads to inefficient execution for which of the following processes?

   I Summing the five smallest numbers in the list
   II Finding the maximum value in the list
   III Inserting and deleting numbers

   (A) I only
   (B) III only
   (C) II and III only
   (D) I and III only
   (E) I, II, and III

6. Which of the following is not necessarily a feature of a robust program?

   (A) Does not allow execution to proceed with invalid data
   (B) Uses algorithms that give correct answers for extreme data values
   (C) Will run on any computer without modification
   (D) Will not allow division by zero
   (E) Will anticipate the types of errors that users of the program may make

7. A certain freight company charges its customers for shipping overseas according to this scale:

   $80 per ton for a weight of 10 tons or less
   $40 per ton for each additional ton over 10 tons but not exceeding 25 tons
   $30 per ton for each additional ton over 25 tons

   For example, to ship a weight of 12 tons will cost 10(80) + 2(40) = $880. To ship 26 tons will cost 10(80) + 15(40) + 1(30) = $1430.

   A method takes as parameter an integer that represents a valid shipping weight and outputs the charge for the shipment. Which of the following is the smallest set of input values for shipping weights that will adequately test this method?

   (A) 10, 25
   (B) 5, 15, 30
   (C) 5, 10, 15, 25, 30
   (D) 0, 5, 10, 15, 25, 30
   (E) 5, 10, 15, 20, 25, 30
8. A code segment calculates the mean of values stored in integers \( n_1, n_2, n_3, \) and \( n_4 \) and stores the result in \( \text{average} \), which is of type \text{double}. What kind of error is caused with this statement?

\[
\text{double average} = n_1 + n_2 + n_3 + n_4 / (\text{double}) 4;
\]

(A) Logic  
(B) Run-time  
(C) Overflow  
(D) Syntax  
(E) Type mismatch

9. A program evaluates binary arithmetic expressions that are read from an input file. All of the operands are integers, and the only operators are \( +, -, *, \) and \( / \). In writing the program, the programmer forgot to include a test that checks whether the right-hand operand in a division expression equals zero. When will this oversight be detected by the computer?

(A) At compile time  
(B) While editing the program  
(C) As soon as the data from the input file is read  
(D) During evaluation of the expressions  
(E) When at least one incorrect value for the expressions is output

10. Which best describes the precondition of a method? It is an assertion that

(A) describes precisely the conditions that must be true at the time the method is called.  
(B) initializes the parameters of the method.  
(C) describes the effect of the method on its postcondition.  
(D) explains what the method does.  
(E) states what the initial values of the local variables in the method must be.
11. Consider the following code fragment:

```c
/*** Precondition: a1, a2, a3 contain 3 distinct integers.
* Postcondition: max contains the largest of a1, a2, a3. */
//first set max equal to larger of a1 and a2
if (a1 > a2)
    max = a1;
else
    max = a2;
//set max equal to larger of max and a3
if (max < a3)
    max = a3;
```

For this algorithm, which of the following initial setups for \(a1\), \(a2\), and \(a3\) will cause

1. the least number of computer operations (best case) and
2. the greatest number of computer operations (worst case)?

(A) (1) largest value in \(a1\) or \(a2\)  (2) largest value in \(a3\)
(B) (1) largest value in \(a2\) or \(a3\)  (2) largest value in \(a1\)
(C) (1) smallest value in \(a1\)  (2) largest value in \(a2\)
(D) (1) largest value in \(a2\)  (2) smallest value in \(a3\)
(E) (1) smallest value in \(a1\) or \(a2\)  (2) largest value in \(a3\)

12. Refer to the following code segment.

```c
/*** Compute the mean of integers 1 .. N.
* N is an integer >= 1 and has been initialized. */
int k = 1;
double mean, sum = 1.0;
while (k < N) {
    /* loop body */
}
mean = sum / N;
```

What is the precondition for the while loop?

(A) \(k \geq N\), \(\text{sum} = 1.0\)
(B) \(\text{sum} = 1 + 2 + 3 + \ldots + k\)
(C) \(k < N\), \(\text{sum} = 1.0\)
(D) \(N \geq 1\), \(k = 1\), \(\text{sum} = 1.0\)
(E) \(\text{mean} = \text{sum} / N\)
13. The sequence of Fibonacci numbers is 1, 1, 2, 3, 5, 8, 13, 21, .... The first two Fibonacci numbers are each 1. Each subsequent number is obtained by adding the previous two. Consider this method:

```java
/**
 * Precondition: n >= 1.
 * Postcondition: The nth Fibonacci number has been returned.
 */
public static int fib(int n)
{
    int prev = 1, next = 1, sum = 1;
    for (int i = 3; i <= n; i++)
    {
        /* assertion */
        sum = next + prev;
        prev = next;
        next = sum;
    }
    return sum;
}
```

Which of the following is a correct /* assertion */ about the loop variable `i`?
(A) 1 \leq i \leq n
(B) 0 \leq i \leq n
(C) 3 \leq i \leq n
(D) 3 < i \leq n
(E) 3 < i < n+1

14. Refer to the following method.

```java
/**
 * Precondition: a and b are initialized integers.
 */
public static int mystery(int a, int b)
{
    int total = 0, count = 1;
    while (count <= b)
    {
        total += a;
        count++;
    }
    return total;
}
```

What is the postcondition for method `mystery`?
(A) total \equiv a + b
(B) total \equiv a^b
(C) total \equiv b^a
(D) total \equiv a \times b
(E) total \equiv a / b
15. A program is to be written that prints an invoice for a small store. A copy of the invoice will be given to the customer and will display
   • A list of items purchased.
   • The quantity, unit price, and total price for each item.
   • The amount due.

Three candidate classes for this program are Invoice, Item, and ItemList, where an Item is a single item purchased and ItemList is the list of all items purchased. Which class is a reasonable choice to be responsible for the amountDue method, which returns the amount the customer must pay?

I Item
II ItemList
III Invoice

(A) I only
(B) III only
(C) I and II only
(D) II and III only
(E) I, II, and III

16. Which is a false statement about classes in object-oriented program design?

(A) If a class C1 has an instance variable whose type is another class, C2, then C1 has-a C2.
(B) If a class C1 is associated with another class, C2, then C1 depends on C2 for its implementation.
(C) If classes C1 and C2 are related such that C1 is-a C2, then C2 has-a C1.
(D) If class C1 is independent, then none of its methods will have parameters that are objects of other classes.
(E) Classes that have common methods do not necessarily define an inheritance relationship.
17. A Java program maintains a large database of vehicles and parts for a car dealership. Some of the classes in the program are Vehicle, Car, Truck, Tire, Circle, SteeringWheel, and AirBag. The declarations below show the relationships between classes. Which is a poor choice?

(A) public class Vehicle
        {
            ...
            private Tire[] tires;
            private SteeringWheel sw;
            ...
        }

(B) public class Tire extends Circle
        {
            ...
            //inherits methods that compute circumference
            //and center point
        }

(C) public class Car extends Vehicle
        {
            ...
            //inherits private Tire[] tires from Vehicle class
            //inherits private SteeringWheel sw from Vehicle class
            ...
        }

(D) public class Tire
        {
            ...
            private String rating;  //speed rating of tire
            private Circle boundary;
        }

(E) public class SteeringWheel
        {
            ...
            private AirBag ab;  //AirBag is stored in SteeringWheel
            private Circle boundary;
        }

18. A Java programmer has completed a preliminary design for a large program. The programmer has developed a list of classes, determined the methods for each class, established the relationships between classes, and written an outline for each class. Which class(es) should be implemented first?

(A) Any superclasses
(B) Any subclasses
(C) All collaborator classes (classes that will be used to implement other classes)
(D) The class that represents the dominant object in the program
(E) All independent classes (classes that have no references to other classes)
Chapter 5  Program Design and Analysis

Use the program description below for Questions 19–21.

A program is to be written that simulates bumper cars in a video game. The cars move on a square grid and are located on grid points \((x, y)\), where \(x\) and \(y\) are integers between \(-20\) and \(20\). A bumper car moves in a random direction, either left, right, up, or down. If it reaches a boundary (i.e., \(x\) or \(y\) is \(\pm 20\)), then it reverses direction. If it is about to collide with another bumper car, it reverses direction. Your program should be able to add bumper cars and run the simulation. One step of the simulation allows each car in the grid to move. After a bumper car has reversed direction twice, its turn is over and the next car gets to move.

19. To identify classes in the program, the nouns in the specification are listed:

program, bumper car, grid, grid point, integer, direction, boundary, simulation

How many nouns in the list should immediately be discarded because they are unsuitable as classes for the program?

(A) 0
(B) 1
(C) 2
(D) 3
(E) 4
A programmer decides to include the following classes in the program. Refer to them for Questions 20 and 21.

- Simulation will run the simulation.
- Display will show the state of the game.
- BumperCar will know its identification number, position in the grid, and current direction when moving.
- GridPoint will be a position in the grid. It will be represented by two integer fields, x_coord and y Coord.
- Grid will keep track of all bumper cars in the game, the number of cars, and their positions in the grid. It will update the grid each time a car moves. It will be implemented with a two-dimensional array of BumperCar.

20. Which operation should not be the responsibility of the GridPoint class?

(A) isEmpty returns false if grid point contains a BumperCar, true otherwise
(B) atBoundary returns true if x or y coordinate = ±20, false otherwise
(C) left if not at left boundary, change grid point to 1 unit left of current point
(D) up if not at top of grid, change grid point to 1 unit above current point
(E) get_x return x-coordinate of this point

21. Which method is not suitable for the BumperCar class?

(A) public boolean atBoundary()
   //Returns true if BumperCar at boundary, false otherwise.
(B) public void selectRandomDirection()
   //Select random direction (up, down, left, or right)
   //at start of turn.
(C) public void reverseDirection()
   //Move to grid position that is in direction opposite to
   //current direction.
(D) public void move()
   //Take turn to move. Stop move after two changes
   //of direction.
(E) public void update()
   //Modify Grid to reflect new position after each stage
   //of move.
ANSWER KEY

1. E  8. A  15. D
3. E  10. A  17. B
6. C  13. C  20. A

ANSWERS EXPLAINED

1. (E) A programmer should never make unilateral decisions about a program specification. When in doubt, check with the person who wrote the specification.

2. (D) In I and II a three-digit number is the object being manipulated. For III, however, the object is a six-character string, which suggests a class other than a ThreeDigitNumber.

3. (E) Top-down programming consists of listing the methods for the main object and then using stepwise refinement to break each method into a list of subtasks. Eliminate choices A, C, and D: Top-down programming refers to the design and planning stage and does not involve any actual writing of code. Choice B is closer to the mark, but “top-down” implies a list of operations, not an essay describing the methods.

4. (E) All three considerations are valid when choosing an algorithm. III is especially important if your code will be part of a larger project created by several programmers. Yet even if you are the sole writer of a piece of software, be aware that your code may one day need to be modified by others.

5. (B) A process that causes excessive data movement is inefficient. Inserting an element into its correct (sorted) position involves moving elements to create a slot for this element. In the worst case, the new element must be inserted into the first slot, which involves moving every element up one slot. Similarly, deleting an element involves moving elements down a slot to close the “gap.” In the worst case, where the first element is deleted, all elements in the array will need to be moved. Summing the five smallest elements in the list means summing the first five elements. This requires no testing of elements and no excessive data movement, so it is efficient. Finding the maximum value in a sorted list is very fast—just select the element at the appropriate end of the list.

6. (C) “Robustness” implies the ability to handle all data input by the user and to give correct answers even for extreme values of data. A program that is not robust may well run on another computer without modification, and a robust program may need modification before it can run on another computer.

7. (C) Eliminate choice D because 0 is an invalid weight, and you may infer from the method description that invalid data have already been screened out. Eliminate
choice E because it tests two values in the range 10–25. (This is not wrong, but choice C is better.) Eliminate choice A since it tests only the endpoint values. Eliminate B because it tests no endpoint values.

8. (A) The statement is syntactically correct, but as written it will not find the mean of the integers. The bug is therefore an intent or logic error. To execute as intended, the statement needs parentheses:

   double average = (n1 + n2 + n3 + n4) / (double) 4;

9. (D) The error that occurs is a run-time error caused by an attempt to divide by zero (ArithmeticException). Don’t be fooled by choice C. Simply reading an expression 8/0 from the input file won’t cause the error. Note that if the operands were of type double, the correct answer would be E. In this case, dividing by zero does not cause an exception; it gives an answer of Infinity. Only on inspecting the output would it be clear that something was wrong.

10. (A) A precondition does not concern itself with the action of the method, the local variables, the algorithm, or the postcondition. Nor does it initialize the parameters. It simply asserts what must be true directly before execution of the method.

11. (A) The best case causes the fewest computer operations, and the worst case leads to the maximum number of operations. In the given algorithm, the initial test if (a1 > a2) and the assignment to max will occur irrespective of which value is the largest. The second test, if (max < a3), will also always occur. The final statement, max = a3, will occur only if the largest value is in a3; thus, this represents the worst case. So the best case must have the biggest value in a1 or a2.

12. (D) The precondition is an assertion about the variables in the loop just before the loop is executed. Variables n, k, and std have all been initialized to the values shown in choice D. Choice C is wrong because k may equal n. Choice A is wrong because k may be less than n. Choice E is wrong because mean is not defined until the loop has been exited. Choice B is wrong because it omits the assertions about n and k.

13. (C) Eliminate choices A and B, since i is initialized to 3 in the for loop. Choices D and E are wrong because i is equal to 3 the first time through the loop.

14. (D) a is being added to total b times, which means that at the end of execution total = a*b.

15. (D) It makes sense for an Item to be responsible for its name, unit price, quantity, and total price. It is not reasonable for it to be responsible for other Items. Since an ItemList, however, will contain information for all the Items purchased, it is reasonable to have it also compute the total amountDue. It makes just as much sense to give an Invoice the responsibility for displaying information for the Items purchased, as well as providing a final total, amountDue.

16. (C) The is-a relationship defines inheritance, while the has-a relationship defines association. These types of relationship are mutually exclusive. For example, a graduate student is-a student. It doesn’t make sense to say a student has-a graduate student!

17. (B) Even though it’s convenient for a Tire object to inherit Circle methods, an inheritance relationship between a Tire and a Circle is incorrect: It is false to say...
that a Tire is a Circle. A Tire is a car part, while a Circle is a geometric shape. Notice that there is an association relationship between a Tire and a Circle: A Tire has a Circle as its boundary.

18. (E) Independent classes do not have relationships with other classes and can therefore be more easily coded and tested.

19. (C) The word “program” is never included when it’s used in this context. The word “integer” describes the type of coordinates $x$ and $y$ and has no further use in the specification. While words like “direction,” “boundary,” and “simulation” may later be removed from consideration as classes, it is not unreasonable to keep them as candidates while you ponder the design.

20. (A) A GridPoint object knows only its $x$ and $y$ coordinates. It has no information about whether a BumperCar is at that point. Notice that operations in all of the other choices depend on the $x$ and $y$ coordinates of a GridPoint object. An isEmpty method should be the responsibility of the Grid class that keeps track of the status of each position in the grid.

21. (E) A BumperCar is responsible for itself—keeping track of its own position, selecting an initial direction, making a move, and reversing direction. It is not, however, responsible for maintaining and updating the grid. That should be done by the Grid class.
Arrays and Array Lists

Chapter 6

Should array indices start at 0 or 1?
My compromise of 0.5 was rejected,
without, I thought, proper consideration.
—S. Kelly-Bootle

Chapter Goals

• One-dimensional arrays
• The ArrayList<E> class
• Two-dimensional arrays
• The List<E> interface

ONE-DIMENSIONAL ARRAYS

An array is a data structure used to implement a list object, where the elements in the list are of the same type; for example, a class list of 25 test scores, a membership list of 100 names, or a store inventory of 500 items.

For an array of \( N \) elements in Java, index values ("subscripts") go from \( 0 \) to \( N - 1 \). Individual elements are accessed as follows: If \( arr \) is the name of the array, the elements are \( arr[0], arr[1], \ldots, arr[N-1] \). If a negative subscript is used, or a subscript \( k \) where \( k \geq N \), an ArrayIndexOutOfBoundsException is thrown.

Initialization

In Java, an array is an object; therefore, the keyword \texttt{new} must be used in its creation. The size of an array remains fixed once it has been created. As with String objects, however, an array reference may be reassigned to a new array of a different size.

Example

All of the following are equivalent. Each creates an array of 25 double values and assigns the reference \texttt{data} to this array.

1. \texttt{double[]} \texttt{data} = \texttt{new double}[25];
2. \texttt{double data[]} = \texttt{new double}[25];
3. \texttt{double[]} \texttt{data;}
   \texttt{data} = \texttt{new double}[25];

A subsequent statement like
data = new double[40];

reassigns data to a new array of length 40. The memory allocated for the previous

data array is recycled by Java's automatic garbage collection system.

When arrays are declared, the elements are automatically initialized to zero for the

primitive numeric data types (int and double), to false for boolean variables, or to

null for object references.

It is possible to declare several arrays in a single statement. For example,

int[] intList1, intList2;  //declares intList1 and intList2 to
  //contain int values
int[] arr1 = new int[15], arr2 = new int[30];  //reserves 15 slots
  //for arr1, 30 for arr2

INITIALIZER LIST

Small arrays whose values are known can be declared with an initializer list. For exam-
ple, instead of writing

int[] coins = new int[4];
coins[0] = 1;
coins[1] = 5;
coins[2] = 10;
coins[3] = 25;

you can write

int[] coins = {1, 5, 10, 25};

This construction is the one case where new is not required to create an array.

Length of Array

A Java array has a final public instance variable (i.e., a constant), length, which can be

accessed when you need the number of elements in the array. For example,

String[] names = new String[25];
  < code to initialize names >

//loop to process all names in array
for (int i = 0; i < names.length; i++)
  < process names >

NOTE

1. The array subscripts go from 0 to names.length-1; therefore, the test on i in
   the for loop must be strictly less than names.length.
2. length is not a method and therefore is not followed by parentheses. Contrast
   this with String objects, where length is a method and must be followed by
   parentheses. For example,

   String s = "Confusing syntax!";
   int size = s.length();  //assigns 17 to size
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Traversing an Array

Use a for-each loop whenever you need access to every element in an array without replacing or removing any elements. Use a for loop in all other cases: to access the index of any element, to replace or remove elements, or to access just some of the elements.

Note that if you have an array of objects (not primitive types), you can use the for-each loop and mutator methods of the object to modify the fields of any instance (see the shuffleAll method on p. 239).

Example 1

```java
/** @return the number of even integers in array arr of integers */
public static int countEven(int[] arr)
{
    int count = 0;
    for (int num : arr)
        if ( num % 2 == 0)  //num is even
            count++;
    return count;
}
```

Example 2

```java
/** Change each even-indexed element in array arr to 0.
 * Precondition: arr contains integers.
 * Postcondition: arr[0], arr[2], arr[4], ... have value 0.
 */
public static void changeEven(int[] arr)
{
    for (int i = 0; i < arr.length; i += 2)
        arr[i] = 0;
}
```

Arrays as Parameters

Since arrays are treated as objects, passing an array as a parameter means passing its object reference. No copy is made of the array. Thus, the elements of the actual array can be accessed—and modified.

Example 1

Array elements accessed but not modified:

```java
/** @return index of smallest element in array arr of integers */
public static int findMin (int[] arr)
{
    int min = arr[0];
    int minIndex = 0;
    for (int i = 1; i < arr.length; i++)
        if (arr[i] < min)  //found a smaller element
            { 
                min = arr[i];
                minIndex = i;
            }
    return minIndex;
}
```

To call this method (in the same class that it’s defined):
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```java
int[] array;
<code to initialize array>
int min = findMin(array);
```

Example 2

Array elements modified:

```java
/** Add 3 to each element of array b. */
public static void changeArray(int[] b)
{
    for (int i = 0; i < b.length; i++)
        b[i] += 3;
}
```

To call this method (in the same class):

```java
int[] list = {1, 2, 3, 4};
changeArray(list);
System.out.print("The changed list is ");
for (int num : list)
    System.out.print(num + " ");
```

The output produced is

```
The changed list is 4 5 6 7
```

Look at the memory slots to see how this happens:

When an array is passed as a parameter, it is possible to alter the contents of the array.

<table>
<thead>
<tr>
<th>Before the method call</th>
<th>At the start of the method call</th>
</tr>
</thead>
<tbody>
<tr>
<td>list</td>
<td>list</td>
</tr>
<tr>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>1 2 3 4</td>
<td>1 2 3 4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Just before exiting the method</th>
<th>After exiting the method</th>
</tr>
</thead>
<tbody>
<tr>
<td>list</td>
<td>list</td>
</tr>
<tr>
<td>1 2 3 4</td>
<td>4 5 6 7</td>
</tr>
<tr>
<td>b</td>
<td></td>
</tr>
</tbody>
</table>

Example 3

Contrast the changeArray method with the following attempt to modify one array element:

```java
/** Add 3 to an element. */
public static void changeElement(int n)
{ n += 3; }
```

Here is some code that invokes this method:
int[] list = {1, 2, 3, 4};
System.out.print("Original array: ");
for (int num : list)
    System.out.print(num + " ");
changeElement(list[0]);
System.out.print("Modified array: ");
for (int num : list)
    System.out.print(num + " ");

Contrary to the programmer’s expectation, the output is
Original array: 1 2 3 4
Modified array: 1 2 3 4

A look at the memory slots shows why the list remains unchanged.

Before the method call:

<table>
<thead>
<tr>
<th>list</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
</table>

At the start of the method call:

<table>
<thead>
<tr>
<th>list</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>n</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Just before exiting the method:

<table>
<thead>
<tr>
<th>list</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>n</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

After exiting the method:

<table>
<thead>
<tr>
<th>list</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
</table>

The point of this is that primitive types—including single array elements of type int or double—are passed by value. A copy is made of the actual parameter, and the copy is erased on exiting the method.

Example 4

/** Swap arr[i] and arr[j] in array arr. */
public static void swap(int[] arr, int i, int j)
{
    int temp = arr[i];
    arr[i] = arr[j];
    arr[j] = temp;
}

To call the swap method:

int[] list = {1, 2, 3, 4};
swap(list, 0, 3);
System.out.print("The changed list is: ");
for (int num : list)
    System.out.print(num + " ");

The output shows that the program worked as intended:
The changed list is: 4 2 3 1
Example 5

```java
/** @return array containing NUM_ELEMENTS integers read from the keyboard */
* Precondition: Array undefined.
* Postcondition: Array contains NUM_ELEMENTS integers read from
* the keyboard.
*/
public int[] getIntegers()
{
    int[] arr = new int[NUM_ELEMENTS];
    for (int i = 0; i < arr.length; i++)
    {
        System.out.println("Enter integer: ");
        arr[i] = IO.readInt(); //read user input
    }
    return arr;
}
```

To call this method:

```java
int[] list = getIntegers();
```

Array Variables in a Class

Consider a simple `Deck` class in which a deck of cards is represented by the integers 0 to 51.

```java
public class Deck
{
    private int[] deck;
    public static final int NUMCARDS = 52;

    /** constructor */
    public Deck()
    {
        deck = new int[NUMCARDS];
        for (int i = 0; i < NUMCARDS; i++)
            deck[i] = i;
    }

    /** Write contents of Deck. */
    public void writeDeck()
    {
        for (int card : deck)
            System.out.print(card + " ");
        System.out.println();
        System.out.println();
    }

    /** Swap arr[i] and arr[j] in array arr. */
    private void swap(int[] arr, int i, int j)
    {
        int temp = arr[i];
        arr[i] = arr[j];
        arr[j] = temp;
    }
}
/** Shuffle Deck: Generate a random permutation by picking a
 * random card from those remaining and putting it in the
 * next slot, starting from the right. */
 public void shuffle()
 { int index;
   for (int i = NUMCARDS - 1; i > 0; i--)
   {
     // generate an int from 0 to i
     index = (int) (Math.random() * (i + 1));
     swap(deck, i, index);
   }
 }

Here is a simple driver class that tests the Deck class:

public class DeckMain
{
  public static void main(String args[])
  {
    Deck d = new Deck();
    d.shuffle();
    d.writeDeck();
  }
}

NOTE
There is no evidence of the array that holds the deck of cards—deck is a private instance
variable and is therefore invisible to clients of the Deck class.

Array of Class Objects

Suppose a large card tournament needs to keep track of many decks. The code to do
this could be implemented with an array of Deck:

public class ManyDecks
{
  private Deck[] allDecks;
  public static final int NUMDECKS = 500;

  /** constructor */
  public ManyDecks()
  {
    allDecks = new Deck[NUMDECKS];
    for (int i = 0; i < NUMDECKS; i++)
      allDecks[i] = new Deck();
  }

  /** Shuffle the Decks. */
  public void shuffleAll()
  {
    for (Deck d : allDecks)
      d.shuffle();
  }
}
Chapter 6  Arrays and Array Lists

/** Write contents of all the Decks. */
public void printDecks()
{
    for (Deck d : allDecks)
        d.writeDeck();
}

NOTE
1. The statement
   
   allDecks = new Deck[NUMDECKS];

   creates an array, allDecks, of 500 Deck objects. The default initialization for
   these Deck objects is null. In order to initialize them with actual decks, the
   Deck constructor must be called for each array element. This is achieved with
   the for loop of the ManyDecks constructor.

2. In the shuffleAll method, it’s OK to use a for-each loop to modify each deck
   in the array with the mutator method shuffle.

Analyzing Array Algorithms

Example 1
Discuss the efficiency of the countNegs method below. What are the best and worst
condition of the data?

/** Precondition: arr[0],...,arr[arr.length-1] contain integers.
* @return the number of negative values in arr
*/
public static int countNegs(int[] arr)
{
    int count = 0;
    for (int num : arr)
        if (num < 0)
            count++;
    return count;
}

Solution:
This algorithm sequentially examines each element in the array. In the best case, there
are no negative elements, and count++ is never executed. In the worst case, all the
elements are negative, and count++ is executed in each pass of the for loop.

Example 2
The code fragment below inserts a value, num, into its correct position in a sorted
array of integers. Discuss the efficiency of the algorithm.
Array Lists

Array Lists

An ArrayList provides an alternative way of storing a list of objects and has the following advantages over an array:

- An ArrayList shrinks and grows as needed in a program, whereas an array has a fixed length that is set when the array is created.
- In an ArrayList list, the last slot is always list.size()-1, whereas in a partially filled array, you, the programmer, must keep track of the last slot currently in use.
- For an ArrayList, you can do insertion or deletion with just a single statement. Any shifting of elements is handled automatically. In an array, however, insertion or deletion requires you to write the code that shifts the elements.

The Collections API

The ArrayList class is in the Collections API (Application Programming Interface), which is a library provided by Java. Most of the API is in java.util. This library gives the programmer access to prepackaged data structures and the methods to manipulate them. The implementations of these container classes are invisible and should not be of concern to the programmer. The code works. And it is reusable.

All of the collections classes, including ArrayList, have the following features in common:
They are designed to be both memory and run-time efficient.
They provide methods for insertion and removal of items (i.e., they can grow and shrink).
They provide for iteration over the entire collection.

The Collections Hierarchy

Inheritance is a defining feature of the Collections API. The interfaces that are used to manipulate the collections specify the operations that must be defined for any container class that implements that interface.

The diagram below shows that the ArrayList class implements the List interface.

Collections and Generics

The collections classes are generic, with type parameters. Thus, List<E> and ArrayList<E> contain elements of type E.

When a generic class is declared, the type parameter is replaced by an actual object type. For example,

```java
private ArrayList<Clown> clowns;
```

NOTE

1. The clowns list must contain only Clown objects. An attempt to add an Acrobat to the list, for example, will cause a compile-time error.
2. Since the type of objects in a generic class is restricted, the elements can be accessed without casting.
3. All of the type information in a program with generic classes is examined at compile time. After compilation the type information is erased. This feature of generic classes is known as erasure. During execution of the program, any attempt at incorrect casting will lead to a ClassCastException.

Auto-Boxing and -Unboxing

There are no primitive types in collections classes. An ArrayList must contain objects, not types like double and int. Numbers must therefore be boxed—placed in wrapper classes like Integer and Double—before insertion into an ArrayList.

Auto-boxing is the automatic wrapping of primitive types in their wrapper classes.

To retrieve the numerical value of an Integer (or Double) stored in an ArrayList, the intValue() (or doubleValue()) method must be invoked (unwrapping). Auto-unboxing is the automatic conversion of a wrapper class to its corresponding primitive type. This means that you don’t need to explicitly call the intValue() or
doubleValue() methods. Be aware that if a program tries to auto-unbox `null`, the method will throw a `NullPointerException`.

Note that while auto-boxing and -unboxing cut down on code clutter, these operations must still be performed behind the scenes, leading to decreased run-time efficiency. It is much more efficient to assign and access primitive types in an array than an `ArrayList`. You should therefore consider using an array for a program that manipulates sequences of numbers and does not need to use objects.

**NOTE**

Auto-boxing and -unboxing is a feature in Java 5.0 and later versions and will not be tested on the AP exam. It is OK, however, to use this convenient feature in code that you write in the free-response questions.

---

**THE List<E> INTERFACE**

A class that implements the `List<E>` interface—`ArrayList<E>`, for example—is a list of elements of type `E`. In a list, duplicate elements are allowed. The elements of the list are indexed, with 0 being the index of the first element.

A list allows you to

- Access an element at any position in the list using its integer index.
- Insert an element anywhere in the list.
- Iterate over all elements using `ListIterator` or `Iterator` (not in the AP subset).

**The Methods of List<E>**

Here are the methods you should know.

```java
boolean add(E obj)
```

Appends `obj` to the end of the list. Always returns `true`. If the specified element is not of type `E`, throws a `ClassCastException`.

```java
int size()
```

Returns the number of elements in the list.

```java
E get(int index)
```

Returns the element at the specified `index` in the list.

```java
E set(int index, E element)
```

Replaces item at specified `index` in the list with specified `element`. Returns the element that was previously at `index`. Throws a `ClassCastException` if the specified element is not of type `E`. 
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```java
void add(int index, E element)
```

Inserts element at specified index. Elements from position index and higher have 1 added to their indices. Size of list is incremented by 1.

```java
E remove(int index)
```

Removes and returns the element at the specified index. Elements to the right of position index have 1 subtracted from their indices. Size of list is decreased by 1.

```java
Optional topic
Iterator<E> iterator()
```

Returns an iterator over the elements in the list, in proper sequence, starting at the first element.

**The ArrayList<E> Class**

This is an array implementation of the List<E> interface. The main difference between an array and an ArrayList is that an ArrayList is resizable during run time, whereas an array has a fixed size at construction.

Shifting of elements, if any, caused by insertion or deletion, is handled automatically by ArrayList. Operations to insert or delete at the end of the list are very efficient. Be aware, however, that at some point there will be a resizing; but, on average, over time, an insertion at the end of the list is a single, quick operation. In general, insertion or deletion in the middle of an ArrayList requires elements to be shifted to accommodate a new element (add), or to close a “hole” (remove).

**THE METHODS OF ArrayList<E>**

In addition to the two add methods, and size, get, set, and remove, you must know the following constructor.

```java
ArrayList()
```

Constructs an empty list.

**NOTE**

Each method above that has an index parameter—add, get, remove, and set—throws an IndexOutOfBoundsException if index is out of range. For get, remove, and set, index is out of range if

\[ index < 0 \text{ || } index > \text{size()} \]

For add, however, it is OK to add an element at the end of the list. Therefore index is out of range if

\[ index < 0 \text{ || } index > \text{size()} \]
Using ArrayList<E>

Example 1

//Create an ArrayList containing 0 1 4 9.
List<Integer> list = new ArrayList<Integer>(); //An ArrayList is-a List
for (int i = 0; i < 4; i++)
    list.add(i * i); //example of auto-boxing
    //i*i wrapped in an Integer before insertion
Integer intOb = list.get(2); //assigns Integer with value 4 to intOb.
    //Leaves list unchanged.
int n = list.get(3); //example of auto-unboxing
    //Integer is retrieved and converted to int
    //n contains 9
Integer x = list.set(3, 5); //list is 0 1 4 5
    //x contains Integer with value 9
x = list.remove(2); //list is 0 1 5
    //x contains Integer with value 9
list.add(1, 7); //list is 0 7 1 5
list.add(2, 8); //list is 0 7 8 1 5

Example 2

//Traversing an ArrayList of Integer.
//Print the elements of list, one per line.
for (Integer num : list)
    System.out.println(num);

Example 3

/** Precondition: List list is an ArrayList that contains Integer*
 * values sorted in increasing order.
 * Postcondition: value inserted in its correct position in list.
 */
public static void insert(List<Integer> list, Integer value)
{
    int index = 0;
    //find insertion point
    while (index < list.size() &&
        value.compareTo(list.get(index)) > 0)
        index++;
    //insert value
    list.add(index, value);
}

NOTE

Suppose value is larger than all the elements in list. Then the insert method will
throw an IndexOutOfBoundsException if the first part of the test is omitted, namely
index < list.size().
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Example 4
/** @return an ArrayList of random integers from 0 to 100 */
public static List<Integer> getRandomIntList()
{
    List<Integer> list = new ArrayList<Integer>();
    System.out.print("How many integers? ");
    int length = IO.readInt();  //read user input
    for (int i = 0; i < length; i++)
    {
        int newNum = (int) (Math.random() * 101);
        list.add(new Integer(newNum));
    }
    return list;
}

NOTE
1. The variable list is declared to be of type List<Integer> (the interface) but is
    instantiated as type ArrayList<Integer> (the implementation).
2. The add method in getRandomIntList is the List method that appends its
    parameter to the end of the list.

Example 5
/** Swap two values in list, indexed at i and j. */
public static void swap(List<E> list, int i, int j)
{
    E temp = list.get(i);
    list.set(i, list.get(j));
    list.set(j, temp);
}

Example 6
/** Print all negatives in list a.  *
 * Precondition: a contains Integer values.  *
 */
public static void printNegs(List<Integer> a)
{
    System.out.println("The negative values in the list are: ");
    for (Integer i : a)
        if (i.intValue() < 0)
            System.out.println(i);
}

Example 7
/** Change every even-indexed element of strList to the empty string. *
 * Precondition: strList contains String values. *
 */
public static void changeEvenToEmpty(List<String> strList)
{
    boolean even = true;
    int index = 0;
    while (index < strList.size())
    {
        if (even)
            strList.set(index, "");
        index++;
        even = !even;
    }
COLLECTIONS AND ITERATORS

Definition of an Iterator

An iterator is an object whose sole purpose is to traverse a collection, one element at a time. During iteration, the iterator object maintains a current position in the collection, and is the controlling object in manipulating the elements of the collection.

The Iterator\(<E>\) Interface

The package `java.util` provides a generic interface, `Iterator\(<E>\)`, whose methods are `hasNext`, `next`, and `remove`. The Java Collections API allows iteration over each of its collections classes.

THE METHODS OF Iterator\(<E>\)

`boolean hasNext()`

Returns `true` if there’s at least one more element to be examined, `false` otherwise.

`E next()`

Returns the next element in the iteration. If no elements remain, the method throws a `NoSuchElementException`.

`void remove()`

Deletes from the collection the last element that was returned by `next`. This method can be called only once per call to `next`. It throws an `IllegalStateException` if the `next` method has not yet been called, or if the `remove` method has already been called after the last call to `next`.

Using a Generic Iterator

To iterate over a parameterized collection, you must use a parameterized iterator whose parameter is the same type.

Example 1

```java
List<String> list = new ArrayList<String>();
< code to initialize list with strings>
//Print strings in list, one per line.
Iterator<String> itr = list.iterator();
while (itr.hasNext())
    System.out.println(itr.next());
```

NOTE

1. Only classes that allow iteration can use the for-each loop. This is because the loop operates by using an iterator. Thus, the loop in the above example is equivalent to
for (String str : list) //no iterator in sight!
    System.out.println(str);

2. Recall, however, that a for-each loop cannot be used to remove elements from the list. The easiest way to “remove all occurrences of . . . ” from an ArrayList is to use an iterator.

Example 2

/** Remove all 2-character strings from strList.  *
 * Precondition: strList initialized with String objects. 
 */
public static void removeTwos(List<String> strList)
{
    Iterator<String> itr = strList.iterator();
    while (itr.hasNext())
        if (itr.next().length() == 2)
            itr.remove();
}

Example 3

/** Assume a list of integer strings.  *
 * Remove all occurrences of "6" from the list. 
 */
Iterator<String> itr = list.iterator();
while (itr.hasNext())
{
    String num = itr.next();
    if (num.equals("6"))
    {
        itr.remove();
        System.out.println(list);
    }
}

If the original list is 2 6 6 3 5 6 the output will be

[2, 6, 3, 5, 6]
[2, 3, 5, 6]
[2, 3, 5]

Example 4

/** Illustrate NoSuchElementException. */
Iterator<SomeType> itr = list.iterator();
while (true)
    System.out.println(itr.next());

The list elements will be printed, one per line. Then an attempt will be made to move past the end of the list, causing a NoSuchElementException to be thrown. The loop can be corrected by replacing true with itr.hasNext().
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Example 5

/** Illustrate IllegalStateException. */
Iterator<SomeType> itr = list.iterator();
SomeType ob = itr.next();
itr.remove();
itr.remove();

Every remove call must be preceded by a next. The second itr.remove() statement will therefore cause an IllegalStateException to be thrown.

NOTE
In a given program, the declaration

    Iterator<SomeType> itr = list.iterator();

must be made every time you need to initialize the iterator to the beginning of the list.

Example 6

/** Remove all negatives from intList. */
* Precondition: intList contains Integer objects. */
public static void removeNegs(List<Integer> intList)
{
    Iterator<Integer> itr = intList.iterator();
    while (itr.hasNext())
        if (itr.next().intValue() < 0)
            itr.remove();
}

NOTE
1. In Example 6 on p. 246 a for-each loop is used because each element is accessed without changing the list. An iterator operates unseen in the background. Contrast this with Example 6 above, where the list is changed by removing elements. Here you cannot use a for-each loop.
2. To test for a negative value, you could use

        if (itr.next() < 0)

because of auto-unboxing.
3. Use a for-each loop for accessing and modifying objects in a list. Use an iterator for removal of objects.

TWO-DIMENSIONAL ARRAYS

A two-dimensional array (matrix) is often the data structure of choice for objects like board games, tables of values, theater seats, and mazes.

Look at the following 3 × 4 matrix:

\[
\begin{array}{cccc}
2 & 6 & 8 & 7 \\
1 & 5 & 4 & 0 \\
9 & 3 & 2 & 8 \\
\end{array}
\]
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If \( \text{mat} \) is the matrix variable, the row subscripts go from 0 to 2 and the column sub- scripts go from 0 to 3. The element \( \text{mat}[1][2] \) is 4, whereas \( \text{mat}[0][2] \) and \( \text{mat}[2][3] \) are both 8. As with one-dimensional arrays, if the subscripts are out of range, an ArrayIndexOutOfBoundsException is thrown.

Declarations

Each of the following declares a two-dimensional array:

```java
int[][] table; //table can reference a 2-D array of integers
//table is currently a null reference
int[][] matrix = new double[3][4]; //matrix references a 3 x 4
//array of real numbers.
//Each element has value 0.0
String[][] strs = new String[2][5]; //strs references a 2 x 5
//array of String objects.
//Each element is null
```

An initializer list can be used to specify a two-dimensional array:

```java
int[][] mat = { {3, 4, 5}, //row 0
                {6, 7, 8} }; //row 1
```

This defines a \( 2 \times 3 \) rectangular array (i.e., one in which each row has the same number of elements).

The initializer list is a list of lists in which each inside list represents a row of the matrix.

Matrix as Array of Row Arrays

A matrix is implemented as an array of rows, where each row is a one-dimensional array of elements. Suppose \( \text{mat} \) is the \( 3 \times 4 \) matrix

\[
\begin{array}{cccc}
2 & 6 & 8 & 7 \\
1 & 5 & 4 & 0 \\
9 & 3 & 2 & 8 \\
\end{array}
\]

Then \( \text{mat} \) is an array of three arrays:

- \( \text{mat}[0] \) contains \( \{2, 6, 8, 7\} \)
- \( \text{mat}[1] \) contains \( \{1, 5, 4, 0\} \)
- \( \text{mat}[2] \) contains \( \{9, 3, 2, 8\} \)

The quantity \( \text{mat}.\text{length} \) represents the number of rows. In this case it equals 3 because there are three row-arrays in \( \text{mat} \). For any given row \( k \), where \( 0 \leq k < \text{mat}.\text{length} \), the quantity \( \text{mat}[k].\text{length} \) represents the number of elements in that row, namely the number of columns. (Java allows a variable number of elements in each row. Since these “jagged arrays” are not part of the AP Java subset, you can assume that \( \text{mat}[k].\text{length} \) is the same for all rows \( k \) of the matrix, i.e., that the matrix is rectangular.)
Processing a Two-Dimensional Array

There are three common ways to traverse a two-dimensional array:

- **row-column** (for accessing elements, modifying elements that are class objects, or replacing elements)
- **for-each loop** (for accessing elements or modifying elements that are class objects, but no replacement)
- **row-by-row array processing** (for accessing, modifying, or replacement)

**Example 1**

Find the sum of all elements in a matrix `mat`. Here is a row-column traversal.

```java
/**
 * Precondition: mat is initialized with integer values. */
int sum = 0;
for (int r = 0; r < mat.length; r++)
    for (int c = 0; c < mat[r].length; c++)
        sum += mat[r][c];
```

**NOTE**

1. `mat[r][c]` represents the rth row and the cth column.
2. Rows are numbered from 0 to `mat.length-1`, and columns are numbered from 0 to `mat[r].length-1`. Any index that is outside these bounds will generate an `ArrayIndexOutOfBoundsException`.

Since elements are not being replaced, nested for-each loops can be used instead:

```java
for (int[] row : mat) //for each row array in mat
    for (int element : row) //for each element in this row
        sum += element;
```

**NOTE**

Starting in 2015, you will need to know how to use a nested for-each traversal. You will also need to know how to process a matrix as shown below, using the third type of traversal, row-by-row array processing. This traversal assumes access to a method that processes an array. So, continuing with the example to find the sum of all elements in `mat`: In the class where `mat` is defined, suppose you have the method `sumArray`.

```java
/** @return the sum of integers in arr */
public int sumArray(int[] arr)
{
    // implementation not shown
}
```

You could use this method to sum all the elements in `mat` as follows:

```java
int sum = 0;
for (int row = 0; row < mat.length; row++) //for each row in mat,
    sum += sumArray(mat[row]); //add that row's total to sum
```

Note how, since `mat[row]` is an array of int for 0 ≤ row < `mat.length`, you can use the `sumArray` method for each row in `mat`. 
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Example 2

Add 10 to each element in row 2 of matrix mat.

```java
for (int c = 0; c < mat[2].length; c++)
    mat[2][c] += 10;
```

NOTE

1. In the for loop, you can use `c < mat[k].length`, where `0 ≤ k < mat.length`, since each row has the same number of elements.
2. You cannot use a for-each loop here because elements are being replaced.
3. You can, however, use row-by-row array processing. Suppose you have method addTen shown below.

   ```java
   /** Add 10 to each int in arr */
   public void addTen(int[] arr)
   {
       for (int i = 0; i < arr.length; i++)
           arr[i] += 10;
   }
   ```

   You could add 10 to each element in row 2 with the single statement

   ```java
   addTen(mat[2]);
   ```

   You could also add 10 to every element in mat:

   ```java
   for (int row = 0; row < mat.length; row++)
       addTen(mat[row]);
   ```

Example 3

Suppose Card objects have a mutator method changeValue:

```java
public void changeValue(int newValue)
{ value = newValue; }
```

Now consider the declaration

```java
Card[][] cardMatrix;
```

Suppose cardMatrix is initialized with Card objects. A piece of code that traverses the cardMatrix and changes the value of each Card to v is

```java
for (Card[] row : cardMatrix) //for each row array in cardMatrix,
    for (Card c : row) //for each Card in that row,
        c.changeValue(v); //change the value of that card
```

Alternatively:

```java
for (int row = 0; row < cardMatrix.length; row++)
    for (int col = 0; col < cardMatrix[0].length; col++)
        cardMatrix[row][col].changeValue(v);
```

NOTE

The use of the nested for-each loop is OK. Modifying the objects in the matrix with a mutator method is fine. What you can’t do is replace the Card objects with new Cards.
Example 4

The major and minor diagonals of a square matrix are shown below:

![Major diagonal](image1)

![Minor diagonal](image2)

You can process the diagonals as follows:

```java
int[][] mat = new int[SIZE][SIZE]; //SIZE is a constant int value
for (int i = 0; i < SIZE; i++)
    Process mat[i][i]; //major diagonal
OR
    Process mat[i][SIZE - i - 1]; //minor diagonal
```

Two-Dimensional Array as Parameter

Example 1

Here is a method that counts the number of negative values in a matrix.

```java
/**
 * Precondition: mat is initialized with integers.
 * @return count of negative values in mat
 */
public static int countNegs (int[][] mat)
{
    int count = 0;
    for (int[] row : mat)
        for (int num : row)
            if (num < 0)
                count++;
    return count;
}
```

A method in the same class can invoke this method with a statement such as

```java
int negs = countNegs(mat);
```

Example 2

Reading elements into a matrix:

```java
/**
 * Precondition: Number of rows and columns known.
 * @return matrix containing rows \times cols integers
 * read from the keyboard
 */
public static int[][] getMatrix(int rows, int cols)
{
    int[][] mat = new int[rows][cols]; //initialize slots
    System.out.println("Enter matrix, one row per line:");
    System.out.println();

    //read user input and fill slots
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++)
            mat[r][c] = IO.readInt(); //read user input
    return mat;
}
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To call this method:

```java
//prompt for number of rows and columns
int rows = IO.readInt();  //read user input
int cols = IO.readInt();  //read user input
int[][] mat = getMatrix(rows, cols);
```

NOTE

You cannot use a for-each loop in `getMatrix` because elements in `mat` are being replaced. (Their current value is the initialized value of 0. The new value is the input value from the keyboard.)

There is further discussion of arrays and matrices, plus additional questions, in Chapter 9 (The AP Computer Science Labs).

---

Chapter Summary

Manipulation of one-dimensional arrays, two-dimensional arrays, and array lists should be second nature to you by now. Know the Java subset methods for the `List<E>` class. You must also know when these methods throw an `IndexOutOfBoundsException` and when an `ArrayIndexOutOfBoundsException` can occur.

When traversing an `ArrayList`:

- Use a for-each loop to access each element without changing it, or to modify each object in the list using a mutator method.
- Use an `Iterator` to remove elements. (This is not in the AP subset, but it is the easiest way to remove elements from an `ArrayList`.)

A matrix is an array of row arrays. The number of rows is `mat.length`. The number of columns is `mat[0].length`.

When traversing a matrix:

- Use a row-column traversal to access, modify, or replace elements.
- Use a nested for loop to access or modify elements, but not replace them.
- Know how to do row-by-row array processing if you have an appropriate method that takes an array parameter.
MULTIPLE-CHOICE QUESTIONS ON ARRAYS AND ARRAY LISTS

1. Which of the following correctly initializes an array \texttt{arr} to contain four elements each with value 0?
   I \texttt{int[]} \texttt{arr} = \{0, 0, 0, 0\};
   II \texttt{int[]} \texttt{arr} = \texttt{new int}[4];
   III \texttt{int[]} \texttt{arr} = \texttt{new int}[4];
   \hspace{1cm} \texttt{for} (\texttt{int} \texttt{i} = 0; \texttt{i} < \texttt{arr}.\texttt{length}; \texttt{i}++)
   \hspace{1cm} \texttt{arr}[\texttt{i}] = 0;

   (A) I only
   (B) III only
   (C) I and III only
   (D) II and III only
   (E) I, II, and III

2. The following program segment is intended to find the index of the first negative integer in \texttt{arr[0]} \ldots \texttt{arr[N-1]}, where \texttt{arr} is an array of \texttt{N} integers.

   \hspace{1cm} \texttt{int} \texttt{i} = 0;
   \hspace{1cm} \texttt{while} (\texttt{arr}[\texttt{i}] \geq 0)
   \hspace{1cm} \{ \texttt{i}++; \}
   \hspace{1cm} \texttt{location} = \texttt{i};

   This segment will work as intended
   (A) always.
   (B) never.
   (C) whenever \texttt{arr} contains at least one negative integer.
   (D) whenever \texttt{arr} contains at least one nonnegative integer.
   (E) whenever \texttt{arr} contains no negative integers.

3. Refer to the following code segment. You may assume that \texttt{arr} is an array of \texttt{int} values.

   \hspace{1cm} \texttt{int} \texttt{sum} = \texttt{arr[0]}, \texttt{i} = 0;
   \hspace{1cm} \texttt{while} (\texttt{i} < \texttt{arr}.\texttt{length})
   \hspace{1cm} \{ \texttt{i}++;
   \hspace{1cm} \texttt{sum} += \texttt{arr}[\texttt{i}];
   \}

   Which of the following will be the result of executing the segment?
   (A) Sum of \texttt{arr[0]}, \texttt{arr[1]}, \ldots, \texttt{arr[arr.length-1]} will be stored in \texttt{sum}.
   (B) Sum of \texttt{arr[1]}, \texttt{arr[2]}, \ldots, \texttt{arr[arr.length-1]} will be stored in \texttt{sum}.
   (C) Sum of \texttt{arr[0]}, \texttt{arr[1]}, \ldots, \texttt{arr[arr.length]} will be stored in \texttt{sum}.
   (D) An infinite loop will occur.
   (E) A run-time error will occur.
4. Refer to the following code segment. You may assume that array arr1 contains elements arr1[0], arr1[1], ..., arr1[N-1], where N = arr1.length.

```java
int count = 0;
for (int i = 0; i < N; i++)
    if (arr1[i] != 0)
        { 
            arr1[count] = arr1[i];
            count++;
        }
int[] arr2 = new int[count];
for (int i = 0; i < count; i++)
    arr2[i] = arr1[i];
```

If array arr1 initially contains the elements 0, 6, 0, 4, 0, 0, 2 in this order, what will arr2 contain after execution of the code segment?

(A) 6, 4, 2
(B) 0, 0, 0, 0, 6, 4, 2
(C) 6, 4, 2, 4, 0, 0, 2
(D) 0, 6, 0, 4, 0, 0, 2
(E) 6, 4, 2, 0, 0, 0, 0

5. Consider this program segment:

```java
for (int i = 2; i <= k; i++)
    if (arr[i] < someValue)
        System.out.print("SMALL");
```

What is the maximum number of times that SMALL can be printed?

(A) 0
(B) 1
(C) k - 1
(D) k - 2
(E) k
6. What will be output from the following code segment, assuming it is in the same class as the doSomething method?

```java
int[] arr = {1, 2, 3, 4};
doSomething(arr);
System.out.print(arr[1] + " ");
System.out.print(arr[3]);
...
public void doSomething(int[] list)
{
    int[] b = list;
    for (int i = 0; i < b.length; i++)
        b[i] = i;
}
```

(A) 0 0  
(B) 2 4  
(C) 1 3  
(D) 0 2  
(E) 0 3

7. Consider writing a program that reads the lines of any text file into a sequential list of lines. Which of the following is a good reason to implement the list with an ArrayList of String objects rather than an array of String objects?

(A) The get and set methods of ArrayList are more convenient than the [] notation for arrays.  
(B) The size method of ArrayList provides instant access to the length of the list.  
(C) An ArrayList can contain objects of any type, which leads to greater generality.  
(D) If any particular text file is unexpectedly long, the ArrayList will automatically be resized. The array, by contrast, may go out of bounds.  
(E) The String methods are easier to use with an ArrayList than with an array.

8. Consider writing a program that produces statistics for long lists of numerical data. Which of the following is the best reason to implement each list with an array of int (or double), rather than an ArrayList of Integer (or Double) objects?

(A) An array of primitive number types is more efficient to manipulate than an ArrayList of wrapper objects that contain numbers.  
(B) Insertion of new elements into a list is easier to code for an array than for an ArrayList.  
(C) Removal of elements from a list is easier to code for an array than for an ArrayList.  
(D) Accessing individual elements in the middle of a list is easier for an array than for an ArrayList.  
(E) Accessing all the elements is more efficient in an array than in an ArrayList.
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Refer to the following classes for Questions 9–12.

```java
public class Address
{
    private String name;
    private String street;
    private String city;
    private String state;
    private String zip;

    //constructors
    ...

    //accessors
    public String getName()
    { return name; }
    public String getStreet()
    { return street; }
    public String getCity()
    { return city; }
    public String getState()
    { return state; }
    public String getZip()
    { return zip; }
}

public class Student
{
    private int idNum;
    private double gpa;
    private Address address;

    //constructors
    ...

    //accessors
    public Address getAddress()
    { return address; }
    public int getIdNum()
    { return idNum; }
    public double getGpa()
    { return gpa; }
}```
9. A client method has this declaration, followed by code to initialize the list:

    Address[] list = new Address[100];

Here is a code segment to generate a list of *names only*.

    for (Address a : list)
       /* line of code */

Which is a correct /* line of code */?
(A) System.out.println(Address[i].getName());
(B) System.out.println(list[i].getName());
(C) System.out.println(a[i].getName());
(D) System.out.println(a.getName());
(E) System.out.println(list.getName());

10. The following code segment is to print out a list of addresses:

    for (Address addr : list)
       {
           /* more code */
       }

Which is a correct replacement for /* more code */?

   I System.out.println(list[i].getName());
       System.out.println(list[i].getStreet());
       System.out.print(list[i].getCity() + " ");
       System.out.println(list[i].getState() + " ");
       System.out.println(list[i].getZip());

   II System.out.println(addr.getName());
       System.out.println(addr.getStreet());
       System.out.print(addr.getCity() + ", ");
       System.out.println(addr.getState() + " ");
       System.out.println(addr.getZip());

   III System.out.println(addr);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
11. A client method has this declaration:

   Student[] allStudents = new Student[NUM_STUDS];  //NUM_STUDS is
   //an int constant

Here is a code segment to generate a list of Student names only. (You may assume
that allStudents has been initialized.)

   for (Student student : allStudents)
   /* code to print list of names */

Which is a correct replacement for /* code to print list of names */?

(A) System.out.println(allStudents.getName());
(B) System.out.println(student.getName());
(C) System.out.println(student.getAddress().getName());
(D) System.out.println(allStudents.getAddress().getName());
(E) System.out.println(student[i].getAddress().getName());
12. Here is a method that locates the Student with the highest idNum:

```java
/**
 * Precondition: Array stuArr of Student is initialized.
 * return Student with highest idNum
 */
public static Student locate(Student[] stuArr)
{
    /* method body */
}
```

Which of the following could replace /* method body */ so that the method works as intended?

I  
```java
int max = stuArr[0].getIdNum();
for (Student student : stuArr)
    if (student.getIdNum() > max)
    {
        max = student.getIdNum();
        return student;
    }
return stuArr[0];
```

II  
```java
Student highestSoFar = stuArr[0];
int max = stuArr[0].getIdNum();
for (Student student : stuArr)
    if(student.getIdNum() > max)
    {
        max = student.getIdNum();
        highestSoFar = student;
    }
return highestSoFar;
```

III  
```java
int maxPos = 0;
for(int i = 1; i < stuArr.length; i++)
    if(stuArr[i].getIdNum() > stuArr[maxPos].getIdNum())
        maxPos = i;
return stuArr[maxPos];
```

(A) I only  
(B) II only  
(C) III only  
(D) I and III only  
(E) II and III only
Questions 13–15 refer to the Ticket and Transaction classes below.

```java
public class Ticket {
    private String row;
    private int seat;
    private double price;

    //constructor
    public Ticket(String aRow, int aSeat, double aPrice) {
        row = aRow;
        seat = aSeat;
        price = aPrice;
    }

    //accessors getRow(), getSeat(), and getPrice()
    ...
}

public class Transaction {
    private int numTickets;
    private Ticket[] tickList;

    //constructor
    public Transaction(int numTicks) {
        numTickets = numTicks;
        tickList = new Ticket[numTickets];
        String theRow;
        int theSeat;
        double thePrice;
        for (int i = 0; i < numTicks; i++) {
            /* read user input for theRow, theSeat, and thePrice */
            ...
        }
    }

    /** @return total amount paid for this transaction */
    public double totalPaid() {
        double total = 0.0;
        /* code to calculate amount */
        return total;
    }
}
```
13. Which of the following correctly replaces /* more code */ in the Transaction constructor to initialize the tickList array?

(A) tickList[i] = new Ticket(getRow(), getSeat(), getPrice());
(B) tickList[i] = new Ticket(theRow, theSeat, thePrice);
(C) tickList[i] = new tickList(getRow(), getSeat(), getPrice());
(D) tickList[i] = new tickList(theRow, theSeat, thePrice);
(E) tickList[i] = new tickList(numTicks);

14. Which represents correct /* code to calculate amount */ in the totalPaid method?

(A) for (Ticket t : tickList)
   total += t.price;
(B) for (Ticket t : tickList)
   total += tickList.getPrice();
(C) for (Ticket t : tickList)
   total += t.getPrice();
(D) Transaction T;
   for (Ticket t : T)
   total += t.getPrice();
(E) Transaction T;
   for (Ticket t : T)
   total += t.price;

15. Suppose it is necessary to keep a list of all ticket transactions. Assuming that there are NUMSALES transactions, a suitable declaration would be

(A) Transaction[] list0fSales = new Transaction[NUMSALES];
(B) Transaction[] list0fSales = new Ticket[NUMSALES];
(C) Ticket[] list0fSales = new Transaction[NUMSALES];
(D) Ticket[] list0fSales = new Ticket[NUMSALES];
(E) Transaction[] Ticket = new list0fSales[NUMSALES];
16. The following code fragment is intended to find the smallest value in 
arr[0]...arr[n-1].

```c
/** Precondition: 
 * - arr is an array, arr.length = n.
 * - arr[0]...arr[n-1] initialized with integers.
 * Postcondition: min = smallest value in arr[0]...arr[n-1]. */
int min = arr[0];
int i = 1;
while (i < n)
{
    i++;
    if (arr[i] < min)
        min = arr[i];
}
```

This code is incorrect. For the segment to work as intended, which of the following modifications could be made?

I Change the line

```c
int i = 1;
```

to

```c
int i = 0;
```

Make no other changes.

II Change the body of the while loop to

```c
{
    if (arr[i] < min)
        min = arr[i];
    i++;
}
```

Make no other changes.

III Change the test for the while loop as follows:

```c
while (i <= n)
```

Make no other changes.

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
17. Refer to method `match` below:

```java
/**
 * @param v an array of int sorted in increasing order
 * @param w an array of int sorted in increasing order
 * @param N the number of elements in array v
 * @param M the number of elements in array w
 * @return true if there is an integer k that occurs in both arrays; otherwise returns false
 * Precondition:
 * v[0]..v[N-1] and w[0]..w[M-1] initialized with integers.
 * v[0] < v[1] < .. < v[N-1] and w[0] < w[1] < .. < w[M-1].
 */
public static boolean match(int[] v, int[] w, int N, int M)
{
    int vIndex = 0, wIndex = 0;
    while (vIndex < N && wIndex < M)
    {
        if (v[vIndex] == w[wIndex])
            return true;
        else if (v[vIndex] < w[wIndex])
            vIndex++;
        else
            wIndex++;
    }
    return false;
}
```

Assuming that the method has not been exited, which assertion is true at the end of every execution of the `while` loop?

(A) `v[0]..v[vIndex-1] and w[0]..w[wIndex-1] contain no common value, vIndex ≤ N and wIndex ≤ M.`

(B) `v[0]..v[vIndex] and w[0]..w[wIndex] contain no common value, vIndex ≤ N and wIndex ≤ M.`

(C) `v[0]..v[vIndex-1] and w[0]..w[wIndex-1] contain no common value, vIndex ≤ N and wIndex ≤ M-1.`

(D) `v[0]..v[vIndex] and w[0]..w[wIndex] contain no common value, vIndex ≤ N-1 and wIndex ≤ M-1.`

(E) `v[0]..v[N-1] and w[0]..w[M-1] contain no common value, vIndex ≤ N and wIndex ≤ M.`
18. Consider this class:

```java
public class Book {
    private String title;
    private String author;
    private boolean checkoutStatus;

    public Book(String bookTitle, String bookAuthor) {
        title = bookTitle;
        author = bookAuthor;
        checkoutStatus = false;
    }

    /** Change checkout status. */
    public void changeStatus() {
        checkoutStatus = !checkoutStatus;
    }
}
```

A client program has this declaration:

```java
Book[] bookList = new Book[SOME_NUMBER];
```

Suppose `bookList` is initialized so that each `Book` in the list has a title, author, and checkout status. The following piece of code is written, whose intent is to change the checkout status of each book in `bookList`.

```java
for (Book b : bookList)
    b.changeStatus();
```

Which is true about this code?

(A) The `bookList` array will remain unchanged after execution.
(B) Each book in the `bookList` array will have its checkout status changed, as intended.
(C) A `NullPointerException` may occur.
(D) A run-time error will occur because it is not possible to modify objects using the for-each loop.
(E) A logic error will occur because it is not possible to modify objects in an array without accessing the indexes of the objects.
Consider this class for Questions 19 and 20:

```java
class BingoCard {
    private int[] card;

    /** Default constructor: Creates BingoCard with
     * 20 random digits in the range 1 - 90. */
    public BingoCard() {
        // implementation not shown
    }

    /** Display BingoCard. */
    public void display() {
        // implementation not shown
    }
}
```

A program that simulates a bingo game declares an array of `BingoCard`. The array has `NUMPLAYERS` elements, where each element represents the card of a different player. Here is a code segment that creates all the bingo cards in the game:

```java
/* declare array of BingoCard */
/* construct each BingoCard */

19. Which of the following is a correct replacement for

```java
/* declare array of BingoCard */
```

(A) `int[] BingoCard = new BingoCard[NUMPLAYERS];`
(B) `BingoCard[] players = new int[NUMPLAYERS];`
(C) `BingoCard[] players = new BingoCard[20];`
(D) `BingoCard[] players = new BingoCard[NUMPLAYERS];`
(E) `int[] players = new BingoCard[NUMPLAYERS];`

20. Assuming that `players` has been declared as an array of `BingoCard`, which of the following is a correct replacement for

```java
/* construct each BingoCard */
```

I for (BingoCard card : players)  
   card = new BingoCard();

II for (BingoCard card : players)  
   players[card] = new BingoCard();

III for (int i = 0; i < players.length; i++)  
   players[i] = new BingoCard();

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III
Chapter 6  Arrays and Array Lists

21. Which declaration will cause an error?

I  List<String> stringList = new ArrayList<String>();
II List<int> intList = new ArrayList<int>();
III ArrayList<String> compList = new ArrayList<String>();

(A) I only  (B) II only  (C) III only  (D) I and III only  (E) II and III only

22. Consider these declarations:

List<String> strList = new ArrayList<String>();
String ch = " ";
Integer intOb = new Integer(5);

Which statement will cause an error?

(A) strList.add(ch);
(B) strList.add(new String("handy andy"));
(C) strList.add(intOb.toString());
(D) strList.add(ch + 8);
(E) strList.add(intOb + 8);

23. Let list be an ArrayList<Integer> containing these elements:

2 5 7 6 0 1

Which of the following statements would not cause an error to occur? Assume that each statement applies to the given list, independent of the other statements.

(A) Object ob = list.get(6);
(B) Integer intOb = list.add(3.4);
(C) list.add(6, 9);
(D) Object x = list.remove(6);
(E) Object y = list.set(6, 8);
24. Refer to method insert below:

```java
/** @param list an ArrayList of String objects
 * @param element a String object
 * Precondition: list contains String values sorted in decreasing order.
 * Postcondition: element inserted in its correct position in list.
 */
public void insert(List<String> list, String element)
{
    int index = 0;
    while (element.compareTo(list.get(index)) < 0)
        index++;
    list.add(index, element);
}
```

Assuming that the type of element is compatible with the objects in the list, which is a true statement about the insert method?

(A) It works as intended for all values of element.
(B) It fails for all values of element.
(C) It fails if element is greater than the first item in list and works in all other cases.
(D) It fails if element is smaller than the last item in list and works in all other cases.
(E) It fails if element is either greater than the first item or smaller than the last item in list and works in all other cases.

25. Consider the following code segment, applied to list, an ArrayList of Integer values.

```java
int len = list.size();
for (int i = 0; i < len; i++)
{
    list.add(i + 1, new Integer(i));
    Object x = list.set(i, new Integer(i + 2));
}
```

If list is initially 6 1 8, what will it be following execution of the code segment?

(A) 2 3 4 2 1 8
(B) 2 3 4 6 2 2 0 1 8
(C) 2 3 4 0 1 2
(D) 2 3 4 6 1 8
(E) 2 3 3 2
Questions 26 and 27 are based on the Coin and Purse classes given below:

```java
/* A simple coin class */
public class Coin {
    private double value;
    private String name;

    // constructor
    public Coin(double coinValue, String coinName) {
        value = coinValue;
        name = coinName;
    }

    /** @return the value of this coin */
    public double getValue() { return value; }

    /** @return the name of this coin */
    public String getName() { return name; }

    /** @param obj a Coin object
     * @return true if this coin equals obj; otherwise false
     */
    public boolean equals(Object obj) { return name.equals(((Coin) obj).name); }

    // Other methods are not shown.
}

/* A purse holds a collection of coins */
public class Purse {
    private List<Coin> coins;

    /** Creates an empty purse. */
    public Purse() { coins = new ArrayList<Coin>(); }

    /** Adds aCoin to the purse. *
     * @param aCoin the coin to be added to the purse *
     */
    public void add(Coin aCoin) { coins.add(aCoin); }

    /** @return the total value of coins in purse */
    public double getTotal() { /* implementation not shown */ }
}
```
26. Here is the `getTotal` method from the `Purse` class:

```java
/** @return the total value of coins in purse */
public double getTotal()
{
    double total = 0;
    /** more code */
    return total;
}
```

Which of the following is a correct replacement for `/** more code */`?

(A) for (Coin c : coins)
   {
       c = coins.get(i);
       total += c.getValue();
   }

(B) for (Coin c : coins)
   {
       Coin value = c.getValue();
       total += value;
   }

(C) for (Coin c : coins)
   {
       Coin c = coins.get(i);
       total += c.getValue();
   }

(D) for (Coin c : coins)
   {
       total += coins.getValue();
   }

(E) for (Coin c : coins)
   {
       total += c.getValue();
   }
27. Two coins are said to *match* each other if they have the same name or the same value. You may assume that coins with the same name have the same value and coins with the same value have the same name. A boolean method `find` is added to the `Purse` class:

```java
/** @return true if the purse has a coin that matches aCoin, 
 * false otherwise 
 */
public boolean find(Coin aCoin) {
    for (Coin c : coins) {
        /* code to find match */
        if (c.equals(aCoin))
            return true;
    }
    return false;
}
```

Which is a correct replacement for /* code to find match */?

I if (c.equals(aCoin))
    return true;

II if ((c.getName()).equals(aCoin.getName()))
    return true;

III if ((c.getValue()).equals(aCoin.getValue()))
    return true;

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III

28. Which of the following initializes an 8 × 10 matrix with integer values that are perfect squares? (0 is a perfect square.)

I int[][] mat = new int[8][10];

II int[][] mat = new int[8][10];
    for (int r = 0; r < mat.length; r++)
        for (int c = 0; c < mat[r].length; c++)
            mat[r][c] = r * r;

III int[][] mat = new int[8][10];
    for (int c = 0; c < mat[r].length; c++)
        for (int r = 0; r < mat.length; r++)
            mat[r][c] = c * c;

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
29. Consider a class that has this private instance variable:

private int[][] mat;

The class has the following method, alter:

```java
public void alter(int c)
{
    for (int i = 0; i < mat.length; i++)
        for (int j = c + 1; j < mat[0].length; j++)
            mat[i][j-1] = mat[i][j];
}
```

If a 3 × 4 matrix mat is

```
1 3 5 7
2 4 6 8
3 5 7 9
```

then alter(1) will change mat to

(A) 1 5 7 7
    2 6 8 8
    3 7 9 9

(B) 1 5 7
    2 6 8
    3 7 9

(C) 1 3 5 7
    3 5 7 9

(D) 1 3 5 7
    3 5 7 9
    3 5 7 9

(E) 1 7 7 7
    2 8 8 8
    3 9 9 9
30. Consider the following method that will alter the matrix mat:

```java
/** @param mat the initialized matrix
 * @param row the row number
 */
public static void matStuff(int[][] mat, int row)
{
    int numCols = mat[0].length;
    for (int col = 0; col < numCols; col++)
        mat[row][col] = row;
}
```

Suppose mat is originally

```
1 4 9 0
2 7 8 6
5 1 4 3
```

After the method call `matStuff(mat, 2)`, matrix mat will be

(A) 1 4 9 0
    2 7 8 6
    2 2 2 2

(B) 1 4 9 0
    2 2 2 2
    5 1 4 3

(C) 2 2 2 2
    2 2 2 2
    2 2 2 2

(D) 1 4 2 0
    2 7 2 6
    5 1 2 3

(E) 1 2 9 0
    2 2 8 6
    5 2 4 3
31. Assume that a square matrix `mat` is defined by

```java
int[][] mat = new int[SIZE][SIZE];
// SIZE is an integer constant >= 2
```

What does the following code segment do?

```java
for (int i = 0; i < SIZE - 1; i++)
    for (int j = 0; j < SIZE - i - 1; j++)
        swap(mat, i, j, SIZE - j - 1, SIZE - i - 1);
```

You may assume the existence of this `swap` method:

```java
/** Interchange mat[a][b] and mat[c][d]. */
public void swap(int[][] mat, int a, int b, int c, int d)
```

(A) Reflects `mat` through its major diagonal. For example,

```
2 6   2 4
4 3   6 3
```

(B) Reflects `mat` through its minor diagonal. For example,

```
2 6   3 6
4 3   4 2
```

(C) Reflects `mat` through a horizontal line of symmetry. For example,

```
2 6   4 3
4 3   2 6
```

(D) Reflects `mat` through a vertical line of symmetry. For example,

```
2 6   6 2
4 3   3 4
```

(E) Leaves `mat` unchanged.
32. Consider a class `MatrixStuff` that has a private instance variable:

```java
private int[][] mat;
```

Refer to method `alter` below that occurs in the `MatrixStuff` class. (The lines are numbered for reference.)

```java
/** @param mat the matrix initialized with integers
 * @param c the column to be removed
 * Postcondition:
 * - Column c has been removed.
 * - The last column is filled with zeros.
 */
public void alter(int[][] mat, int c)
{
    for (int i = 0; i < mat.length; i++)
        for (int j = c; j < mat[0].length; j++)
            mat[i][j] = mat[i][j+1];
    //code to insert zeros in rightmost column
    ...
}
```

The intent of the method `alter` is to remove column `c`. Thus, if the input matrix `mat` is

```
2 6 8 9
1 5 4 3
0 7 3 2
```

the method call `alter(mat, 1)` should change `mat` to

```
2 8 9 0
1 4 3 0
0 3 2 0
```

The method does not work as intended. Which of the following changes will correct the problem?

I Change line 10 to
```
for (int j = c; j < mat[0].length - 1; j++)
```
and make no other changes.

II Change lines 10 and 11 to
```
for (int j = c + 1; j < mat[0].length; j++)
    mat[i][j-1] = mat[i][j];
```
and make no other changes.

III Change lines 10 and 11 to
```
for (int j = mat[0].length - 1; j > c; j--)
    mat[i][j-1] = mat[i][j];
```
and make no other changes.

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
33. This question refers to the following method:

```java
public static boolean isThere(String[][] mat, int row, int col, String symbol)
{
    boolean yes;
    int i, count = 0;
    for (i = 0; i < SIZE; i++)
        if (mat[i][col].equals(symbol))
            count++;
    yes = (count == SIZE);
    count = 0;
    for (i = 0; i < SIZE; i++)
        if (mat[row][i].equals(symbol))
            count++;
    return (yes || count == SIZE);
}
```

Now consider this code segment:

```java
public final int SIZE = 8;
String[][] mat = new String[SIZE][SIZE];
```

Which of the following conditions on a matrix `mat` of the type declared in the code segment will by itself guarantee that

`isThere(mat, 2, 2, "$")`

will have the value `true` when evaluated?

I The element in row 2 and column 2 is "$
II All elements in both diagonals are "$
III All elements in column 2 are "$

(A) I only  
(B) III only  
(C) I and II only  
(D) I and III only  
(E) II and III only
34. The method `changeNegs` below should replace every occurrence of a negative integer in its matrix parameter with 0.

```java
/** @param mat the matrix
 * Precondition: mat is initialized with integers.
 * Postcondition: All negative values in mat replaced with 0.
 */
public static void changeNegs(int[][] mat)
{
    /* code */
}
```

Which is correct replacement for `/* code */`?

I for (int r = 0; r < mat.length; r++)
    for (int c = 0; c < mat[r].length; c++)
        if (mat[r][c] < 0)
            mat[r][c] = 0;

II for (int c = 0; c < mat[0].length; c++)
    for (int r = 0; r < mat.length; r++)
        if (mat[r][c] < 0)
            mat[r][c] = 0;

III for (int[] row : mat)
    for (int element : row)
        if (element < 0)
            element = 0;

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
35. A two-dimensional array of `double`, `rainfall`, will be used to represent the daily rainfall for a given year. In this scheme, `rainfall[month][day]` represents the amount of rain on the given day and month. For example,

\[
\begin{align*}
\text{rainfall}[1][15] & \quad \text{is the amount of rain on Jan. 15} \\
\text{rainfall}[12][25] & \quad \text{is the amount of rain on Dec. 25}
\end{align*}
\]

The array can be declared as follows:

```java
double[][] rainfall = new double[13][32];
```

This creates 13 rows indexed from 0 to 12 and 32 columns indexed from 0 to 31, all initialized to 0.0. Row 0 and column 0 will be ignored. Column 31 in row 4 will be ignored, since April 31 is not a valid day. In years that are not leap years, columns 29, 30, and 31 in row 2 will be ignored since Feb. 29, 30, and 31 are not valid days.

Consider the method `averageRainfall` below:

```java
/**
 * Precondition:
 * - rainfall is initialized with values representing amounts of rain on all valid days.
 * - Invalid days are initialized to 0.0.
 * - Feb 29 is not a valid day.
 * Postcondition: Returns average rainfall for the year.
 */
public double averageRainfall(double rainfall[][]) {
    double total = 0.0;
    /* more code */
    return total / (13 * 32);
}
```

Which of the following is a correct replacement for `/* more code */` so that the postcondition for the method is satisfied?

I for (int month = 1; month < rainfall.length; month++)
    for (int day = 1; day < rainfall[month].length; day++)
        total += rainfall[month][day];
    return total / (13 * 32);
II for (int month = 1; month < rainfall.length; month++)
    for (int day = 1; day < rainfall[month].length; day++)
        total += rainfall[month][day];
    return total / 365;
III for (double[] month : rainfall)
    for (double rainAmt : month)
        total += rainAmt;
    return total / 365;

(A) None
(B) I only
(C) II only
(D) III only
(E) II and III only
36. This question is based on the Point class below:

```java
public class Point {
    /** The coordinates. */
    private int x;
    private int y;

    public Point (int xValue, int yValue) {
        x = xValue;
        y = yValue;
    }

    /** @return the x-coordinate of this point */
    public int getX() {
        return x;
    }

    /** @return the y-coordinate of this point */
    public int gety() {
        return y;
    }

    /** Set x and y to new_x and new_y. */
    public void setPoint(int new_x, int new_y) {
        x = new_x;
        y = new_y;
    }

    //Other methods are not shown.
}
```

The method changeNegs below takes a matrix of Point objects as parameter and replaces every Point that has as least one negative coordinate with the Point (0,0).

```java
/** @param pointMat the matrix of points
 * Precondition: pointMat is initialized with Point objects.
 * Postcondition: Every point with at least one negative coordinate
 * has been changed to have both coordinates equal to zero.
 */
public static void changeNegs (Point [][] pointMat) {
    /* code */
}
```
Which is a correct replacement for /* code */?

I for (int r = 0; r < pointMat.length; r++)
   for (int c = 0; c < pointMat[r].length; c++)
      if (pointMat[r][c].getx() < 0
         || pointMat[r][c].gety() < 0)
         pointMat[r][c].setPoint(0, 0);

II for (int c = 0; c < pointMat[0].length; c++)
   for (int r = 0; r < pointMat.length; r++)
      if (pointMat[r][c].getx() < 0
         || pointMat[r][c].gety() < 0)
         pointMat[r][c].setPoint(0, 0);

III for (Point[] row : pointMat)
   for (Point p : row)
      if (p.getx() < 0 || p.gety() < 0)
         p.setPoint(0, 0);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
37. A simple Tic-Tac-Toe board is a $3 \times 3$ array filled with either X's, O's, or blanks. Here is a class for a game of Tic-Tac-Toe:

```java
public class TicTacToe {
    private String[][] board;
    private static final int ROWS = 3;
    private static final int COLS = 3;

    /** Construct an empty board. */
    public TicTacToe() {
        board = new String[ROWS][COLS];
        for (int r = 0; r < ROWS; r++)
            for (int c = 0; c < COLS; c++)
                board[r][c] = " ";
    }

    /** @param r the row number
     * @param c the column number
     * @param symbol the symbol to be placed on board[r][c]
     * @Precondition: The square board[r][c] is empty.
     * @Postcondition: symbol placed in that square.
     */
    public void makeMove(int r, int c, String symbol) {
        board[r][c] = symbol;
    }

    /** Creates a string representation of the board, e.g.
     * | o |
     * | xx |
     * | o |
     * @return the string representation of board
     */
    public String toString() {
        String s = "\n";
        for (int r = 0; r < ROWS; r++)
            for (int c = 0; c < COLS; c++)
                s = s + board[r][c];
        return s;
    }
}
```

Which segment represents a correct replacement for /* more code */ for the toString method?

(A) for (int r = 0; r < ROWS; r++)
```java
    { }
```
Multiple-Choice Questions on Arrays and Array Lists

(B) for (int r = 0; r < ROWS; r++)
{
    s = s + "|";
    for (int c = 0; c < COLS; c++)
    {
        s = s + board[r][c];
        s = s + "|\n";
    }
}

(C) for (int r = 0; r < ROWS; r++)
{
    s = s + "|";
    for (int c = 0; c < COLS; c++)
    
        s = s + board[r][c];
    
    s = s + "|\n";
}

(D) for (int r = 0; r < ROWS; r++)
    s = s + "|";
    for (int c = 0; c < COLS; c++)
    {
        s = s + board[r][c];
        s = s + "|\n";
    }

(E) for (int r = 0; r < ROWS; r++)
{
    s = s + "|";
    for (int c = 0; c < COLS; c++)
    
        s = s + board[r][c];
    
    s = s + "|\n";
Chapter 6  Arrays and Array Lists

ANSWER KEY

1. E  14. C  27. D  
4. A  17. A  30. A  
12. E  25. A  

ANSWERS EXPLAINED

1. (E) Segment I is an initializer list which is equivalent to

```java
int[] arr = new int[4];
arr[0] = 0;
arr[1] = 0;
arr[2] = 0;
arr[3] = 0;
```

Segment II creates four slots for integers, which by default are initialized to 0. The for loop in segment III is therefore unnecessary. It is not, however, incorrect.

2. (C) If arr contains no negative integers, the value of i will eventually exceed N-1, and arr[i] will cause an ArrayIndexOutOfBoundsException to be thrown.

3. (E) The intent is to sum elements arr[0], arr[1], ..., arr[arr.length-1]. Notice, however, that when i has the value arr.length-1, it is incremented to arr.length in the loop, so the statement sum += arr[i] uses arr[arr.length], which is out of range.

4. (A) The code segment has the effect of removing all occurrences of 0 from array arr1. The algorithm copies the nonzero elements to the front of arr1. Then it transfers them to array arr2.

5. (C) If arr[i] < someValue for all i from 2 to k, SMALL will be printed on each iteration of the for loop. Since there are k - 1 iterations, the maximum number of times that SMALL can be printed is k - 1.

6. (C) Array arr is changed by doSomething. Here are the memory slots:
7. (D) Arrays are of fixed length and do not shrink or grow if the size of the data set varies. An `ArrayList` automatically resizes the list. Choice A is false: The [] notation is compact and easy to use. Choice B is not a valid reason because an array `arr` also provides instant access to its length with the quantity `arr.length`. Choice C is invalid because an array can also contain objects. Also, generality is beside the point in the given program: The list _must_ hold `String` objects. Choice E is false: Whether a `String` object is `arr[i]` or `list.get(i)`, the `String` methods are equally easy to invoke.

8. (A) In order for numerical elements to be added to an `ArrayList`, each element must be wrapped in a wrapper class before insertion into the list. Then, to retrieve a numerical value from the `ArrayList`, the element must be unboxed using the `intValue` or `doubleValue` methods. Even though these operations can be taken care of with auto-boxing and -unboxing, there are efficiency costs. In an array, you simply use the [] notation for assignment (as in `arr[i] = num`) or retrieval (`value = arr[i]`). Note that choices B and C are false statements: Both insertion and deletion for an array involve writing code to shift elements. An `ArrayList` automatically takes care of this through its `add` and `remove` methods. Choice D is a poor reason for choosing an array. While the `get` and `set` methods of `ArrayList` might be slightly more awkward than using the [] notation, both mechanisms work pretty easily. Choice E is false: Efficiency of access is roughly the same.

9. (D) For each `Address` object `a` in `list`, access the name of the object with `a.getName()`.

10. (B) Since the `Address` class does not have a `toString` method, each data field must explicitly be printed. Segment III would work if there _were_ a `toString` method for the class (but there isn’t, so it doesn’t!). Segment I fails because of incorrect use of the for-each loop: The array index should not be accessed.

11. (C) Each `Student` name must be accessed through the `Address` class accessor `getName()`. The expression `student.getAddress()` accesses the entire address of
12. (E) Both correct solutions are careful not to lose the student who has the highest idNum so far. Segment II does it by storing a reference to the student, highestSoFar. Segment III does it by storing the array index of that student. Code segment I is incorrect because it returns the first student whose idNum is greater than max, not necessarily the student with the highest idNum in the list.

13. (B) For each i, tickList[i] is a new Ticket object that must be constructed using the Ticket constructor. Therefore eliminate choices C, D, and E. Choice A is wrong because getRow(), getSeat(), and getPrice() are accessor for values that already exist for some Ticket object. Note also the absence of the dot member construct.

14. (C) To access the price for each Ticket in the tickList array, the getPrice() accessor in the Ticket class must be used, since price is private to that class. This eliminates choices A and E. Choice B uses the array name incorrectly. Choices D and E incorrectly declare a Transaction object. (The method applies to an existing Transaction object.)

15. (A) An array of type Transaction is required. This eliminates choices C and D. Additionally, choices B and D incorrectly use type Ticket on the right-hand side. Choice E puts the identifier listOfSales in the wrong place.

16. (B) There are two problems with the segment as given:
   1. arr[1] is not tested.
   2. When i has a value of n-1, incrementing i will lead to an out-of-range error for the if(arr[i] < min) test.

Modification II corrects both these errors. The change suggested in III corrects neither of these errors. The change in I corrects (1) but not (2).

17. (A) Notice that either vIndex or wIndex is incremented at the end of the loop. This means that, when the loop is exited, the current values of v[vIndex] and w[wIndex] have not been compared. Therefore, you can only make an assertion for values v[0]...v[vIndex-1] and w[0]...w[wIndex-1]. Also, notice that if there is no common value in the arrays, the exiting condition for the while loop will be that the end of one of the arrays has been reached, namely vIndex equals N or wIndex equals M.

18. (B) Objects in an array can be changed in a for-each loop by using mutator methods of the objects’ class. The changeStatus method, a mutator in the Book class, will work as intended in the given code. Choice C would be true if it were not given that each Book in bookList was initialized. If any given b had a value of null, then a NullPointerException would be thrown.

19. (D) The declaration must start with the type of value in the array, namely BingoCard. This eliminates choices A and E. Eliminate choice B: The type on the right of the assignment should be BingoCard. Choice C is wrong because the number of slots in the array should be NUMPLAYERS, not 20.

20. (C) Segment III is the only segment that works, since the for-each loop cannot be used to replace elements in an array. After the declaration

   BingoCard[] players = new BingoCard[NUMPLAYERS];
each element in the players array is null. The intent in the given code is to replace each null reference with a newly constructed BingoCard.

21. (B) The type parameter in a generic ArrayList must be a class type, not a primitive. Declaration II would be correct if it were

```java
List<Integer> intList = new ArrayList<Integer>();
```

22. (E) All elements added to strList must be of type String. Each choice satisfies this except choice E. Note that in choice D, the expression ch + 8 becomes a String since ch is a String (just one of the operands needs to be a String to convert the whole expression to a String). In choice E, neither intOb nor 8 is a String.

23. (C) The effect of choice C is to adjust the size of the list to 7 and to add the Integer 9 to the last slot (i.e., the slot with index 6). Choices A, D, and E will all cause an IndexOutOfBoundsException because there is no slot with index 6: the last slot has index 5. Choice B will cause a compile-time error, since it is attempting to add an element of type Double to a list of type Integer.

24. (D) If element is smaller than the last item in the list, it will be compared with every item in the list. Eventually index will be incremented to a value that is out of bounds. To avoid this error, the test in the while loop should be

```java
while(index < list.size() &&
   element.compareTo(list.get(index)) < 0)
```

Notice that if element is greater than or equal to at least one item in list, the test as given in the problem will eventually be false, preventing an out-of-range error.

25. (A) Recall that add(index, obj) shifts all elements, starting at index, one unit to the right, then inserts obj at position index. The set(index, obj) method replaces the element in position index with obj. So here is the state of list after each change:

```
   i = 0   6 0 1 8
          2 0 1 8
   i = 1   2 0 1 1 8
          2 3 1 1 8
   i = 2   2 3 1 2 1 8
          2 3 4 2 1 8
```

26. (E) The value of each Coin c in coins must be accessed with c.getValue(). This eliminates choice D. Eliminate choices A and B: The loop accesses each Coin in the coins ArrayList, which means that there should not be any statements attempting to get the next Coin. Choice B would be correct if the first statement in the loop body were

```java
double value = c.getValue();
```

27. (D) Code segment III is wrong because the equals method is defined for objects only. Since getValue returns a double, the quantities c.getValue() and aCoin.getValue() must be compared either using ==, or as described in the box on p. 65 (better).

28. (D) Segment II is the straightforward solution. Segment I is correct because it initializes all slots of the matrix to 0, a perfect square. (By default, all arrays of int or double are initialized to 0.) Segment III fails because r is undefined in the condition c < mat[r].length. In order to do a column-by-column traversal, you need to get the number of columns in each row. The outer for loop could be
for (int c = 0; c < mat[0].length; c++)

Now segment III works. Note that since the array is rectangular, you can use any index \( k \) in the conditional \( c < mat[k].length \), provided that \( k \) satisfies the condition \( 0 \leq k < mat.length \) (the number of rows).

29. (A) Method \( \text{alter} \) shifts all the columns, starting at column \( c+1 \), one column to the left. Also, it does it in a way that overwrites column \( c \). Here are the replacements for the method call \( \text{alter}(1) \):

\[
\begin{align*}
\text{mat}[0][1] &= \text{mat}[0][2] \\
\text{mat}[0][2] &= \text{mat}[0][3] \\
\text{mat}[1][1] &= \text{mat}[1][2] \\
\text{mat}[1][2] &= \text{mat}[1][3] \\
\text{mat}[2][1] &= \text{mat}[2][2] \\
\text{mat}[2][2] &= \text{mat}[2][3]
\end{align*}
\]

30. (A) \( \text{matStuff} \) processes the row selected by the row parameter, 2 in the method call. The row value, 2, overwrites each element in row 2. Don’t make the mistake of selecting choice B—the row labels are 0, 1, 2.

31. (B) Hand execute this for a \( 2 \times 2 \) matrix. \( i \) goes from 0 to 0, \( j \) goes from 0 to 0, so the only interchange is swap \( \text{mat}[0][0] \) with \( \text{mat}[1][1] \), which suggests choice B. Check with a \( 3 \times 3 \) matrix:

\[
\begin{align*}
\text{mat}[0][0] &= \text{mat}[2][2] \\
\text{mat}[0][1] &= \text{mat}[2][2] \\
\text{mat}[0][2] &= \text{mat}[2][2] \\
\text{mat}[1][0] &= \text{mat}[2][2] \\
\text{mat}[1][1] &= \text{mat}[2][2] \\
\text{mat}[1][2] &= \text{mat}[2][2] \\
\text{mat}[2][0] &= \text{mat}[2][2] \\
\text{mat}[2][1] &= \text{mat}[2][2] \\
\text{mat}[2][2] &= \text{mat}[2][2]
\end{align*}
\]

The elements to be interchanged are shown paired in the following figure. The result will be a reflection through the minor diagonal.

32. (D) The method as given will throw an \( \text{ArrayIndexOutOfBoundsException} \). For the matrix in the example, \( \text{mat}[0].length \) is 4. The call \( \text{mat.alter}(1) \) gives \( c \) a value of 1. Thus, in the inner \( for \) loop, \( j \) goes from 1 to 3. When \( j \) is 3, the line

\[
\text{mat}[i][j] = \text{mat}[i][j+1]
\]

becomes \( \text{mat}[i][3] = \text{mat}[i][4] \). Since columns go from 0 to 3, \( \text{mat}[i][4] \) is out of range. The changes in segments I and II both fix this problem. In each case, the correct replacements are made for each row

\[
\begin{align*}
\text{mat}[i][1] &= \text{mat}[i][2] \\
\text{mat}[i][2] &= \text{mat}[i][3]
\end{align*}
\]

Segment III makes the following incorrect replacements as \( j \) goes from 3 to 2:

\[
\begin{align*}
\text{mat}[i][2] &= \text{mat}[i][3] \\
\text{mat}[i][1] &= \text{mat}[i][2]
\end{align*}
\]

This will cause both columns 1 and 2 to be overwritten. Before inserting zeros in the last column, \( \text{mat} \) will be

\[
\begin{align*}
2 & 9 & 9 & 9 \\
1 & 3 & 3 & 3 \\
0 & 2 & 2 & 2
\end{align*}
\]

This does not achieve the intended postcondition of the method.

33. (B) For the method call \( \text{isThere(mat, 2, 2, "$")} \), the code counts how many times "$" appears in row 2 and how many times in column 2. The method returns true only if \( \text{count} == \text{SIZE} \) for either the row or column pass (i.e., the
whole of row 2 or the whole of column 2 contains the symbol "$". This eliminates choices I and II.

34. (D) Segment I is a row-by-row traversal; segment II is a column-by-column traversal. Each achieves the correct postcondition. Segment III traverses the matrix but does not alter it. All that is changed is the local variable element. You cannot use this kind of loop to replace elements in an array.

35. (E) Since there are 365 valid days in a year, the divisor in calculating the average must be 365. It may appear that segments II and III are incorrect because they include rainfall for invalid days in total. Since these values are initialized to 0.0, however, including them in the total won’t affect the final result.

36. (E) This is similar to the previous question, but in this case segment III is also correct. This is because instead of replacing a matrix element, you are modifying it using a mutator method.

37. (E) There are three things that must be done in each row:
   • Add an opening boundary line:
     ```
     s = s + "|";
     ```
   • Add the symbol in each square:
     ```
     for (int c = 0; c < COLS; c++)
     s = s + board[r][c];
     ```
   • Add a closing boundary line and go to the next line:
     ```
     s = s + "|n";
     ```

   All of these statements must therefore be enclosed in the outer for loop, that is,
   ```
   for (int r = ...)
   ```
Recursion

Chapter 7

Recursion n. See recursion.

Chapter Goals

- Understanding recursion
- Recursive methods
- Recursion in two-dimensional grids
- Recursive helper methods
- Analysis of recursive algorithms
- Tracing recursive algorithms

RECURSIVE METHODS

A recursive method is a method that calls itself. For example, here is a program that calls a recursive method `stackWords`.

```java
public class WordPlay {
    public static void stackWords() {
        String word = IO.readString(); //read user input
        if (word.equals("."))
            System.out.println();
        else
            stackWords();
        System.out.println(word);
    }

    public static void main(String args[]) {
        System.out.println("Enter list of words, one per line.");
        System.out.println("Final word should be a period (.)");
        stackWords();
    }
}
```

Here is the output if you enter

```
hold
my
hand
```

In the multiple-choice section of the AP exam, you will be asked to understand and trace recursive methods. You will not, however, be asked to come up with code for recursive methods in the free-response part of the exam.
You get

```
  .
  hand
  my
  hold
```

The program reads in a list of words terminated with a period, and prints the list in reverse order, starting with the period. How does this happen?

Each time the recursive call to `stackWords()` is made, execution goes back to the start of a new method call. The computer must remember to complete all the pending calls to the method. It does this by stacking the statements that must still be executed as follows: The first time `stackWords()` is called, the word "hold" is read and tested for being a period. No it’s not, so `stackWords()` is called again. The statement to output "hold" (which has not yet been executed) goes on a stack, and execution goes to the start of the method. The word "my" is read. No, it’s not a period, so the command to output "my" goes on the stack. And so on. The stack looks something like this before the recursive call in which the period is read:

```
System.out.println("hand");
System.out.println("my");
System.out.println("hold");
```

Imagine that these statements are stacked like plates. In the final `stackWords()` call, word has the value ".": Yes, it is a period, so the `stackWords()` line is skipped, the period is printed on the screen, and the method call terminates. The computer now completes each of the previous method calls in turn by “popping” the statements off the top of the stack. It prints "hand", then "my", then "hold", and execution of method `stackWords()` is complete.

**NOTE**

1. Each time `stackWords()` is called, a new local variable word is created.
2. The first time the method actually terminates, the program returns to complete the most recently invoked previous call. That’s why the words get reversed in this example.

---

**GENERAL FORM OF SIMPLE RECURSIVE METHODS**

Every recursive method has two distinct parts:

- A base case or termination condition that causes the method to end.
- A nonbase case whose actions move the algorithm toward the base case and termination.

---

1Actually, the computer stacks the pending statements in a recursive method call more efficiently than the way described. But conceptually this is how it is done.
Here is the framework for a simple recursive method that has no specific return type.

```java
public void recursiveMethod( ... )
{
    if (base case)
        <Perform some action>
    else
    {
        <Perform some other action>
        recursiveMethod( ... );  //recursive method call
    }
}
```

The base case typically occurs for the simplest case of the problem, such as when an integer has a value of 0 or 1. Other examples of base cases are when some key is found, or an end-of-file is reached. A recursive algorithm can have more than one base case.

In the `else` or nonbase case of the framework shown, the code fragment `<Perform some other action>` and the method call `recursiveMethod` can sometimes be interchanged without altering the net effect of the algorithm. Be careful though, because what does change is the order of executing statements. This can sometimes be disastrous. (See the `eraseBlob` example on p. 299.)

**Example 1**

```java
public void drawLine(int n)
{
    if (n == 0)
        System.out.println("That’s all, folks!");
    else
    {
        for (int i = 1; i <= n; i++)
            System.out.print("*");
        System.out.println();
        drawLine(n - 1);
    }
}
```

The method call `drawLine(3)` produces this output:

```
***
**
*
That’s all, folks!
```

**NOTE**

1. A method that has no pending statements following the recursive call is an example of *tail recursion*. Method `drawLine` is such a case, but `stackWords` is not.
2. The base case in the `drawLine` example is `n == 0`. Notice that each subsequent call, `drawLine(n - 1)`, makes progress toward termination of the method. If your method has no base case, or if you never reach the base case, you will create *infinite recursion*. This is a catastrophic error that will cause your computer eventually to run out of memory and give you heart-stopping messages like `java.lang.StackOverflowError ... .`
Example 2

//Illustrates infinite recursion.
public void catastrophe(int n)
{
    System.out.println(n);
    catastrophe(n);
}

Try running the case catastrophe(1) if you have lots of time to waste!

## Writing Recursive Methods

To come up with a recursive algorithm, you have to be able to frame a process recursively (i.e., in terms of a simpler case of itself). This is different from framing it iteratively, which repeats a process until a final condition is met. A good strategy for writing recursive methods is to first state the algorithm recursively in words.

### Example 1

Write a method that returns \( n! \) \((n \text{ factorial})\).

<table>
<thead>
<tr>
<th>(n!) defined iteratively</th>
<th>(n!) defined recursively</th>
</tr>
</thead>
<tbody>
<tr>
<td>(0! = 1)</td>
<td>(0! = 1)</td>
</tr>
<tr>
<td>(1! = 1)</td>
<td>(1! = (1)(0!))</td>
</tr>
<tr>
<td>(2! = (2)(1))</td>
<td>(2! = (2)(1))</td>
</tr>
<tr>
<td>(3! = (3)(2)(1))</td>
<td>(3! = (3)(2)!)</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
</tr>
</tbody>
</table>

The general recursive definition for \( n! \) is

\[
n! = \begin{cases} 
1 & n = 0 \\
(n(n-1))! & n > 0 
\end{cases}
\]

The definition seems to be circular until you realize that if \( 0! \) is defined, all higher factorials are defined. Code for the recursive method follows directly from the recursive definition:

```java
/** Compute \( n! \) recursively. 
 * @param n a nonnegative integer 
 * @return \( n! \) 
 */
public static int factorial(int n)
{
    if (n == 0) //base case
        return 1;
    else
        return n * factorial(n - 1);
}
```

### Example 2

Write a recursive method `revDigs` that outputs its integer parameter with the digits reversed. For example,
First, describe the process recursively: Output the rightmost digit. Then, if there are
still digits left in the remaining number \( n/10 \), reverse its digits. Repeat this until
\( n/10 \) is 0. Here is the method:

```java
/** @param n a nonnegative integer
 * @return n with its digits reversed */
public static void revDigs(int n)
{
    System.out.print(n % 10); // rightmost digit
    if (n / 10 != 0) // base case
        revDigs(n / 10);
}
```

NOTE
On the AP exam, you are expected to “understand and evaluate” recursive methods.
This means that you would not be asked to come up with the code for methods such
as `factorial` and `revDigs` (as shown above). You could, however, be asked to identify
output for any given call to `factorial` or `revDigs`.

ANALYSIS OF RECURSIVE METHODS

Recall the Fibonacci sequence 1, 1, 2, 3, 5, 8, 13, . . . . The \( n \)th Fibonacci number equals
the sum of the previous two numbers if \( n \geq 3 \). Recursively,

\[
Fib(n) = \begin{cases} 
1, & n = 1, 2 \\
Fib(n - 1) + Fib(n - 2), & n \geq 3
\end{cases}
\]

Here is the method:

```java
/** @param n a positive integer
 * @return the nth Fibonacci number */
public static int fib(int n)
{
    if (n == 1 || n == 2)
        return 1;
    else
        return fib(n - 1) + fib(n - 2);
}
```

Notice that there are two recursive calls in the last line of the method. So to find \( Fib(5) \),
for example, takes eight recursive calls to `fib`!
In general, each call to `fib` makes two more calls, which is the tipoff for an exponential algorithm (i.e., one that is very inefficient). This is much slower than the run time of the corresponding iterative algorithm (see Chapter 5, Question 13).

You may ask: Since every recursive algorithm can be written iteratively, when should programmers use recursion? Bear in mind that recursive algorithms can incur extra run time and memory. Their major plus is elegance and simplicity of code.

### General Rules for Recursion

1. Avoid recursion for algorithms that involve large local arrays—too many recursive calls can cause memory overflow.
2. Use recursion when it significantly simplifies code.
3. Avoid recursion for simple iterative methods like factorial, Fibonacci, and the linear search on the next page.
4. Recursion is especially useful for
   - Branching processes like traversing trees or directories.
   - Divide-and-conquer algorithms like mergesort and binary search.

### SORTING ALGORITHMS THAT USE RECURSION

Mergesort and quicksort are discussed in Chapter 8.

### RECURSIVE HELPER METHODS

A common technique in designing recursive algorithms is to have a public nonrecursive driver method that calls a private recursive helper method to carry out the task. The main reasons for doing this are

- To hide the implementation details of the recursion from the user.
- To enhance the efficiency of the program.

**Example 1**

Consider the simple example of recursively finding the sum of the first `n` positive integers.

```java
/** @param n a positive integer
 * @return 1 + 2 + 3 + ... + n
 */
public static int sum(int n) {
    if (n == 1)
        return 1;
    else
        return n + sum(n - 1);
}
```
Notice that you get infinite recursion if \( n \leq 0 \). Suppose you want to include a test for \( n > 0 \) before you execute the algorithm. Placing this test in the recursive method is inefficient because if \( n \) is initially positive, it will remain positive in subsequent recursive calls. You can avoid this problem by using a driver method called \( \text{getSum} \), which does the test on \( n \) just once. The recursive method \( \text{sum} \) becomes a private helper method.

```java
public class FindSum {
    /** Private recursive helper method. *
     * @param n a positive integer
     * @return 1 + 2 + 3 + ... + n *
     */
    private static int sum(int n) {
        if (n == 1)
            return 1;
        else
            return n + sum(n - 1);
    }

    /* Driver method */
    public static int getSum(int n) {
        if (n > 0)
            return sum(n);
        else
            throw new IllegalArgumentException(
                "Error: n must be positive");
    }
}
```

**NOTE**

This is a trivial method used to illustrate a private recursive helper method. In practice, you would never use recursion to find a simple sum!

**Example 2**

Consider a recursive solution to the problem of doing a sequential search for a key in an array of strings. If the key is found, the method returns \text{true}, otherwise it returns \text{false}.

The solution can be stated recursively as follows:

- If the key is in \( a[0] \), then the key is found.
- If not, recursively search the array starting at \( a[1] \).
- If you are past the end of the array, then the key wasn’t found.

Here is a straightforward (but inefficient) implementation:
public class Searcher {
    /** Recursively search array a for key.
     * @param a the array of String objects
     * @param key a String object
     * @return true if a[k] equals key for 0 <= k < a.length;
     * false otherwise
     */
    public boolean search(String[] a, String key) {
        if (a.length == 0) //base case. key not found
            return false;
        else if (a[0].compareTo(key) == 0) //base case 
            return true;
        else {
            String[] shorter = new String[a.length-1];
            for (int i = 0; i < shorter.length; i++)
                shorter[i] = a[i+1];
            return search(shorter, key);
        }
    }

    public static void main(String[] args) {
        String[] list = {"Mary", "Joe", "Lee", "Jake"};
        Searcher s = new Searcher();
        System.out.println("Enter key: Mary, Joe, Lee or Jake.");
        String key = IO.readString(); //read user input
        boolean result = s.search(list, key);
        if (!result)
            System.out.println(key + " was not found.");
        else
            System.out.println(key + " was found.");
    }
}

Notice how horribly inefficient the search method is: For each recursive call, a new array shorter has to be created! It is much better to use a parameter, startIndex, to keep track of where you are in the array. Replace the search method above with the following one, which calls the private helper method recurSearch:

    /** Driver method. Searches array a for key.
     * @Precondition: a contains at least one element.
     * @param a the array of String objects
     * @param key a String object
     * @return true if a[k] equals key for 0 <= k < a.length;
     * false otherwise
     */
    public boolean search(String[] a, String key) {
        return recurSearch(a, 0, key);
    }

    public boolean recurSearch(String[] a, int startIndex, String key) {
        if (startIndex >= a.length) //base case. key not found
            return false;
        else if (a[startIndex].compareTo(key) == 0) //base case
            return true;
        else {
            String[] shorter = new String[a.length-1];
            for (int i = startIndex; i < shorter.length; i++)
                shorter[i] = a[i+1];
            return recurSearch(shorter, startIndex+1, key);
        }
    }
/** Recursively search array a for key, starting at startIndex.
 * Precondition:
 * - a contains at least one element.
 * - 0 <= startIndex <= a.length.
 * @return true if a[k] equals key for 0 <= k < a.length;
 * false otherwise
 */
private boolean recurSearch(String[] a, int startIndex, String key) {
    if (startIndex == a.length) // base case. key not found
        return false;
    else if (a[startIndex].compareTo(key) == 0) // base case
        return true;
    else
        return recurSearch(a, startIndex+1, key);
}

NOTE
1. Using the parameter startIndex avoids having to create a new array object for each recursive call. Making startIndex a parameter of a helper method hides implementation details from the user.
2. The helper method is private because it is called only by search within the Searcher class.
3. It’s easy to modify the search method to return the index in the array where the key is found: Make the return type int and return startIndex if the key is found, -1 (say) if it isn’t.

RECURSION IN TWO-DIMENSIONAL GRIDS

Here is a commonly used technique: using recursion to traverse a two-dimensional array. The problem comes in several different guises, for example,

1. A game board from which you must remove pieces.
2. A maze with walls and paths from which you must try to escape.
3. White “containers” enclosed by black “walls” into which you must “pour paint.”

In each case, you will be given a starting position (row, col) and instructions on what to do. The recursive solution typically involves these steps:

Check that the starting position is not out of range:
If (starting position satisfies some requirement)
Perform some action to solve problem
RecursiveCall(row+1, col)
RecursiveCall(row−1, col)
RecursiveCall(row, col + 1)
RecursiveCall(row, col − 1)
Example

On the right is an image represented as a square grid of black and white cells. Two cells in an image are part of the same “blob” if each is black and there is a sequence of moves from one cell to the other, where each move is either horizontal or vertical to an adjacent black cell. For example, the diagram represents an image that contains two blobs, one of them consisting of a single cell.

Assuming the following Image class declaration, you are to write the body of the eraseBlob method, using a recursive algorithm.

```
public class Image {
    private final int BLACK = 1;
    private final int WHITE = 0;
    private int[][] image;  //square grid
    private int size;       //number of rows and columns

    public Image()  //constructor
    { /* implementation not shown */ }

    public void display()  //displays Image
    { /* implementation not shown */ }

    /**
     * Precondition: Image is defined with either BLACK or WHITE cells.
     * Postcondition: If 0 <= row < size, 0 <= col < size, and
     * image[row][col] is BLACK, set all cells in the
     * same blob to WHITE. Otherwise image is unchanged.
     * @param row the given row
     * @param col the given column
     */
    public void eraseBlob(int row, int col)
    { /* your code goes here */ }
}
```

Solution:

```
public void eraseBlob(int row, int col)
{
    if (row >= 0 && row < size && col >= 0 && col < size)
        if (image[row][col] == BLACK)
            {image[row][col] = WHITE;
             eraseBlob(row - 1, col);
             eraseBlob(row + 1, col);
             eraseBlob(row, col - 1);
             eraseBlob(row, col + 1);
            }
}
```

NOTE

1. The ordering of the four recursive calls is irrelevant.
2. The test
   
   ```java
   if (image[row][col] == BLACK)
   ```

   can be included as the last piece of the test in the first line:

   ```java
   if (row >= 0 && ...
   ```

   If row or col is out of range, the test will short-circuit, avoiding the dreaded `ArrayIndexOutOfBoundsException`.

3. If you put the statement
   ```java
   image[row][col] = WHITE;
   ```

   after the four recursive calls, you get infinite recursion if your blob has more than one cell. This is because, when you visit an adjacent cell, one of its recursive calls visits the original cell. If this cell is still BLACK, yet more recursive calls are generated, ad infinitum.

A final thought: Recursive algorithms can be tricky. Try to state the solution recursively in words before you launch into code. Oh, and don’t forget the base case!

**Sample Free-Response Question 1**

Here is a sample free-response question that uses recursion in a two-dimensional array. See if you can answer it before looking at the solution.

A *color grid* is defined as a two-dimensional array whose elements are character strings having values "b" (blue), "r" (red), "g" (green), or "y" (yellow). The elements are called pixels because they represent pixel locations on a computer screen. For example,

```
  b b g r  y g r
  g r g r  b y g
```

A *connected region* for any pixel is the set of all pixels of the same color that can be reached through a direct path along horizontal or vertical moves starting at that pixel. A connected region can consist of just a single pixel or the entire color grid. For example, if the two-dimensional array is called `pixels`, the connected region for `pixels[1][0]` is as shown here for three different arrays.

```
  b b g r  y g r b  b b
  g r g r  g g y g  b g g
```

The class `ColorGrid`, whose declaration is shown below, is used for storing, displaying, and changing the colors in a color grid.
public class ColorGrid
{
    private String[][] pixels;
    private int rows;
    private int cols;

    /** Creates numRows × numCols ColorGrid from String s.
     * @param s the string containing colors of the ColorGrid
     * @param numRows the number of rows in the ColorGrid
     * @param numCols the number of columns in the ColorGrid
     */
    public ColorGrid(String s, int numRows, int numCols)
    { /* to be implemented in part (a) */ }

    /** Precondition:
     * - pixels[row][col] is oldColor, one of "r", "b","g", or "y".
     * - newColor is one of "r","b","g", or "y".
     * Postcondition:
     * - If 0 <= row < rows and 0 <= col < cols, paints the
     *   connected region of pixels[row][col] the newColor.
     * - Does nothing if oldColor is the same as newColor.
     * @param row the given row
     * @param col the given column
     * @param newColor the new color for painting
     * @param oldColor the current color of pixels[row][col]
     */
    public void paintRegion(int row, int col, String newColor,
                             String oldColor)
    { /* to be implemented in part (b) */ }

    //Other methods are not shown.
}

(a) Write the implementation code for the ColorGrid constructor. The constructor should initialize the pixels matrix of the ColorGrid as follows: The dimensions of pixels are numRows × numCols. String s contains numRows × numCols characters, where each character is one of the colors of the grid—"r", "g", "b", or "y". The characters are contained in s row by row from top to bottom and left to right. For example, given that numRows is 3, and numCols is 4, if s is "brrygrgyyyr", pixels should be initialized to be

b r r y
g r g g
y y y r

Complete the constructor below:

/** Creates numRows × numCols ColorGrid from String s.
 * @param s the string containing colors of the ColorGrid
 * @param numRows the number of rows in the ColorGrid
 * @param numCols the number of columns in the ColorGrid
 */
public ColorGrid(String s, int numRows, int numCols)
(continued) 

(b) Write the implementation of the paintRegion method as started below. **Note:**
**You must write a recursive solution.** The paintRegion paints the connected region of the given pixel, specified by row and col, a different color specified by the newColor parameter. If newColor is the same as oldColor, the color of the given pixel, paintRegion does nothing. To visualize what paintRegion does, imagine that the different colors surrounding the connected region of a given pixel form a boundary. When paint is poured onto the given pixel, the new color will fill the connected region up to the boundary.

For example, the effect of the method call `c.paintRegion(2, 3, "b", "r")` on the ColorGrid `c` is shown here. (The starting pixel is shown in a frame, and its connected region is shaded.)

```
before                                    after
 r r b g y y                                r r b g y y
 b r b y r r                                b r b y b b
 g g r r x r b                              g g b b b b
 y r x y r b                                y b b y b b
```

Complete the method paintRegion below. **Note:** Only a recursive solution will be accepted.

```java
/**
 * Precondition:
 * - pixels[row][col] is oldColor, one of "r", "b", "g", or "y".
 * - newColor is one of "r", "b", "g", or "y".
 * - If 0 \leq row < rows and 0 \leq col < cols, paints the connected region of pixels[row][col] the newColor.
 * - Does nothing if oldColor is the same as newColor.
 * @param row the given row
 * @param col the given column
 * @param newColor the new color for painting
 * @param oldColor the current color of pixels[row][col]
 */
public void paintRegion(int row, int col, String newColor, String oldColor)
```

**Solution**

(a) public ColorGrid(String s, int numRows, int numCols)
```java
{ 
    rows = numRows;
    cols = numCols;
    pixels = new String[numRows][numCols];
    int stringIndex = 0;
    for (int r = 0; r < numRows; r++)
        for (int c = 0; c < numCols; c++)
            { 
                pixels[r][c] = s.substring(stringIndex, stringIndex + 1);
                stringIndex++;
            }
} 
```
Recursion in Two-Dimensional Grids

(b) public void paintRegion(int row, int col, String newColor, String oldColor)
{
    if (row >= 0 && row < rows && col >= 0 && col < cols)
        if (!pixels[row][col].equals(newColor) &&
            pixels[row][col].equals(oldColor))
            {  
                pixels[row][col] = newColor;
                paintRegion(row + 1, col, newColor, oldColor);
                paintRegion(row - 1, col, newColor, oldColor);
                paintRegion(row, col + 1, newColor, oldColor);
                paintRegion(row, col - 1, newColor, oldColor);
            }
}

NOTE

• In part (a), you don’t need to test if stringIndex is in range: The precondition states that the number of characters in s is numRows * numCols.
• In part (b), each recursive call must test whether row and col are in the correct range for the pixels array; otherwise, your algorithm may sail right off the edge!
• Don’t forget to test if newColor is different from that of the starting pixel. Method paintRegion does nothing if the colors are the same.
• Also, don’t forget to test if the current pixel is oldColor—you don’t want to overwrite all the colors, just the connected region of oldColor!
• The color-change assignment pixels[row][col] = newColor must precede the recursive calls to avoid infinite recursion.

Sample Free-Response Question 2

Here is another sample free-response question that uses recursion.

This question refers to the Sentence class below. Note: A word is a string of consecutive nonblank (and nonwhitespace) characters. For example, the sentence

“Hello there!” she said.

consists of the four words

"Hello there!" she said.
(a) Complete the `Sentence` constructor as started below. The constructor assigns `str` to `sentence`. You should write the subsequent code that assigns a value to `numWords`, the number of words in `sentence`.

Complete the constructor below:
Recursion in Two-Dimensional Grids

/** Constructor. Creates sentence from String str.  
* Finds the number of words in sentence.  
* @param str the string containing a sentence 
*/
public Sentence(String str) {
    sentence = str;
}

(b) Consider the problem of testing whether a string is a palindrome. A palindrome reads the same from left to right and right to left, ignoring spaces, punctuation, and capitalization. For example,

A Santa lived as a devil at NASA.  
Flo, gin is a sin! I golf.  
Eva, can I stab bats in a cave?

A public method isPalindrome is added to the Sentence class. Here is the method and its implementation:

/** @return true if sentence is a palindrome, false otherwise  
*/
public boolean isPalindrome() {
    String temp = removeBlanks(sentence);
    temp = removePunctuation(temp);
    temp = lowerCase(temp);
    return isPalindrome(temp, 0, temp.length() - 1);
}

The overloaded isPalindrome method contained in the code is a private recursive helper method, also added to the Sentence class. You are to write the implementation of this method. It takes a “purified” string as a parameter, namely one that has been stripped of blanks and punctuation and is all lowercase letters. It also takes as parameters the first and last index of the string. It returns true if this “purified” string is a palindrome, false otherwise.

An recursive algorithm for testing if a string is a palindrome is as follows:

• If the string has length 0 or 1, it’s a palindrome.  
• Remove the first and last letters.  
• If those two letters are the same, and the remaining string is a palindrome, then the original string is a palindrome. Otherwise it’s not.

Complete the isPalindrome method below:

/** Private recursive helper method that tests whether a substring  
* of string s is a palindrome.  
* @param s the given string  
* @param start the index of the first character of the substring  
* @param end the index of the last character of the substring  
* @return true if the substring is a palindrome, false otherwise  
* @Precondition: s contains no spaces, punctuation, or capitals. 
*/
private static boolean isPalindrome(String s, int start, int end)

(continued)
Chapter 7  Recursion

Solution

(a) public Sentence(String str)
{
    sentence = str;
    numWords = 1;
    int k = str.indexOf(" ");
    while (k != -1) //while there are still blanks in str
    {
        numWords++;
        str = str.substring(k + 1); //substring after blank
        k = str.indexOf(" "); //get index of next blank
    }
}

(b) private static boolean isPalindrome(String s, int start, int end)
{
    if (start >= end) //substring has length 0 or 1
        return true;
    else
    {
        String first = s.substring(start, start + 1);
        String last = s.substring(end, end + 1);
        if (first.equals(last))
            return isPalindrome(s, start + 1, end - 1);
        else
            return false;
    }
}

NOTE

• In part (a), for every occurrence of a blank in sentence, numWords must be incremented. (Be sure to initialize numWords to 1!)
• In part (a), the code locates all the blanks in sentence by replacing str with the substring that consists of the piece of str directly following the most recently located blank.
• Recall that indexOf returns -1 if its String parameter does not occur as a substring in its String calling object.
• In part (b), the start and end indexes move toward each other with each subsequent recursive call. This shortens the string to be tested in each call. When start and end meet, the base case has been reached.
• Notice the private static methods in the Sentence class, including the helper method you were asked to write. They are static because they are not invoked by a Sentence object (no dot member construct). The only use of these methods is to help achieve the postconditions of other methods in the class.

Chapter Summary

On the AP exam you will be expected to calculate the results of recursive method calls. Recursion becomes second nature when you practice a lot of examples. For the
more difficult questions, untangle the statements with either repeated method calls (like that shown in the solution to Question 5 on p. 319), or box diagrams (as shown in the solution to Question 12 on p. 320).

You should understand that recursive algorithms can be very inefficient.
MULTIPLE-CHOICE QUESTIONS ON RECURSION

1. Which of the following statements about recursion are true?

   I. Every recursive algorithm can be written iteratively.
   II. Tail recursion is always used in “divide-and-conquer” algorithms.
   III. In a recursive definition, a process is defined in terms of a simpler case of itself.

   (A) I only
   (B) III only
   (C) I and II only
   (D) I and III only
   (E) II and III only

2. Which of the following, when used as the /* body */ of method sum, will enable that method to compute $1 + 2 + \cdots + n$ correctly for any $n > 0$?

   /** @param n a positive integer
    * @return 1 + 2 + \cdots + n
    */
   public int sum(int n) {
      /* body */
   }

   I. return n + sum(n - 1);
   II. if (n == 1)
      return 1;
      else
      return n + sum(n - 1);
   III. if (n == 1)
      return 1;
      else
      return sum(n) + sum(n - 1);

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) I, II, and III
3. Refer to the method `stringRecur`:

```java
public void stringRecur(String s)
{
    if (s.length() < 15)
    {
        System.out.println(s);
        stringRecur(s + "*");
    }
}
```

When will method `stringRecur` terminate without error?
(A) Only when the length of the input string is less than 15
(B) Only when the length of the input string is greater than or equal to 15
(C) Only when an empty string is input
(D) For all string inputs
(E) For no string inputs

4. Refer to method `strRecur`:

```java
public void strRecur(String s)
{
    if (s.length() < 15)
    {
        System.out.println(s);
        strRecur(s + "*");
    }
}
```

When will method `strRecur` terminate without error?
(A) Only when the length of the input string is less than 15
(B) Only when the length of the input string is greater than or equal to 15
(C) Only when an empty string is input
(D) For all string inputs
(E) For no string inputs

Questions 5 and 6 refer to method `result`:

```java
public int result(int n)
{
    if (n == 1)
        return 2;
    else
        return 2 * result(n - 1);
}
```

5. What value does `result(5)` return?
(A) 64
(B) 32
(C) 16
(D) 8
(E) 2
6. If \( n > 0 \), how many times will \( \text{result} \) be called to evaluate \( \text{result}(n) \) (including the initial call)?
   (A) 2  
   (B) \( 2^n \)  
   (C) \( n \)  
   (D) \( 2n \)  
   (E) \( n^2 \)

7. Refer to method \( \text{mystery} \):

   ```java
   public int mystery(int n, int a, int d)
   {
       if (n == 1)
           return a;
       else
           return d + mystery(n - 1, a, d);
   }
   ```

   What value is returned by the call \( \text{mystery}(3, 2, 6) \)?
   (A) 20  
   (B) 14  
   (C) 10  
   (D) 8  
   (E) 2

8. Refer to method \( f \):

   ```java
   public int f(int k, int n)
   {
       if (n == k)
           return k;
       else
           if (n > k)
               return f(k, n - k);
           else
               return f(k - n, n);
   }
   ```

   What value is returned by the call \( f(6, 8) \)?
   (A) 8  
   (B) 4  
   (C) 3  
   (D) 2  
   (E) 1
9. What does method `recur` do?

```java
/** @param x an array of n integers
 * @param n a positive integer */
public int recur(int[] x, int n)
{
    int t;
    if (n == 1)
        return x[0];
    else
    {
        t = recur(x, n - 1);
        if (x[n-1] > t)
            return x[n-1];
        else
            return t;
    }
}
```

(A) It finds the largest value in `x` and leaves `x` unchanged.
(B) It finds the smallest value in `x` and leaves `x` unchanged.
(C) It sorts `x` in ascending order and returns the largest value in `x`.
(D) It sorts `x` in descending order and returns the largest value in `x`.
(E) It returns `x[0]` or `x[n-1]`, whichever is larger.

10. Which best describes what the `printString` method below does?

```java
public void printString(String s)
{
    if (s.length() > 0)
    {
        printString(s.substring(1));
        System.out.print(s.substring(0, 1));
    }
}
```

(A) It prints string `s`.
(B) It prints string `s` in reverse order.
(C) It prints only the first character of string `s`.
(D) It prints only the first two characters of string `s`.
(E) It prints only the last character of string `s`.
11. Refer to the method `power`:

```java
/** @param base a nonzero real number
 * @param expo an integer
 * @return base raised to the expo power */
public double power(double base, int expo)
{
    if (expo == 0)
        return 1;
    else if (expo > 0)
        return base * power(base, expo - 1);
    else
        return /* code */;
}
```

Which /* code */ correctly completes method `power`?
(Recall that \(a^{-n} = 1/a^n, a \neq 0\); for example, \(2^{-3} = 1/2^3 = 1/8\).)
(A) \((1 / base) * power(base, expo + 1)\)
(B) \((1 / base) * power(base, expo - 1)\)
(C) \(base * power(base, expo + 1)\)
(D) \(base * power(base, expo - 1)\)
(E) \((1 / base) * power(base, expo)\)

12. Consider the following method:

```java
public void doSomething(int n)
{
    if (n > 0)
    {
        doSomething(n - 1);
        System.out.print(n);
        doSomething(n - 1);
    }
}
```

What would be output following the call `doSomething(3)`?
(A) 3211211
(B) 1121213
(C) 1213121
(D) 1211213
(E) 1123211
13. A user enters several positive integers at the keyboard and terminates the list with
a sentinel (-999). A writeEven method reads those integers and outputs the even
integers only, in the reverse order that they are read. Thus, if the user enters

3 5 14 6 1 8 -999

the output for the writeEven method will be

8 6 14

Assume that the user enters at least one positive integer and terminates the list
with -999. Here is the method:

```java
/**
 * Postcondition: All even integers in the list are output in
 * reverse order.
 */
public static void writeEven()
{
    int num = IO.readInt(); //read user input
    if (num != -999)
    {
        /* code */
    }
}
```

Which /* code */ satisfies the postcondition of method writeEven?

I if (num % 2 == 0)
    System.out.print(num + " ");
    writeEven();

II if (num % 2 == 0)
    writeEven();
    System.out.print(num + " ");

III writeEven();
    if (num % 2 == 0)
        System.out.print(num + " ");

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
Chapter 7  Recursion

14. Refer to the following recursive method.

```java
public int mystery(int n)
{
    if (n < 0)
        return 2;
    else
        return mystery(n - 1) + mystery(n - 3);
}
```

What value is returned by the call `mystery(3)`?

(A) 12  
(B) 10  
(C) 8   
(D) 6   
(E) 4
Questions 15 and 16 refer to method t:

```java
/** @param n a positive integer */
public int t(int n)
{
    if (n == 1 || n == 2)
        return 2 * n;
    else
        return t(n - 1) - t(n - 2);
}
```

15. What will be returned by t(5)?

- (A) 4
- (B) 2
- (C) 0
- (D) -2
- (E) -4

16. For the method call t(6), how many calls to t will be made, including the original call?

- (A) 6
- (B) 7
- (C) 11
- (D) 15
- (E) 25

17. This question refers to methods f1 and f2 that are in the same class:

```java
public int f1(int a, int b)
{
    if (a == b)
        return b;
    else
        return a + f2(a - 1, b);
}

public int f2(int p, int q)
{
    if (p < q)
        return p + q;
    else
        return p + f1(p - 2, q);
}
```

What value will be returned by a call to f1(5, 3)?

- (A) 5
- (B) 6
- (C) 7
- (D) 12
- (E) 15
18. Consider method `foo`:

```java
public int foo(int x)
{
    if (x == 1 || x == 3)
        return x;
    else
        return x * foo(x - 1);
}
```

Assuming no possibility of integer overflow, what will be the value of `z` after execution of the following statement?

```
int z = foo(foo(3) + foo(4));
```

(A) \((15!)/(2!)\)
(B) \(3! + 4!\)
(C) \((7!)\)
(D) \((3! + 4)!\)
(E) 15

Questions 19 and 20 refer to the `IntFormatter` class below.

```java
public class IntFormatter {
    /** Write 3 digits adjacent to each other. */
    public static void writeThreeDigits(int n) {
        System.out.print(n / 100);
        System.out.print((n / 10) % 10);
        System.out.print(n % 10);
    }

    /** Insert commas in n, every 3 digits starting at the right. */
    public static void writeWithCommas(int n) {
        if (n < 1000)
            System.out.print(n);
        else {
            writeThreeDigits(n % 1000);
            System.out.print(",");
            writeWithCommas(n / 1000);
        }
    }
}
```
19. The method writeWithCommas is supposed to print its nonnegative int argument with commas properly inserted (every three digits, starting at the right). For example, the integer 27048621 should be printed as 27,048,621. Method writeWithCommas does not always work as intended, however. Assuming no integer overflow, which of the following integer arguments will not be printed correctly?

(A) 896  
(B) 251462251  
(C) 365051  
(D) 278278  
(E) 4

20. Which change in the code of the given methods will cause method writeWithCommas to work as intended?

(A) Interchange the lines System.out.print(n / 100) and System.out.print(n % 10) in method writeThreeDigits.

(B) Interchange the lines writeThreeDigits(n % 1000) and writeWithCommas(n / 1000) in method writeWithCommas.

(C) Change the test in writeWithCommas to if (n > 1000).

(D) In the method writeWithCommas, change the line writeThreeDigits(n % 1000) to writeThreeDigits(n / 1000).

(E) In the method writeWithCommas, change the recursive call writeWithCommas(n / 1000) to writeWithCommas(n % 1000).
21. Consider the following method:

```java
public static void sketch(int x1, int y1, int x2, int y2, int n)
{
    if (n <= 0)
        drawLine(x1, y1, x2, y2);
    else
    {
        int xm = (x1 + x2 + y1 - y2) / 2;
        int ym = (y1 + y2 + x2 - x1) / 2;
        sketch(x1, y1, xm, ym, n - 1);
        sketch(xm, ym, x2, y2, n - 1);
    }
}
```

Assume that the screen looks like a Cartesian coordinate system with the origin at the center, and that `drawLine` connects `(x1,y1)` to `(x2,y2)`. Assume also that `x1`, `y1`, `x2`, and `y2` are never too large or too small to cause errors. Which picture best represents the sketch drawn by the method call

```
sketch(a, 0, -a, 0, 2)
```

where `a` is a positive integer?

(A) ![Diagram A]

(B) ![Diagram B]

(C) ![Diagram C]

(D) ![Diagram D]

(E) ![Diagram E]
### ANSWER KEY

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### ANSWERS EXPLAINED

1. **(D)** Tail recursion is when the recursive call of a method is made as the last executable step of the method. Divide-and-conquer algorithms like those used in mergesort or quicksort have recursive calls before the last step. Thus, statement II is false.

2. **(B)** Code segment I is wrong because there is no base case. Code segment III is wrong because, besides anything else, `sum(n)` prevents the method from terminating—the base case `n == 1` will not be reached.

3. **(E)** When `stringRecur` is invoked, it calls itself irrespective of the length of `s`. Since there is no action that leads to termination, the method will not terminate until the computer runs out of memory (run-time error).

4. **(D)** The base case is `s.length() >= 15`. Since `s` gets longer on each method call, the method will eventually terminate. If the original length of `s` is `>= 16`, the method will terminate without output on the first call.

5. **(B)** Letting `R` denote the method `result`, we have

   \[
   R(5) = 2 \times R(4) \\
   = 2 \times (2 \times (R(3))) \\
   = \ldots \\
   = 2 \times (2 \times (2 \times (R(1)))) \\
   = 2^5 \\
   = 32
   \]

6. **(C)** For `result(n)` there will be `(n - 1)` recursive calls before `result(1)`, the base case, is reached. Adding the initial call gives a total of `n` method calls.

7. **(B)** This method returns the `n`th term of an arithmetic sequence with first term `a` and common difference `d`. Letting `M` denote method `mystery`, we have

   \[
   M(3, 2, 6) = 6 + M(2, 2, 6) \\
   = 6 + (6 + M(1, 2, 6)) \quad \text{(base case)} \\
   = 6 + 6 + 2 \\
   = 14
   \]
8. (D) Here are the recursive calls that are made, in order: \( f(6,8) \to f(6,2) \to f(4,2) \to f(2,2) \), base case. Thus, 2 is returned.

9. (A) If there is only one element in \( x \), then \( \text{recur} \) returns that element. Having the recursive call at the beginning of the \( \text{else} \) part of the algorithm causes the \( \text{if} \) part for each method call to be stacked until \( t \) eventually gets assigned to \( x[0] \). The pending \( \text{if} \) statements are then executed, and \( t \) is compared to each element in \( x \). The largest value in \( x \) is returned.

10. (B) Since the recursive call is made directly following the base case, the \( \text{System.out.print...} \) statements are stacked up. If \( \text{printString("cat")} \) is called, here is the sequence of recursive calls and pending statements on the stack:

```
printString("at") \to print "c"       print "t"
printString("t") \to print "a"       print "a"
printString(""") \to print "t"       print "c"
```

Execution stack

When \( \text{printString(""}) \), the base case, is called, the print statements are then popped off the stack in reverse order, which means that the characters of the string will be printed in reverse order.

11. (A) The required code is for a negative \( \text{expo} \). For example, \( \text{power}(2, -3) \) should return \( 2^{-3} = 1/8 \). Notice that

\[
\begin{align*}
2^{-3} &= \frac{1}{2} (2^{-2}) \\
2^{-2} &= \frac{1}{2} (2^{-1}) \\
2^{-1} &= \frac{1}{2} (2^0)
\end{align*}
\]

In general:

\[ 2^n = \frac{1}{2} (2^{n+1}) \quad \text{whenever} \quad n < 0 \]

This is equivalent to \( (1 \div \text{base}) \times \text{power(base, expo + 1)} \).

12. (C) Each box in the diagram below represents a recursive call to \( \text{doSomething} \). The numbers to the right of the boxes show the order of execution of the statements. Let \( D \) denote \( \text{doSomething} \).

![Diagram with recursive calls and execution order](image)
The numbers in each box refer to that method call only. D(0) is the base case, so the statement immediately following it is executed next. When all statements in a given box (method call) have been executed, backtrack along the arrow to find the statement that gets executed next. The circled numbers represent the statements that produce output. Following them in order, statements 4, 6, 9, 11, 15, 17, and 20 produce the output in choice C.

13. (C) Since even numbers are printed before the recursive call in segment I, they will be printed in the order in which they are read from the keyboard. Contrast this with the correct choice, segment III, in which the recursive call is made before the test for evenness. These tests will be stacked until the last number is read. Recall that the pending statements are removed from the stack in reverse order (most recent recursive call first), which leads to even numbers being printed in reverse order. Segment II is wrong because all numbers entered will be printed, irrespective of whether they are even or not. Note that segment II would work if the input list contained only even numbers.

14. (A) Let mystery(3) be denoted m(3). Picture the execution of the method as follows:

```
   m(3)
  /    \  
 m(2)   m(0)
 / \  /  \  
m(1) m(-1) m(-1) m(-3)
 / \  /  \  /  
m(0) m(-2) m(-2) m(-3)
 /  
m(-1) m(-3)
```

The base cases are shaded. Note that each of the six base case calls returns 2, resulting in a total of 12.

15. (E) The method generates a sequence. The first two terms, t(1) and t(2), are 2 and 4. Each subsequent term is generated by subtracting the previous two terms. This is the sequence: 2, 4, 2, -2, -4, -2, 2, 4, ... Thus, t(5) = -4. Alternatively,

\[
t(5) = t(4) - t(3) = [t(3) - t(2)] - t(3) = -t(2) = -4
\]

16. (D) 15. Count them! (Note that you stop at t(2) since it’s a base case.)
17. (E) This is an example of mutual recursion, where two methods call each other.

\[
f_1(5,3) = 5 + f_2(4,3) \\
= 5 + (4 + f_1(2,3)) \\
= 5 + (4 + (2 + f_2(1,3))) \\
= 5 + (4 + (2 + 4)) \\
= 15
\]

Note that \(f_2(1,3)\) is a base case.

18. (A) \(\text{foo}(3) = 3\) (This is a base case). Also, \(\text{foo}(4) = 4 \times \text{foo}(3) = 12\). So you need to find \(\text{foo}(\text{foo}(3) + \text{foo}(4)) = \text{foo}(15)\).

\[
\text{foo}(15) = 15 \times \text{foo}(14) \\
= 15 \times (14 \times \text{foo}(13)) \\
= \cdots \\
= 15 \times 14 \times \cdots \times 4 \times \text{foo}(3) \\
= 15 \times 14 \times \cdots \times 4 \times 3 \\
= (15)!(/2)
\]

19. (C) Suppose that \(n = 365051\). The method call \(\text{writeWithCommas}(365051)\) will write 051 and then execute the call \(\text{writeWithCommas}(365)\). This is a base case, so 365 will be written out, resulting in 051,365. A number like 278278 (two sets of three identical digits) will be written out correctly, as will a “symmetrical” number like 251462251. Also, any \(n < 1000\) is a base case and the number will be written out correctly as is.

20. (B) The cause of the problem is that the numbers are being written out with the sets of three digits in the wrong order. The problem is fixed by interchanging \(\text{writeThreeDigits}(n \% 1000)\) and \(\text{writeWithCommas}(n / 1000)\). For example, here is the order of execution for \(\text{writeWithCommas}(365051)\).

\[
\text{writeWithCommas}(365) \rightarrow \text{Base case. Writes 365} \\
\text{System.out.print(","); } \rightarrow 365, \\
\text{writeThreeDigits(051)} \rightarrow 365,051 \text{ which is correct}
\]

21. (B) Here is the “box diagram” for the recursive method calls, showing the order of execution of statements. Notice that the circled statements are the base case calls, the only statements that actually draw a line. Note also that the first time you reach a base case (see circled statement 6), you can get the answer: The picture in choice B is the only one that has a line segment joining \((a,0)\) to \((a,-a)\).
Critics search for ages for the wrong word, which, to give them credit, they eventually find.
—Peter Ustinov (1952)

Chapter Goals

- Java implementation of sorting algorithms
- Selection and insertion sorts
- Recursive sorts: mergesort and quicksort
- Sequential search and binary search

In each of the following sorting algorithms, assume that an array of \( n \) elements, \( a[0], a[1], \ldots, a[n-1] \), is to be sorted in ascending order.

**SORTS: SELECTION AND INSERTION SORTS**

**Selection Sort**

This is a “search-and-swap” algorithm. Here’s how it works.

Find the smallest element in the array and exchange it with \( a[0] \), the first element. Now find the smallest element in the subarray \( a[1] \ldots a[n-1] \) and swap it with \( a[1] \), the second element in the array. Continue this process until just the last two elements remain to be sorted, \( a[n-2] \) and \( a[n-1] \). The smaller of these two elements is placed in \( a[n-2] \); the larger, in \( a[n-1] \); and the sort is complete.

Trace these steps with a small array of four elements. The unshaded part is the subarray still to be searched.

\[
\begin{array}{cccc}
8 & 1 & 4 & 6 \\
1 & 8 & 4 & 6 & \text{after first pass} \\
1 & 4 & 8 & 6 & \text{after second pass} \\
1 & 4 & 6 & 8 & \text{after third pass}
\end{array}
\]
NOTE

1. For an array of \( n \) elements, the array is sorted after \( n - 1 \) passes.
2. After the \( k \)th pass, the first \( k \) elements are in their final sorted position.

Insertion Sort

Think of the first element in the array, \( a[0] \), as being sorted with respect to itself. The array can now be thought of as consisting of two parts, a sorted list followed by an unsorted list. The idea of insertion sort is to move elements from the unsorted list to the sorted list one at a time; as each item is moved, it is inserted into its correct position in the sorted list. In order to place the new item, some elements may need to be moved down to create a slot.

Here is the array of four elements. In each case, the boxed element is “it,” the next element to be inserted into the sorted part of the list. The shaded area is the part of the list sorted so far.

\[

data = [8, 1, 4, 6]  
\]

1. After first pass
2. After second pass
3. After third pass

NOTE

1. For an array of \( n \) elements, the array is sorted after \( n - 1 \) passes.
2. After the \( k \)th pass, \( a[0], a[1], \ldots, a[k] \) are sorted with respect to each other but not necessarily in their final sorted positions.
3. The worst case for insertion sort occurs if the array is initially sorted in reverse order, since this will lead to the maximum possible number of comparisons and moves.
4. The best case for insertion sort occurs if the array is already sorted in increasing order. In this case, each pass through the array will involve just one comparison, which will indicate that “it” is in its correct position with respect to the sorted list. Therefore, no elements will need to be moved.

Recursive Sorts: Mergesort and Quicksort

Selection and insertion sorts are inefficient for large \( n \), requiring approximately \( n \) passes through a list of \( n \) elements. More efficient algorithms can be devised using a “divide-and-conquer” approach, which is used in both the sorting algorithms that follow.

Mergesort

Here is a recursive description of how mergesort works:
If there is more than one element in the array
Break the array into two halves.
Mergesort the left half.
Mergesort the right half.
Merge the two subarrays into a sorted array.

Mergesort uses a merge method to merge two sorted pieces of an array into a single sorted array. For example, suppose array \( a[0] \ldots a[n-1] \) is such that \( a[0] \ldots a[k] \) is sorted and \( a[k+1] \ldots a[n-1] \) is sorted, both parts in increasing order. Example:

<p>| | | | | | |</p>
<table>
<thead>
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<td></td>
</tr>
<tr>
<td>2</td>
<td>5</td>
<td>8</td>
<td>9</td>
<td>1</td>
<td>6</td>
</tr>
</tbody>
</table>

In this case, \( a[0] \ldots a[3] \) and \( a[4] \ldots a[5] \) are the two sorted pieces. The method call \( \text{merge}(a, 0, 3, 5) \) should produce the “merged” array:

<p>| | | | | | |</p>
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<tr>
<td>1</td>
<td>2</td>
<td>5</td>
<td>6</td>
<td>8</td>
<td>9</td>
</tr>
</tbody>
</table>

The middle numerical parameter in \( \text{merge} \) (the 3 in this case) represents the index of the last element in the first “piece” of the array. The first and third numerical parameters are the lowest and highest index, respectively, of array \( a \).

Here’s what happens in mergesort:

1. Start with an unsorted list of \( n \) elements.
2. The recursive calls break the list into \( n \) sublists, each of length 1. Note that these \( n \) arrays, each containing just one element, are sorted!
3. Recursively merge adjacent pairs of lists. There are then approximately \( n/2 \) lists of length 2; then, approximately \( n/4 \) lists of approximate length 4, and so on, until there is just one list of length \( n \).

An example of mergesort follows:

Break list into \( n \) sublists of length 1

\[
\begin{array}{cccccc}
5 & -3 & 2 & 4 & 0 & 6 \\
5 & -3 & 2 & 4 & 0 & 6 \\
5 & -3 & 2 & 4 & 0 & 6 \\
-3 & 5 & 2 & 0 & 4 & 6 \\
-3 & 2 & 5 & 0 & 4 & 6 \\
-3 & 0 & 2 & 4 & 5 & 6 \\
\end{array}
\]

Merge adjacent pairs of lists

\[
\begin{array}{cccccc}
5 & -3 & 2 & 4 & 0 & 6 \\
5 & -3 & 2 & 4 & 0 & 6 \\
5 & -3 & 2 & 4 & 0 & 6 \\
-3 & 5 & 2 & 0 & 4 & 6 \\
-3 & 2 & 5 & 0 & 4 & 6 \\
-3 & 0 & 2 & 4 & 5 & 6 \\
\end{array}
\]
Analysis of Mergesort:

1. The major disadvantage of mergesort is that it needs a temporary array that is as large as the original array to be sorted. This could be a problem if space is a factor.
2. Mergesort is not affected by the initial ordering of the elements. Thus, best, worst, and average cases have similar run times.

Quicksort

For large $n$, quicksort is, on average, the fastest known sorting algorithm. Here is a recursive description of how quicksort works:

If there are at least two elements in the array

- Partition the array.
- Quicksort the left subarray.
- Quicksort the right subarray.

The partition method splits the array into two subarrays as follows: a pivot element is chosen at random from the array (often just the first element) and placed so that all items to the left of the pivot are less than or equal to the pivot, whereas those to the right are greater than or equal to it.

For example, if the array is 4, 1, 2, 7, 5, -1, 8, 0, 6, and $a[0] = 4$ is the pivot, the partition method produces

$$-1 \ 1 \ 2 \ 0 \ 4 \ 5 \ 8 \ 7 \ 6$$

Here’s how the partitioning works: Let $a[0]$, 4 in this case, be the pivot. Markers up and down are initialized to index values 0 and $n - 1$, as shown. Move the up marker until a value less than the pivot is found, or down equals up. Move the down marker until a value greater than the pivot is found, or down equals up. Swap $a[up]$ and $a[down]$. Continue the process until down equals up. This is the pivot position. Swap $a[0]$ and $a[pivotPosition]$.

Notice that the pivot element, 4, is in its final sorted position.

Analysis of Quicksort:

1. For the fastest run time, the array should be partitioned into two parts of roughly the same size.
2. If the pivot happens to be the smallest or largest element in the array, the split is not much of a split—one of the subarrays is empty! If this happens repeatedly, quicksort degenerates into a slow, recursive version of selection sort and is very inefficient.

3. The worst case for quicksort occurs when the partitioning algorithm repeatedly divides the array into pieces of size 1 and \( n - 1 \). An example is when the array is initially sorted in either order and the first or last element is chosen as the pivot. Some algorithms avoid this situation by initially shuffling up the given array (!) or selecting the pivot by examining several elements of the array (such as first, middle, and last) and then taking the median.

NOTE
For both quicksort and mergesort, when a subarray gets down to some small size \( m \), it becomes faster to sort by straight insertion. The optimal value of \( m \) is machine-dependent, but it’s approximately equal to 7.

SORTING ALGORITHMS IN JAVA

Unlike the container classes like ArrayList, whose elements must be objects, arrays can hold either objects or primitive types like int or double.

A common way of organizing code for sorting arrays is to create a sorter class with an array private instance variable. The class holds all the methods for a given type of sorting algorithm, and the constructor assigns the user’s array to the private array variable.

Example
Selection sort for an array of int.

```java
/* A class that sorts an array of ints from largest to smallest using selection sort. */

public class SelectionSort {
    private int[] a;

    public SelectionSort(int[] arr) {
        a = arr;
    }

    /** Swap a[i] and a[j] in array a.
     * @param i an index for array a
     * @param j an index for array a
     */
    private void swap(int i, int j) {
        int temp = a[i];
        a[i] = a[j];
        a[j] = temp;
    }
}
```
/** Sort array a from largest to smallest using selection sort.
 *    Precondition: a is an array of ints.
 */
public void selectionSort()
{
    int maxPos, max;

    for (int i = 0; i < a.length - 1; i++)
    {
        //find max element in a[i+1] to a[a.length-1]
        max = a[i];
        maxPos = i;
        for (int j = i + 1; j < a.length; j++)
            if (max < a[j])
            {
                max = a[j];
                maxPos = j;
            }
        swap(i, maxPos); //swap a[i] and a[maxPos]
    }
}

Note that in order to sort objects, there must be a compareTo method in the class, since you need to be able to compare elements.

**SEQUENTIAL SEARCH**

Assume that you are searching for a key in a list of $n$ elements. A sequential search starts at the first element and compares the key to each element in turn until the key is found or there are no more elements to examine in the list. If the list is sorted, in ascending order, say, stop searching as soon as the key is less than the current list element.

Analysis:

1. The best case has key in the first slot.
2. The worst case occurs if the key is in the last slot or not in the list. In the worst case, all $n$ elements must be examined.
3. On average, there will be $n/2$ comparisons.

**BINARY SEARCH**

If the elements are in a sorted array, a divide-and-conquer approach provides a much more efficient searching algorithm. The following recursive pseudo-code algorithm shows how the binary search works.

Assume that $a[low] \ldots a[high]$ is sorted in ascending order and that a method binSearch returns the index of key. If key is not in the array, it returns $-1$. 

`Binary search works only if the array is sorted on the search key.`
if (low > high)  //Base case. No elements left in array.
    return -1;
else
{
    mid = (low + high)/2;
    if (key is equal to a[mid])  //found the key
        return mid;
    else if (key is less than a[mid])  //key in left half of array
        binSearch for key in a[low] to a[mid-1] >
    else  //key in right half of array
        binSearch for key in a[mid+1] to a[high] >
}

NOTE
When low and high cross, there are no more elements to examine, and key is not in the array.

Example: suppose 5 is the key to be found in the following array:

\[
\begin{array}{cccccccc}
\text{a[0]} & \text{a[1]} & \text{a[2]} & \text{a[3]} & \text{a[4]} & \text{a[5]} & \text{a[6]} & \text{a[7]} & \text{a[8]} \\
1 & 4 & 5 & \ldots & 7 & 9 & 12 & 15 & 20 \ldots 21
\end{array}
\]

First pass:  mid = (8+0)/2 = 4.  Check a[4].
Second pass: mid = (0+3)/2 = 1.  Check a[1].
Third pass:  mid = (2+3)/2 = 2.  Check a[2].  Yes! Key is found.

Analysis of Binary Search:

1. In the best case, the key is found on the first try (i.e., (low + high)/2 is the index of key).
2. In the worst case, the key is not in the list or is at either end of a sublist. Here the \( n \) elements must be divided by 2 until there is just one element, and then that last element must be tested. An easy way to find the number of comparisons in the worst case is to round \( n \) up to the next power of 2 and take the exponent. For example, in the array above, \( n = 9 \). Suppose 21 were the key. Round 9 up to 16, which equals \( 2^4 \). Thus you would need four comparisons to find it. Try it!

Chapter Summary

You should not memorize any sorting code. You must, however, be familiar with the mechanism used in each of the sorting algorithms. For example, you should be able to explain how the merge method of Mergesort works, or how many elements are in their final sorted position after a certain number of passes through the Selection sort loop. You should know the best and worst case situations for each of the sorting algorithms.

Be familiar with the sequential and binary search algorithms. You should know that a binary search is more efficient than a sequential search, and that a binary search can only be used for an array that is sorted on the search key.
MULTIPLE-CHOICE QUESTIONS ON SORTING AND SEARCHING

1. The decision to choose a particular sorting algorithm should be made based on

   I Run-time efficiency of the sort
   II Size of the array
   III Space efficiency of the algorithm

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) I, II, and III

2. The following code fragment does a sequential search to determine whether a given integer, value, is stored in an array a[0] ... a[n-1].

   ```
   int i = 0;
   while (/* boolean expression */) {
       i++;
       if (i == n)
           return -1;  // value not found
       else
           return i;  // value found at location i
   }
   ```

   Which of the following should replace /* boolean expression */ so that the algorithm works as intended?
   (A) value != a[i]
   (B) i < n && value == a[i]
   (C) value != a[i] && i < n
   (D) i < n && value != a[i]
   (E) i < n || value != a[i]

3. A feature of data that is used for a binary search but not necessarily used for a sequential search is

   (A) length of list.
   (B) type of data.
   (C) order of data.
   (D) smallest value in the list.
   (E) median value of the data.
4. Array `unsortedArr` contains an unsorted list of integers. Array `sortedArr` contains a sorted list of integers. Which of the following operations is more efficient for `sortedArr` than `unsortedArr`? Assume the most efficient algorithms are used.

I Inserting a new element  
II Searching for a given element  
III Computing the mean of the elements

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) I, II, and III

5. An algorithm for searching a large sorted array for a specific value `x` compares every third item in the array to `x` until it finds one that is greater than or equal to `x`. When a larger value is found, the algorithm compares `x` to the previous two items. If the array is sorted in increasing order, which of the following describes all cases when this algorithm uses fewer comparisons to find `x` than would a binary search?

(A) It will never use fewer comparisons.  
(B) When `x` is in the middle position of the array  
(C) When `x` is very close to the beginning of the array  
(D) When `x` is very close to the end of the array  
(E) When `x` is not in the array

6. Assume that `a[0] ... a[N-1]` is an array of `N` positive integers and that the following assertion is true:

\[ a[0] > a[k] \] for all `k` such that `0 < k < N`

Which of the following must be true?

(A) The array is sorted in ascending order.  
(B) The array is sorted in descending order.  
(C) All values in the array are different.  
(D) `a[0]` holds the smallest value in the array.  
(E) `a[0]` holds the largest value in the array.

7. The following code is designed to set `index` to the location of the first occurrence of `key` in array `a` and to set `index` to −1 if `key` is not in `a`.

```c
index = 0;
while (a[index] != key)
    index++;
if (a[index] != key)
    index = -1;
```

In which case will this program definitely fail to perform the task described?

(A) When `key` is the first element of the array  
(B) When `key` is the last element of the array  
(C) When `key` is not in the array  
(D) When `key` equals 0  
(E) When `key` equals `a[key]`
8. Consider the following class.

```java
/** A class that sorts an array of Integer objects from largest to smallest using a selection sort. */
public class Sorter {
    private Integer[] a;

    public Sorter(Integer[] arr) {
        a = arr;
    }

    /** Swap a[i] and a[j] in array a. */
    private void swap(int i, int j) {
        /* implementation not shown */
    }

    /** Sort array a from largest to smallest using selection sort. */
    public void selectionSort() {
        for (int i = 0; i < a.length - 1; i++) {
            //find max element in a[i+1] to a[n-1]
            Integer max = a[i];
            int maxPos = i;
            for (int j = i + 1; j < a.length; j++)
                if (max.compareTo(a[j]) < 0) //max less than a[j]
                    { max = a[j]; maxPos = j; }
            swap(i, maxPos); //swap a[i] and a[maxPos]
        }
    }
}
```

If an array of Integer contains the following elements, what would the array look like after the third pass of selectionSort, sorting from high to low?

89 42 −3 13 109 70 2

(A) 109 89 70 13 42 −3 2
(B) 109 89 70 42 13 2 −3
(C) 109 89 70 −3 2 13 42
(D) 89 42 13 −3 109 70 2
(E) 109 89 42 −3 13 70 2
Chapter 8  Sorting and Searching

9. Refer to method search.

```java
/** @param v an initialized array of integers
 * @param key the value to be found
 * Postcondition:
 * - Returned value k is such that -1 <= k <= v.length-1.
 * - If k >= 0 then v[k] == key.
 * - If k == -1, then key != any of the elements in v.
 */
public static int search(int[] v, int key)
{
    int index = 0;
    while (index < v.length && v[index] < key)
        index++;
    if (v[index] == key)
        return index;
    else
        return -1;
}
```

Assuming that the method works as intended, which of the following should be added to the precondition of search?

(A) v is sorted smallest to largest.
(B) v is sorted largest to smallest.
(C) v is unsorted.
(D) There is at least one occurrence of key in v.
(E) key occurs no more than once in v.

Questions 10–14 are based on the binSearch method and the private instance variable a for some class:

```java
private int[] a;

/** Does binary search for key in array a[0]...a[a.length-1],
 * sorted in ascending order.
 * @param key the integer value to be found
 * Postcondition:
 * - index has been returned such that a[index]==key.
 * - If key not in a, return -1.
 */
public int binSearch(int key)
{
    int low = 0;
    int high = a.length - 1;
    while (low <= high)
    {
        int mid = (low + high) / 2;
        if (a[mid] == key)
            return mid;
        else if (a[mid] < key)
            low = mid + 1;
        else
            high = mid - 1;
    }
    return -1;
}
```
A binary search will be performed on the following list.

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<thead>
<tr>
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</thead>
<tbody>
<tr>
<td>4</td>
<td>7</td>
<td>9</td>
<td>11</td>
<td>20</td>
<td>24</td>
<td>30</td>
<td>41</td>
</tr>
</tbody>
</table>

10. To find the key value 27, the search interval after the first pass through the while loop will be
   (A) a[0] ... a[7]
   (B) a[5] ... a[6]
   (C) a[4] ... a[7]
   (D) a[2] ... a[6]
   (E) a[6] ... a[7]

11. How many iterations will be required to determine that 27 is not in the list?
   (A) 1
   (B) 3
   (C) 8
   (D) 27
   (E) An infinite loop since 27 is not found

12. What will be stored in y after executing the following?
   ```cpp
   int y = binSearch(4);
   ```
   (A) 20
   (B) 7
   (C) 4
   (D) 0
   (E) -1

13. If the test for the while loop is changed to
   ```cpp
   while (low < high)
   ```
   the binSearch method does not work as intended. Which value in the given list will not be found?
   (A) 4
   (B) 7
   (C) 11
   (D) 24
   (E) 30

14. For binSearch, which of the following assertions will be true following every iteration of the while loop?
   (A) key = a[mid] or key is not in a.
   (B) a[low] ≤ key ≤ a[high]
   (C) low ≤ mid ≤ high
   (D) key = a[mid], or a[low] ≤ key ≤ a[high]
   (E) key = a[mid], or a[low] ≤ key ≤ a[high], or key is not in array a.
15. A large sorted array containing about 30,000 elements is to be searched for a value key using an iterative binary search algorithm. Assuming that key is in the array, which of the following is closest to the smallest number of iterations that will guarantee that key is found? Note: \(10^3 \approx 2^{10}\).

(A) 15  
(B) 30  
(C) 100  
(D) 300  
(E) 3000

For Questions 16–19 refer to the `insertionSort` method and the private instance variable `a`, both in a `Sorter` class.

```java
private Integer[] a;

/**
 * Precondition: a[0], a[1]...a[a.length-1] is an unsorted array of Integer objects.
 * Postcondition: Array a is sorted in descending order.
 */
public void insertionSort()
{
    for (int i = 1; i < a.length; i++)
    {
        Integer temp = a[i];
        int j = i - 1;
        while (j >= 0 && temp.compareTo(a[j]) > 0)
        {
            a[j+1] = a[j];
            j--;
        }
        a[j+1] = temp;
    }
}
```

16. An array of `Integer` is to be sorted biggest to smallest using the `insertionSort` method. If the array originally contains

\[
1 \ 7 \ 9 \ 5 \ 4 \ 12
\]

what will it look like after the third pass of the `for` loop?

(A) 9 7 1 5 4 12  
(B) 9 7 5 1 4 12  
(C) 12 9 7 1 5 4  
(D) 12 9 7 5 4 1  
(E) 9 7 12 5 4 1

17. When sorted biggest to smallest with `insertionSort`, which list will need the fewest changes of position for individual elements?

(A) 5, 1, 2, 3, 4, 9  
(B) 9, 5, 1, 4, 3, 2  
(C) 9, 4, 2, 5, 1, 3  
(D) 9, 3, 5, 1, 4, 2  
(E) 3, 2, 1, 9, 5, 4
18. When sorted biggest to smallest with insertionSort, which list will need the greatest number of changes in position?
   (A) 5, 1, 2, 3, 4, 7, 6, 9
   (B) 9, 5, 1, 4, 3, 2, 1, 0
   (C) 9, 4, 6, 2, 1, 5, 1, 3
   (D) 9, 6, 9, 5, 6, 7, 2, 0
   (E) 3, 2, 1, 0, 9, 6, 5, 4

19. While typing the insertionSort method, a programmer by mistake enters

   while (temp.compareTo( a[j]) > 0)

   instead of

   while (j >= 0 && temp.compareTo( a[j]) > 0)

Despite this mistake, the method works as intended the first time the programmer enters an array to be sorted in descending order. Which of the following could explain this?

   I The first element in the array was the largest element in the array.
   II The array was already sorted in descending order.
   III The first element was less than or equal to all the other elements in the array.

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) II and III only
Chapter 8  Sorting and Searching

20. The elements in a long list of integers are roughly sorted in decreasing order. No more than 5 percent of the elements are out of order. Which of the following is a valid reason for using an insertion sort rather than a selection sort to sort this list into decreasing order?

I  There will be fewer comparisons of elements for insertion sort.
II  There will be fewer changes of position of elements for insertion sort.
III  There will be less space required for insertion sort.

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III

Optional topic

21. The code shown sorts array a[0] . . . a[a.length-1] in descending order.

```java
public static void sort(String[] a)
{
    for (int i = 0; i < a.length - 1; i++)
        for (int j = 0; j < a.length - i - 1; j++)
            if (a[j].compareTo(a[j+1]) < 0)
                swap(a, j, j+1);       //swap a[j] and a[j+1]
}
```

This is an example of

(A) selection sort.
(B) insertion sort.
(C) mergesort.
(D) quicksort.
(E) none of the above.

22. Which of the following is a valid reason why mergesort is a better sorting algorithm than insertion sort for sorting long, randomly ordered lists?

I  Mergesort requires less code than insertion sort.
II  Mergesort requires less storage space than insertion sort.
III  Mergesort runs faster than insertion sort.

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) II and III only

23. A large array of lowercase characters is to be searched for the pattern “pqrs.” The first step in a very efficient searching algorithm is to look at characters with index

(A) 0, 1, 2, . . . until a “p” is encountered.
(B) 0, 1, 2, . . . until any letter in “p” . . . “s” is encountered.
(C) 3, 7, 11, . . . until an “s” is encountered.
(D) 3, 7, 11, . . . until any letter in “p” . . . “s” is encountered.
(E) 3, 7, 11, . . . until any letter other than “p” . . . “s” is encountered.
24. The array \texttt{names[0], names[1], \ldots, names[9999]} is a list of 10,000 name strings. The list is to be searched to determine the location of some name \( X \) in the list. Which of the following preconditions is necessary for a binary search? 
(A) There are no duplicate names in the list. 
(B) The number of names \( N \) in the list is large. 
(C) The list is in alphabetical order. 
(D) Name \( X \) is definitely in the list. 
(E) Name \( X \) occurs near the middle of the list.

25. Consider the following method:

\begin{verbatim}
 /** Precondition: a[0],a[1]...a[n-1] contain integers. */
 public static int someMethod(int[] a, int n, int value)
 {
     if (n == 0)
         return -1;
     else
     {
         if (a[n-1] == value)
             return n - 1;
         else
             return someMethod(a, n - 1, value);
     }
 }
\end{verbatim}

The method shown is an example of
(A) insertion sort. 
(B) mergesort. 
(C) selection sort. 
(D) binary search. 
(E) sequential search.

26. The \texttt{partition} method for quicksort partitions a list as follows:
(i) A pivot element is selected from the array. 
(ii) The elements of the list are rearranged such that all elements to the left of the pivot are less than or equal to it; all elements to the right of the pivot are greater than or equal to it.

Partitioning the array requires which of the following? 
(A) A recursive algorithm 
(B) A temporary array 
(C) An external file for the array 
(D) A swap algorithm for interchanging array elements 
(E) A merge method for merging two sorted lists

27. Assume that mergesort will be used to sort an array \texttt{arr} of \( n \) integers into increasing order. What is the purpose of the \texttt{merge} method in the mergesort algorithm? 
(A) Partition \texttt{arr} into two parts of roughly equal length, then merge these parts. 
(B) Use a recursive algorithm to sort \texttt{arr} into increasing order. 
(C) Divide \texttt{arr} into \( n \) subarrays, each with one element. 
(D) Merge two sorted parts of \texttt{arr} into a single sorted array. 
(E) Merge two sorted arrays into a temporary array that is sorted.
28. A binary search is to be performed on an array with 600 elements. In the worst case, which of the following best approximates the number of iterations of the algorithm?
   (A) 6
   (B) 10
   (C) 100
   (D) 300
   (E) 600

29. A worst case situation for insertion sort would be
   I A list in correct sorted order.
   II A list sorted in reverse order.
   III A list in random order.
   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) II and III only
30. Consider a binary search algorithm to search an ordered list of numbers. Which of the following choices is closest to the maximum number of times that such an algorithm will execute its main comparison loop when searching a list of 1 million numbers?

(A) 6
(B) 20
(C) 100
(D) 120
(E) 1000

31. Consider these three tasks:

I A sequential search of an array of \( n \) names
II A binary search of an array of \( n \) names in alphabetical order
III An insertion sort into alphabetical order of an array of \( n \) names that are initially in random order

For large \( n \), which of the following lists these tasks in order (from least to greatest) of their average case run times?

(A) II I III
(B) I II III
(C) II III I
(D) III I II
(E) III II I
Questions 32 and 33 are based on the Sort interface and MergeSort and QuickSort classes shown below.

```java
public interface Sort {
    void sort();
}

public class MergeSort implements Sort {
    private String[] a;

    public MergeSort(String[] arr) {
        a = arr;
    }

    /** Merge a[lb] to a[mi] and a[mi+1] to a[ub].
     * Precondition: a[lb] to a[mi] and a[mi+1] to a[ub] both sorted
     * in increasing order.
     */
    private void merge(int lb, int mi, int ub) {
        /* Implementation not shown. */
    }

    /** Sort a[first]..a[last] in increasing order using mergesort.
     * Precondition: a is an array of String objects.
     */
    private void sort(int first, int last) {
        int mid;

        if (first != last) {
            mid = (first + last) / 2;
            sort(first, mid);
            sort(mid + 1, last);
            merge(first, mid, last);
        }
    }

    /** Sort array a from smallest to largest using mergesort.
     * Precondition: a is an array of String objects.
     */
    public void sort() {
        sort(0, a.length - 1);
    }
}
```
Multiple-Choice Questions on Sorting and Searching

32. Notice that the MergeSort and QuickSort classes both have a private helper method that implements the recursive sort routine. For this example, which of the following is a valid reason for having a helper method?

I The helper method hides the implementation details of the sorting algorithm from the user.
II A method with additional parameters is needed to implement the recursion.
III Providing a helper method increases the run-time efficiency of the sorting algorithm.

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
33. A piece of code to test the `QuickSort` and `MergeSort` classes is as follows:

```java
//Create an array of String values
String[] strArray = makeArray(strList);
writeList(strArray);
/ * more code */
```

where `makeArray` creates an array of `String` from a list `strList`. Which of the following replacements for `/* more code */` is reasonable code to test `QuickSort` and `MergeSort`? You can assume `writeList` correctly writes out an array of `String`.

(A) `Sort q = new QuickSort(strArray);`  
   `Sort m = new MergeSort(strArray);`  
   `q.sort();`  
   `writeList(strArray);`  
   `m.sort();`  
   `writeList(strArray);`

(B) `QuickSort q = new Sort(strArray);`  
    `MergeSort m = new Sort(strArray);`  
    `q.sort();`  
    `writeList(strArray);`  
    `m.sort();`  
    `writeList(strArray);`

(C) `Sort q = new QuickSort(strArray);`  
   `Sort m = new MergeSort(strArray);`  
   `String[] copyArray = makeArray(strList);`  
   `q.sort(0, strArray.length - 1);`  
   `writeList(strArray);`  
   `m.sort(0, copyArray.length - 1);`  
   `writeList(copyArray);`

(D) `QuickSort q = new Sort(strArray);`  
    `String[] copyArray = makeArray(strList);`  
    `MergeSort m = new Sort(strArray);`  
    `q.sort();`  
    `writeList(strArray);`  
    `m.sort();`  
    `writeList(copyArray);`

(E) `Sort q = new QuickSort(strArray);`  
    `String[] copyArray = makeArray(strList);`  
    `Sort m = new MergeSort(copyArray);`  
    `q.sort();`  
    `writeList(strArray);`  
    `m.sort();`  
    `writeList(copyArray);`
Questions 34–36 refer to the Hi-Lo game described below.

Consider the problem of writing a Hi-Lo game in which a user thinks of an integer from 1 to 100 inclusive and the computer tries to guess that number. Each time the computer makes a guess, the user makes one of three responses:

- “lower” (i.e., the number is lower than the computer’s guess)
- “higher” (i.e., the number is higher than the computer’s guess)
- “you got it in <however many> tries!”

34. Suppose the game is programmed so that the computer uses a binary search strategy for making its guesses. What is the maximum number of guesses the computer could make before guessing the user’s number?
   (A) 50
   (B) 25
   (C) 10
   (D) 7
   (E) 6

35. Suppose the computer used a sequential search strategy for guessing the user’s number. What is the maximum number of guesses the computer could make before guessing the user’s number?
   (A) 100
   (B) 99
   (C) 50
   (D) 25
   (E) 10

36. Using a sequential search strategy, how many guesses on average would the computer need to guess the number?
   (A) 100
   (B) 51
   (C) 50
   (D) 25
   (E) Fewer than 25
ANSWER KEY

8. A 20. A 32. D
10. C 22. C 34. D
11. B 23. D 35. A

ANSWERS EXPLAINED

1. (E) The time and space requirements of sorting algorithms are affected by all three of the given factors, so all must be considered when choosing a particular sorting algorithm.

2. (D) Choice B doesn’t make sense: The loop will be exited as soon as a value is found that does not equal a[i]. Eliminate choice A because, if value is not in the array, a[i] will eventually go out of bounds. You need the i < n part of the boolean expression to avoid this. The test i < n, however, must precede value != a[i] so that if i < n fails, the expression will be evaluated as false, the test will be short-circuited, and an out-of-range error will be avoided. Choice C does not avoid this error. Choice E is wrong because both parts of the expression must be true in order to continue the search.

3. (C) The binary search algorithm depends on the array being sorted. Sequential search has no ordering requirement. Both depend on choice A, the length of the list, while the other choices are irrelevant to both algorithms.

4. (B) Inserting a new element is quick and easy in an unsorted array—just add it to the end of the list. Computing the mean involves finding the sum of the elements and dividing by n, the number of elements. The execution time is the same whether the list is sorted or not. Operation II, searching, is inefficient for an unsorted list, since a sequential search must be used. In sortedArr, the efficient binary search algorithm, which involves fewer comparisons, could be used. In fact, in a sorted list, even a sequential search would be more efficient than for an unsorted list: If the search item were not in the list, the search could stop as soon as the list elements were greater than the search item.

5. (C) Suppose the array has 1000 elements and x is somewhere in the first 8 slots. The algorithm described will find x using no more than five comparisons. A binary search, by contrast, will chop the array in half and do a comparison six
times before examining elements in the first 15 slots of the array (array size after each chop: 500, 250, 125, 62, 31, 15).

6. (E) The assertion states that the first element is greater than all the other elements in the array. This eliminates choices A and D. Choices B and C are incorrect because you have no information about the relative sizes of elements $a[1] \ldots a[n-1]$.

7. (C) When key is not in the array, index will eventually be large enough that $a[index]$ will cause an ArrayIndexOutOfBoundsException. In choices A and B, the algorithm will find key without error. Choice D won't fail if 0 is in the array. Choice E will work if $a[key]$ is not out of range.

8. (A)

| After 1st pass: | 109 | 42 | -3 | 13 | 89 | 70 | 2 |
| After 2nd pass: | 109 | 89 | -3 | 13 | 42 | 70 | 2 |
| After 3rd pass: | 109 | 89 | 70 | 13 | 42 | -3 | 2 |

9. (A) The algorithm uses the fact that array $v$ is sorted smallest to largest. The while loop terminates—which means that the search stops—as soon as $v[index] \geq key$.

10. (C) The first pass uses the interval $a[0] \ldots a[7]$. Since $mid = (0 + 7)/2 = 3$, low gets adjusted to $mid + 1 = 4$, and the second pass uses the interval $a[4] \ldots a[7]$.

11. (B) First pass: compare 27 with $a[3]$, since $low = 0$ high = 7 $mid = (0 + 7)/2 = 3$. Second pass: compare 27 with $a[5]$, since $low = 4$ high = 7 $mid = (4 + 7)/2 = 5$. Third pass: compare 27 with $a[6]$, since $low = 6$ high = 7 $mid = (6 + 7)/2 = 6$. The fourth pass doesn't happen, since $low = 6$, high = 5, and therefore the test ($low \leq high$) fails. Here's the general rule for finding the number of iterations when key is not in the list: If $n$ is the number of elements, round $n$ up to the nearest power of 2, which is 8 in this case. $8 = 2^3$, which implies 3 iterations of the “divide-and-compare” loop.

12. (D) The method returns the index of the key parameter, 4. Since $a[0]$ contains 4, $binSearch(4)$ will return 0.

13. (A) Try 4. Here are the values for low, high, and mid when searching for 4:

| First pass: | low = 0, high = 7, mid = 3 |
| Second pass: | low = 0, high = 2, mid = 1 |

After this pass, high gets adjusted to mid - 1, which is 0. Now low equals high, and the test for the while loop fails. The method returns -1, indicating that 4 wasn’t found.

14. (E) When the loop is exited, either key = $a[mid]$ (and mid has been returned) or key has not been found, in which case either $a[low] \leq key \leq a[high]$ or key is not in the array. The correct assertion must account for all three possibilities.

15. (A) $30,000 = 1000 \times 30 \approx 2^{10} \times 2^5 = 2^{15}$. Since a successful binary search in the worst case requires $\log_2 n$ iterations, 15 iterations will guarantee that key is found. (Note that $30,000 < 2^{10} \times 2^5 = 32,768$.)

16. (B) Start with the second element in the array.
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17. (B) An insertion sort compares a[1] and a[0]. If they are not in the correct order, a[0] is moved and a[1] is inserted in its correct position. a[2] is then inserted in its correct position, and a[0] and a[1] are moved if necessary, and so on. Since B has only one element out of order, it will require the fewest changes.

18. (A) This list is almost sorted in reverse order, which is the worst case for insertion sort, requiring the greatest number of comparisons and moves.

19. (D) \( j \geq 0 \) is a stopping condition that prevents an element that is larger than all those to the left of it from going off the left end of the array. If no error occurred, it means that the largest element in the array was a[0], which was true in situations I and II. Omitting the \( j \geq 0 \) test will cause a run-time (out-of-range) error whenever temp is bigger than all elements to the left of it (i.e., the insertion point is 0).

20. (A) Look at a small array that is almost sorted:

\[
10 \ 8 \ 9 \ 6 \ 2
\]

For insertion sort you need four passes through this array.

For the first pass compares 8 and 10—one comparison, no moves.

For the second pass compares 9 and 8, then 9 and 10. The array becomes

\[
10 \ 9 \ 8 \ 6 \ 2
\]

two comparisons, two moves.

For the third and fourth passes compare 6 and 8, and 2 and 6—no moves.

In summary, there are approximately one or two comparisons per pass and no more than two moves per pass.

For selection sort, there are four passes too.

The first pass finds the biggest element in the array and swaps it into the first position.

The array is still \( 10 \ 8 \ 9 \ 6 \ 2 \)—four comparisons. There are two moves if your algorithm makes the swap in this case, otherwise no moves.

The second pass finds the biggest element from a[1] to a[4] and swaps it into the second position: \( 10 \ 9 \ 8 \ 6 \ 2 \)—three comparisons, two moves.

For the third pass there are two comparisons, and one for the fourth. There are zero or two moves each time.

Summary: \( 4 + 3 + 2 + 1 \) total comparisons and a possible two moves per pass.

Notice that reason I is valid. Selection sort makes the same number of comparisons irrespective of the state of the array. Insertion sort does far fewer comparisons if the array is almost sorted. Reason II is invalid. There are roughly the same number of data movements for insertion and selection. Insertion may even have more changes, depending on how far from their insertion points the unsorted elements are. Reason III is wrong because insertion and selection sorts have the same space requirements.

21. (E) In the first pass through the outer for loop, the smallest element makes its way to the end of the array. In the second pass, the next smallest element moves to the second last slot, and so on. This is different from the sorts in choices A through D; in fact, it is a bubble sort.

22. (C) Reject reason I. Mergesort requires both a merge and a mergeSort method—
more code than the relatively short and simple code for insertion sort. Reject reason II. The merge algorithm uses a temporary array, which means more storage space than insertion sort. Reason III is correct. For long lists, the “divide-and-conquer” approach of mergesort gives it a faster run time than insertion sort.

23. (D) Since the search is for a four-letter sequence, the idea in this algorithm is that if you examine every fourth slot, you'll find a letter in the required sequence very quickly. When you find one of these letters, you can then examine adjacent slots to check if you have the required sequence. This method will, on average, result in fewer comparisons than the strictly sequential search algorithm in choice A. Choice B is wrong. If you encounter a “q,” “r,” or “s” without a “p” first, you can’t have found “pqrs.” Choice C is wrong because you may miss the sequence completely. Choice E doesn’t make sense.

24. (C) The main precondition for a binary search is that the list is ordered.

25. (E) This algorithm is just a recursive implementation of a sequential search. It starts by testing if the last element in the array, \( a[n-1] \), is equal to value. If so, it returns the index \( n - 1 \). Otherwise, it calls itself with \( n \) replaced by \( n - 1 \). The net effect is that it examines \( a[n-1], a[n-2], \ldots \). The base case, \( \text{if } (n == 0) \), occurs when there are no elements left to examine. In this case, the method returns \(-1\), signifying that value was not in the array.

26. (D) The partition algorithm performs a series of swaps until the pivot element is swapped into its final sorted position (see p. 327). No temporary arrays or external files are used, nor is a recursive algorithm invoked. The merge method is used for mergesort, not quicksort.

27. (D) Recall the mergesort algorithm:

   Divide arr into two parts.
   Mergesort the left side.
   Mergesort the right side.
   Merge the two sides into a single sorted array.

   The merge method is used for the last step of the algorithm. It does not do any sorting or partitioning of the array, which eliminates choices A, B, and C. Choice E is wrong because merge starts with a single array that has two sorted parts.

28. (B) Round 600 up to the next power of 2, which is 1024 = \( 2^{10} \). For the worst case, the array will be split in half \( \log_{2} 1024 = 10 \) times.

29. (B) If the list is sorted in reverse order, each pass through the array will involve the maximum possible number of comparisons and the maximum possible number of element movements if an insertion sort is used.

30. (B) 1 million = \( 10^6 = (10^3)^2 \approx (2^{10})^2 = 2^{20} \). Thus, there will be on the order of 20 comparisons.

31. (A) A binary search, on average, has a smaller run time than a sequential search. All of the sorting algorithms have greater run times than a sequential search. This is because a sequential search looks at each element once. A sorting algorithm, however, processes other elements in the array for each element it looks at.

32. (D) Reason I is valid—it’s always desirable to hide implementation details from users of a method. Reason II is valid too—since QuickSort and MergeSort implement the Sort interface, they must have a sort method with no parameters. But parameters are needed to make the recursion work. Therefore each sort requires
a helper method with parameters. Reason III is invalid in this particular example of helper methods. There are many examples in which a helper method enhances efficiency (e.g., Example 2 on p. 296), but the sort example is not one of them.

33. (E) Since Sort is an interface, you can’t create an instance of it. This eliminates choices B and D. The sort methods alter the contents of strArray. Thus invoking q.sort() followed by m.sort() means that sort will always operate on a sorted array, assuming quicksort works correctly! In order to test both quicksort and mergesort on unsorted arrays, you need to make a copy of the original array or create a different array. Eliminate choice A (and B again!), which does neither of these. Choice C is wrong because it calls the private sort methods of the classes. The Sort interface has just a single public method, sort, with no arguments. The two classes shown must provide an implementation for this sort method, and it is this method that must be invoked in the client program.

34. (D) The computer should find the number in no more than seven tries. This is because the guessing interval is halved on each successive try:

1. $100 \div 2 = 50$ numbers left to try
2. $50 \div 2 = 25$ numbers left to try
3. $25 \div 2 = 13$ numbers left to try
4. $13 \div 2 = 7$ numbers left to try
5. $7 \div 2 = 4$ numbers left to try
6. $4 \div 2 = 2$ numbers left to try
7. $2 \div 2 = 1$ number left to try

Seven iterations of the loop leaves just 1 number left to try!

35. (A) The maximum number of guesses is 100. A sequential search means that the computer starts at the first possible number, namely 1, and tries each successive number until it gets to 100. If the user’s number is 100, the computer will take 100 guesses to reach it.

36. (C) On average the computer will make 50 guesses. The user is equally likely to pick any number between 1 and 100. Half the time it will be less than 50; half the time, greater than 50. So on the average, the distance of the number from 1 is 50.
The AP Computer Science A Labs

I don’t like museums, I like labs.
—Amit Kalantri

Chapter Goals

- The Magpie Lab
- The Elevens Lab
- The Picture Lab

The AP Computer Science A labs were developed as a replacement for the GridWorld case study. Starting in May 2015, there will be no exam questions on GridWorld. And there will be no specific questions that require knowledge of the content of the labs. Instead, new test questions will focus on concepts from the AP Java subset that are emphasized in the labs.

What follows below is a brief summary of the labs, the concepts they illustrate, the concepts they particularly emphasize, and some sample multiple-choice questions based on these concepts.

THE MAGPIE LAB

In this lab, students modify a chatbot, which is a computer program designed to simulate an intelligent conversation between a computer and a human user. Students enter phrases, the computer searches for keywords, then comes up with an intelligent-seeming response.

Student activities include:

- Working through the Magpie code (if statements)
- Using Magpie and String methods (while loops, strings, and Javadoc)
- Using an array of possible responses in generating a random response from the computer (arrays, ArrayLists, and random integers)
- Improving the search to find keywords that are complete words, not substrings buried in other strings (String methods)
- Transforming a computer response based on the format of the statement entered by the user (String methods)
Special Emphasis

STRING METHODS

The String methods substring and indexOf are used continually in this lab. Be sure that you recall:

- The first index of a String is 0.
- The method call s.substring(start, end) returns the substring of s starting at index start but ending at index end-1.
- The method call s.indexOf(sub) returns the index of the first occurrence of sub in s.
- s.indexOf(sub) returns -1 if sub is not in s.

You should be nimble and well practiced in processing strings.

The following type of code is used repeatedly in the lab to look for multiple occurrences of a substring in a given string:

```java
int pos = s.indexOf(someSubstring);
while (pos >= 0) {
    doSomething();
    s = s.substring(pos + 1); // throw away all characters of s
    pos = s.indexOf(someSubstring); // Is there another occurrence
    // of someSubstring?
}
```

A modified version of the above code, using some combination of a loop, indexOf, and substring, can be used to

- count number of occurrences of substring in str.
- replace all occurrences of substring in str with replacementStr.
- remove all occurrences of substring in str.

On the AP exam, there will almost certainly be at least one free-response question that requires you to manipulate strings in this way.

RANDOM ELEMENT SELECTION

Another skill that is demonstrated in this lab is returning a random element from an array or ArrayList. For example, suppose responses is an ArrayList<String> of surprised responses the computer may make to a user's crazy input. If the contents of responses are currently

<table>
<thead>
<tr>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Oh my!</td>
<td>Say what?</td>
<td>No!</td>
<td>Heavens!</td>
<td>You're kidding me.</td>
<td>Jumping Jellybeans!</td>
</tr>
</tbody>
</table>

You should be able to randomly return one of these responses. The key is to select a random index from 0 to 5, inclusive, and then return the string in the responses list that is at that index.

Recall that the expression (int)(Math.random() * howMany) generates a random int in the range 0...howMany-1. In the given example, howMany is 6. The piece of code that returns a random response is:
int randIndex = (int) (Math.random() * 6);
String response = responses.get(randIndex);

CONDITIONALS: if...else STATEMENT

The Magpie lab is loaded with conditionals, searching for keywords that will trigger different responses from the chatbot (computer). Using if and if...else should be second nature to you.

Example
The user will enter a sentence and the chatbot will produce a chatBotReply.

```java
if (sentence.indexOf("love") != -1)
{
    if (sentence.indexOf("you") != -1)
        chatBotReply = "I'm in heaven!";
    else
        chatBotReply = "But do you love me?";
} else
    chatBotReply = "My heart is in pieces on the floor.";
```

Here are some possible sentences that the user may enter, with the corresponding chatBoxReply:

<table>
<thead>
<tr>
<th>Sentence</th>
<th>chatBoxReply</th>
</tr>
</thead>
<tbody>
<tr>
<td>I love chocolate cake.</td>
<td>But do you love me?</td>
</tr>
<tr>
<td>I love chocolate cake; do you?</td>
<td>I'm in heaven.</td>
</tr>
<tr>
<td>I hate fudge.</td>
<td>My heart is in pieces on the floor.</td>
</tr>
</tbody>
</table>

If the substring "love" isn't in the sentence, the opening test will be false, and execution skips to the else outside the braces, producing the chatBotReply "My heart is in pieces on the floor". If sentence contains both "love" and "you", the first test in the braces will be true, and the chatBotReply will be "I'm in heaven!" The middle response "But do you love me?" will be triggered by a sentence that contains "love" but doesn't contain "you", causing the first test in the braces to be false, and the else part in the braces to be executed.

THE ELEVEN'S LAB

In this lab, students simulate a game of solitaire, Elevens, and a related game, Thirteens. A GUI is provided for the labs to make the game interesting and fun to play. You are not required to know about GUIs.

Student activities include:

- Creating a Card class (objects, classes, and Strings)
- Creating a Deck class (arrays, ArrayLists, conditionals, loops)
- Shuffling the deck (Math.random, list manipulation)
- Writing an ElevensBoard class, using an abstract Board class (inheritance, abstract classes)
- Testing and debugging
- Playing the game
Special Emphasis

SHUFFLING

Several different algorithms are discussed for shuffling an array of elements. A key ingredient of a good shuffle is generation of random integers. For example, to shuffle a deck of 52 cards in an array may require a random int from 0 to 51:

```java
int cardNum = (int) (Math.random() * 52);
```

(Recall that the multiplier in parentheses is the number of possible random integers.)

The following code for shuffling an array of Type elements is used often:

```java
for(int k = arr.length - 1; k > 0; k++)
{
    //Pick a random index in the array from 0 to k
    int index = (int) (Math.random() * (k + 1));
    //Swap randomly selected element with element at position k
    Type temp = arr[k];
    arr[k] = arr[index];
    arr[index] = temp;
}
```

WRITING SUBCLASSES

On the AP exam, you will probably be asked to write a subclass of a given class. Don't forget the extends keyword:

```java
public class Subclass extends Superclass
```

Recall that constructors are not inherited, and if you use the keyword super in writing a constructor for your subclass, the line containing it should precede any other code in the constructor.

Example

```java
public class Dog
{
    private String name;
    private String breed;

    public Dog (String aName, String aBreed)
    {
        name = aName;
        breed = aBreed;
    }
    ...
}

public class Poodle extends Dog
{
    private boolean needsGrooming;

    public Poodle (String aName, String aBreed, boolean grooming)
    {
        super(aName, aBreed);
        needsGrooming = grooming;
    }
    ...
}
```
In the Elevens lab there’s extensive discussion about using an abstract class, `Board`, to represent a game board on which the game of Elevens will be played.

The advantage of the abstract class is that its use can be extended for other solitaire games played on similar boards. In the Elevens lab, the subclass `ElevensBoard` is written, which is specific to the game of Elevens. Further on in the lab, another subclass `ThirteensBoard` is discussed, which applies to a different, but similar game, Thirteens.

The abstract `Board` class contains methods that are common to all games that would be played on a `Board`, like `deal`. But methods that would pertain to moves on the board, like `isLegal`, would be different for each of the specific games. These methods are therefore declared `abstract` in the superclass, but are overridden in the subclasses.

Note: If you’re writing a concrete (nonabstract) subclass of an abstract superclass, you must be sure to write an implementation for every abstract method of the superclass.

**POLYMORPHISM**

Consider this hierarchy of classes, and the declarations that follow it:

```
Dog <<<abstract>>>
    /   /
  Poodle  Pitbull  Dachshund

Suppose the `Dog` class has this method:

```java
public abstract void eat();
```

And each of the subclasses, Poodle, PitBull, Dachshund, etc., has a different, overridden `eat` method. Now suppose that `allDogs` is an `ArrayList<Dog>` where each `Dog` declared above has been added to the list. Each `Dog` in the list will be processed to eat by the following lines of code:

```java
for (Dog d: allDogs)
    d.eat();
```

Polymorphism is the process of selecting the correct `eat` method, during run time, for each of the different dogs.

**TESTING AND DEBUGGING**

In the Elevens lab, a lot of emphasis is placed on testing and debugging code as you write it. Here are some general principles:

- Start simple. For example, if writing a `Deck` class, start with a deck that contains just 2 or 3 cards.
- Always have a driver class (one with a `main` method) to test the current class you’re writing.
- In your class, start with a constructor. You want to be sure you can create your object.
- After the constructor, write a `toString` method for clear and easy display. You want to be able to “see“ the results of running your code.
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SIMULATING RANDOM EVENTS
Flipping a coin, tossing a die, or picking a random card from a deck. Those random numbers again! If there are $k$ possible outcomes, each of them equally likely, be sure you can generate a random int from 0 to $k-1$.

THE PICTURE LAB
In this lab, students manipulate digital pictures using two-dimensional arrays. Code for the GUI is provided in the lab.
The main concept emphasized is traversal of two-dimensional arrays. Other concepts used are UML diagrams, binary numbers, inheritance, interfaces, abstract methods, constants, and program analysis.
Student activities include:

- Learning how colors are stored in a program.
- Modifying a picture.
- Creating a mirror image of a picture.
- Mirroring part of a picture.
- Creating a collage.
- Detecting the edge of a picture.

Special Emphasis

PROCESSING A 2-D ARRAY
A matrix is stored as an array of rows, each of which is also an array. In the lab, a for-each loop is often used for traversal. Here is an example that traverses an array of int:

```java
for (int[] row : matrix) // for each row array in the matrix
for (int num : row) // for each int element in the current row
    doSomething();
```

Here is what doSomething can do:

- Access each element in the matrix (count, add, compare, etc.)

Here is what doSomething cannot do:

- Replace an element with another.

Suppose the matrix is an array of objects that can be changed with mutator methods. The for-each loop can be used not only to access elements, but also to modify them. (No replacing with new elements, however). The following code is OK:

```java
for (Clock[] row : clockMatrix)
    for (Clock c : row)
        c.setTime(t);
```
MIRROR IMAGES

A large part of the lab is spent coming up with algorithms that create some kind of mirror image of a matrix. Students are asked to reflect across mirrors placed somewhere in the center of the matrix, horizontally, vertically, or diagonally.

Note that if a vertical mirror is placed down the center of a matrix, so that all elements to the left of the mirror are reflected across it, the element mat[row][col] reflects across to element mat[row][numCols-col-1].

You should teach yourself to trace the following type of code:

```java
public static void matrixMethod(int[][] mat)
{
    int height = mat.length;
    int numCols = mat[0].length;
    for (int col = 0; col < numCols; col++)
        for (int row = 0; row < height/2; row++)
            mat[height - row - 1][col] = mat[row][col];
}
```

What does it do? How does it transform the matrix below?

```
2 3 4
5 6 7
8 9 0
1 1 1
```

Solution: The algorithm reflects the matrix from top to bottom across a horizontal mirror placed at its center.

height = 4, numCols = 3
col takes on values 0, 1, and 2
row takes on values 0 and 1

Here are the replacements that are made:

- col = 0, row = 0: mat[3][0] = mat[0][0]
- row = 1: mat[2][0] = mat[1][0]
- row = 1: mat[2][1] = mat[1][1]
- row = 1: mat[2][2] = mat[1][2]

This transforms the matrix into

```
2 3 4
5 6 7
5 6 7
2 3 4
```

Note that a for-each loop was not used in the traversal, because elements in the matrix are being replaced.

BASE 2, BASE 8, BASE 16

Binary (base 2) and hexadecimal (base 16) numbers are discussed in the Picture lab as they apply to storage of colors. You need to be able to convert a given number in base $b$ to a decimal (base 10) number (see p. 62).
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Example
Convert the following octal (base 8) number to a decimal number: \(123_{\text{oct}}\)
Solution:
\[
123_{\text{oct}} = (1)(8^2) + (2)(8^1) + (3)(8^0) = 64 + 16 + 3 = 83_{\text{dec}}
\]

For a base 16 conversion, you’ll be given that A, B, C, D, E, and F represent 10, 11, 12, 13, 14, and 15, respectively.

Example
Convert \(A2B_{\text{hex}}\) to a decimal number.
Solution:
\[
A2B_{\text{hex}} = (A)(16^2) + (2)(16^1) + (B)(16^0) = 2560 + 32 + 11 = 2603_{\text{dec}}
\]

Can you go in the other direction, namely, start with a decimal number and convert it to a different base?

Example
Convert 25 to a binary (base 2) number.
Solution:
Pull out the highest power of 2 less than or equal to 25, which is 16. Thus,
\[
25 = 16 + 9
\]
Now pull out the highest power of 2 less than or equal to 9, which is 8. Thus,\[
25 = 16 + 8 + 1
\]
Now write 25 as a sum of powers of 2, making sure to include the missing powers that are less than the highest power in the first step of the solution:
\[
25 = 16 + 8 + 1 = (1)(2^4) + (1)(2^3) + (0)(2^2) + (0)(2^1) + (1)(2^0)
\]
Note: you must be careful to use 0’s as place holders for the missing powers of 2.

Chapter Summary

String manipulation and matrix processing are the two big topics you should master. Review the meanings and boundary conditions of the parameters in the `String` methods `substring` and `indexOf`. For matrices, you should nail down both the row-column and for-each traversals. Remember, you cannot use a for-each loop for the replacement of elements.
Be sure you can hand-execute tricky matrix algorithms, like those used for modifying matrices using mirror images.

A matrix is an array of row-arrays, so familiarize yourself with the the use of a method with an array parameter to process the rows of a matrix.

Array manipulation is another big topic. Be sure you know how to shuffle the elements of an array.

Other concepts emphasized in the labs are inheritance and polymorphism, writing subclasses, abstract classes, simulation of events using random numbers, multi-base numbers, and conditional (if...else) statements. You should have all of these at your fingertips.
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MULTIPLE-CHOICE QUESTIONS ON THE LAB CONCEPTS

1. For ticket-selling purposes, there are three categories at a certain theater:

<table>
<thead>
<tr>
<th>Age</th>
<th>Category</th>
</tr>
</thead>
<tbody>
<tr>
<td>65 or above</td>
<td>Senior</td>
</tr>
<tr>
<td>From 18 to 64 inclusive</td>
<td>Adult</td>
</tr>
<tr>
<td>Below 18</td>
<td>Child</td>
</tr>
</tbody>
</table>

Which of the following code segments will assign the correct string to category for a given integer age?

I  if (age >= 65)
   category = "Senior";
   if (age >= 18)
     category = "Adult";
   else
     category = "Child";

II if (age >= 65)
    category = "Senior";
    if (18 <= age <= 64)
      category = "Adult";
    else
      category = "Child";

III if (age >= 65)
    category = "Senior";
    else if (age >= 18)
      category = "Adult";
    else
      category = "Child";

(A) I only  
(B) II only  
(C) III only  
(D) II and III only  
(E) I, II, and III
2. What is the output of the following code segment?

```java
String s = "How do you do?";
int index = s.indexOf("o");
while (index >= 0)
{
    System.out.print(index + " ");
    s = s.substring(index + 1);
    index = s.indexOf("o");
}
```

(A) 1 3 2 3  
(B) 2 4 3 4  
(C) 1 5 8 12  
(D) 1 5 8 11  
(E) No output because of an IndexOutOfBoundsException

3. Consider the following method `removeAll` that creates and returns a string that has stripped its input phrase of all occurrences of its single-character `String` parameter `ch`.

```java
public static String removeAll(String phrase, String ch)
{
    String str = "";
    String newPhrase = phrase;
    int pos = phrase.indexOf(ch);
    if (pos == -1)
        return phrase;
    else
    {
        while (pos >= 0)
        {
            str = str + newPhrase.substring(0, pos - 1);
            newPhrase = newPhrase.substring(pos + 1);
            pos = newPhrase.indexOf(ch);
        }
        return str;
    }
}
```

The method doesn’t work as intended. Which of the following changes to the `removeAll` method will make it work as specified?

(A) Change Line 10 to  
while (pos >= -1)

(B) Change Line 12 to  
str = str + newPhrase.substring(0, pos - 1);

(C) Change Line 13 to  
newPhrase = newPhrase.substring(pos + 1);

(D) Change Line 14 to  
pos = newPhrase.indexOf(ch);

(E) Change Line 16 to  
str = str + newPhrase.substring(pos + 1);
4. A programmer has written a program that “chats” to a human user based on statements that the human inputs. The program contains a method `findKeyWord` that searches an input statement for a given keyword. The `findKeyWord` method contains the following line of code:

```java
pos = statement.indexOf(word);
```

Suppose `pos` has a value >= 0, that is, `word` was found. The programmer now wants to test that an actual word was found, not part of another word. For example, if “cat” is the keyword, the programmer needs to check that it’s not part of “catch” or “category.” Here is the code that tests if `word` is a stand-alone word. (You may assume that `statement` is all lowercase and contains only letters and blanks.)

```java
pos = statement.indexOf(word);
//Check for first or last word
if (pos == 0 || pos + word.length() == statement.length())
{
    before = " ";
    after = " ";
}
else
{
    before = statement.substring(pos - 1, pos);
    after = statement.substring(pos + word.length(),
    pos + word.length() + 1);
    if (/* test */)
        //then a stand-alone word was found ...
    else
        //word was part of a larger word
}
```

Which replacement for /* test */ will give the desired result?

(A) `before.compareTo("a") < 0 && before.compareTo("z") > 0` ||
   `after.compareTo("a") > 0 && after.compareTo("z") < 0`

(B) `before.compareTo("a") > 0 && before.compareTo("z") < 0` ||
   `after.compareTo("a") < 0 && after.compareTo("z") > 0`

(C) `before.compareTo("a") < 0 && before.compareTo("z") > 0` ||
   `after.compareTo("a") > 0 && after.compareTo("z") < 0`

(D) `before.compareTo("a") < 0 && before.compareTo("z") > 0` &&
   `after.compareTo("a") > 0 && after.compareTo("z") < 0`

(E) `before.compareTo("a") > 0 && before.compareTo("z") < 0` &&
   `after.compareTo("a") < 0 && after.compareTo("z") > 0`
5. A program that simulates a conversation between a computer and a human user generates a random response to a user’s comment. All possible responses that the computer can generate are stored in an array of String called allResponses. The method given below, getResponse, returns a random response string from the array.

```java
/**
 * Precondition: array allResponses is initialized with strings.
 * Postcondition: returns a random response from allResponses.
 */
public String getResponse();
{
    // implementation
}
```

Which is a correct /* implementation */?

(A) `int i = (int) (Math.random() * allResponses.length);`  
    return allResponses[i];

(B) `return (String) (Math.random() * allResponses.length);`

(C) `int i = Math.random() * allResponses.length;`  
    return allResponses[i];

(D) `int i = (int) (Math.random() * (allResponses.length - 1));`  
    return allResponses[i];

(E) `return (int) (Math.random() * allResponses.length);`
Questions 6 and 7 refer to the Deck class described below.

A Deck class contains an array cards with an even number of Card values and a final variable NUMCARDS, which is an odd integer.

6. Here are two possible algorithms for shuffling the deck.

**Algorithm 1**

Initialize an array of Card called shuffled of length NUMCARDS.
Set k to 0.
For j=0 to NUMCARDS/2-1
  - Copy cards[j] to shuffled[k]
  - Set k to k+2
Set k to 1.
For j=NUMCARDS/2 to NUMCARDS-1
  - Copy cards[j] to shuffled[k]
  - Set k to k+2

**Algorithm 2**

Initialize an array of Card called shuffled containing NUMCARDS slots.
For k=0 to NUMCARDS-1
  - Repeatedly generate a random integer j from 0 to NUMCARDS-1, until cards[j] contains a card not marked as empty
  - Copy cards[j] to shuffled[k]
  - Set cards[j] to empty

Which is a false statement concerning Algorithms 1 and 2?

(A) A disadvantage of Algorithm 1 is that it won’t generate all possible deck permutations.
(B) For Algorithm 2, to determine the last element shuffled requires an average of NUMCARDS calls to the random number generator.
(C) Algorithm 2 will lead to more permutations of the deck than Algorithm 1.
(D) In terms of run time, Algorithm 2 is more efficient than Algorithm 1.
(E) If Algorithm 1 is repeated several times, it may return the deck to its original state.
Multiple-Choice Questions on the Lab Concepts

7. The following shuffle method is used to shuffle the cards in the Deck class.

Line 1: public void shuffle()
Line 2: {
Line 3:     for (int k = NUMCARDS; k > 0; k--)
Line 4:         {
Line 5:             int randPos = (int) (Math.random() * (k + 1));
Line 6:             //swap randomly selected card with card at position k
Line 7:             Card temp = cards[k];
Line 8:             cards[k] = cards[randPos];
Line 9:             cards[randPos] = temp;
Line 10:         }
Line 11: }

The method does not work as intended. Which of the following changes should be made to correct the method?
(A) Replace Line 3 with
   for (int k = NUMCARDS; k >= 0; k--)
(B) Replace Line 3 with
   for (int k = NUMCARDS - 1; k > 0; k--)
(C) Replace Line 3 with
   for (int k = 1; k <= NUMCARDS; k++)
(D) Replace Line 5 with
   int randPos = (int) (Math.random() * k);
(E) Replace Lines 7 – 9 with
   Card temp = cards[randPos];
   cards[randPos] = cards[k];
   cards[k] = temp;
8. A programmer wants to simulate several different but related solitaire games, each of which uses a standard 52-card deck. Each game starts with 10 cards dealt face up on a table. The game types differ in the rules that allow groups of cards to be discarded from the table and new cards to be dealt from the remainder of the deck. For each of the solitaire games, a winning game occurs if there are no cards left in the pile or on the table. To represent the table for the games, the programmer will use the inheritance relationship shown below.

```
Table
<<abstract>>
```

```
Game1Table
Game2Table
Game3Table
```

Which of the following methods should be abstract in the Table class?

I. dealNextCard, which provides the next card for the table

II. checkForMove, which returns true if a move is possible, false otherwise

III. isWinningGame, which returns true if both the table and deck of cards are empty

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) II and III only

Questions 9 and 10 refer to the following.

A word creation game uses letter tiles, where each tile has a letter and a point value for scoring purposes. A Tile class is used to represent a letter tile.

```java
public class Tile {
    private String letter;
    private int pointValue;

    //Constructors and other methods are not shown.
}
```
9. The Tile class contains a toString method that creates a String containing the letter and point value of a Tile. The string should be in the following format:

```
Letter letter (point value = pointValue)
```

For example,

```
Letter A (point value = 1)
Letter Z (point value = 10)
```

Consider the toString method below:

```
public String toString()
{
    return /* code */
}
```

Which /* code */ leads to correct output?
(A) `Letter + "letter " + "(point value = " + pointValue + ")";`
(B) `"Letter " + letter + " (point value = " + pointValue + ")";`
(C) `Letter + this.letter + " (point value = " + pointValue + ")";`
(D) `"Letter " + letter + " (point value = " + (String) pointValue + ")";`
(E) `"Letter " + letter + " (point value = " + pointValue + ")";`

10. Any two tiles in the word game that have the same letter also have the same point value, but the opposite is not necessarily true. For example, all the vowels have a point value of 1. Two tiles are said to match if they have the same letter. Consider the following matches method for the Tile class.

```
/** @return true if the letter on this tile equals the letter * on otherTile */
public boolean matches(Tile otherTile)
{
    return /* code */;
}
```

Which replacements for /* code */ return the desired result? Note: You may not assume that the Tile class has its own equals method.

I `letter == otherTile.letter`
II `this.equals(otherTile)`
III `letter.equals(otherTile.letter)`

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I and III only
11. Consider the following method.

```java
public static void alterArray(int[] arr)
{
    int mid = arr.length/2;
    for (int i = 0; i < mid; i++)
    {
        int temp = arr[i];
        arr[i] = arr[arr.length - i - 1];
        arr[arr.length - i - 1] = temp;
    }
}
```

If the current state of a matrix `mat` is

```
2 7 9 5
8 1 4 3
6 5 0 9
```

which matrix will result from the method call `alterArray(mat[2])`?

(A) `2 7 9 5
  3 4 1 8
  6 5 0 9`

(B) `2 7 0 5
  8 1 4 3
  6 5 9 9`

(C) `5 9 7 2
  3 4 1 8
  9 0 5 6`

(D) `2 7 9 5
  8 1 4 3
  9 0 5 6`

(E) `5 9 7 2
  8 1 4 3
  6 5 0 9`
12. Consider a program to manipulate images. The inheritance hierarchy is as follows:

![Inheritance Hierarchy Diagram]

You may assume that `Picture` has a default (no-argument) constructor, but that `Landscape` and `Portrait` do not have any constructors. Which of the following declarations will compile?

I. `DigitalPicture p = new Portrait();`
II. `Landscape p = new Picture();`
III. `DigitalPicture p = new DigitalPicture();`

(A) I only  
(B) II only  
(C) III only  
(D) II and III only  
(E) I, II, and III
13. The color of a pixel can be represented using the RGB (Red, Green, Blue) color model, which stores integer values for red, green, and blue, each ranging from 0 to 255. A value of 0 represents none of that color, while 255 represents the maximum. Consider a `Pixel` class that, among other methods, contains methods `getRed`, `getGreen`, and `getBlue`. These methods return integer values of those colors for that `Pixel`. There are also methods `setRed`, `setGreen`, and `setBlue`, which allow these values to be changed. For example, `setBlue(250)` would set the amount of blueness for that pixel to 250.

Consider a `Picture` class and a private instance variable `pixels`, where `pixels` is a two-dimensional array of `Pixel` objects. A method `removeRed` in the `Picture` class sets the red value of every pixel to zero:

```java
public void removeRed()
{
    for (int row = 0; row < numRows; row++)
        for (int col = 0; col < numCols; col++)
        {
            /* code to set red value to 0 */
        }
}
```

Which is a correct replacement for `/* code to set red value to 0 */`?

I. `Pixel p = pixels[row][col];
p.setRed(0);`
II. `pixels[row][col].setRed(0);`
III. `pixels[row][col].getRed() = 0;`

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) I, II, and III
14. Consider a class `MatrixStuff` that has a private instance variable

   ```java
   private int[][] mat;
   ```

   The following method uses a vertical mirror down the center of a matrix to reflect the left half of the matrix onto the right. The following two examples show the result of mirroring a two-dimensional array of numbers from left to right vertically. (Another way of saying this is that the right half of the matrix is replaced by a vertical mirror image of the left half.)

   **Example 1:**

<table>
<thead>
<tr>
<th>mat</th>
<th>mat after mirroring</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 2 3 4 5</td>
<td>1 2 3 2 1</td>
</tr>
<tr>
<td>6 7 8 9 10</td>
<td>6 7 8 7 6</td>
</tr>
<tr>
<td>11 12 13 14 15</td>
<td>11 12 13 12 11</td>
</tr>
</tbody>
</table>

   **Example 2:**

<table>
<thead>
<tr>
<th>mat</th>
<th>mat after mirroring</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 2 3 4</td>
<td>1 2 2 1</td>
</tr>
<tr>
<td>5 6 7 8</td>
<td>5 6 6 5</td>
</tr>
<tr>
<td>9 10 11 12</td>
<td>9 10 10 9</td>
</tr>
</tbody>
</table>

   ```java
   public static void mirrorVerticalLeftToRight(int[][] mat)
   {
       int width = mat[0].length;
       int numRows = mat.length;
       for (int row = 0; row < numRows; row++)
           for (int col = 0; col < width/2; col++)
               /* element assignments */
   }
   ```

   Which replacement for `/* element assignments */` will make the method work as intended?

   (A) `mat[row][col] = mat[row][width - col];`
   (B) `mat[row][width - col] = mat[row][col];`
   (C) `mat[row][width - 1 - col] = mat[row][col];`
   (D) `mat[row][col] = mat[row][width - 1 - col];`
   (E) `mat[row][width - 1 - col] = mat[col][row];`
15. Consider a square matrix in a class that has a private instance variable mat:

```java
private int[][] mat;
```

Method alter in the class changes mat:

```java
public void alter()
{
    for (int row = 1; row < mat.length; row++)
    for (int col = 0; col < row; col++)
        mat[col][row] = mat[row][col];
}
```

If mat has current value

```java
{{1, 2, 3},
 {4, 5, 6},
 {7, 8, 9}}
```

what are the contents of mat after method alter has been executed?

(A) {{1, 4, 7},
    {4, 5, 8},
    {7, 8, 9}}

(B) {{1, 4, 7},
    {2, 5, 8},
    {3, 6, 9}}

(C) {{1, 2, 3},
    {2, 5, 6},
    {3, 6, 9}}

(D) {{9, 6, 3},
    {8, 5, 6},
    {7, 8, 9}}

(E) {{1, 2, 3},
    {4, 5, 2},
    {7, 4, 1}}
ANSWER KEY

5. A  10. C  15. A

ANSWERS EXPLAINED

1. (C) Segment III works because if you enter an age of 90, say, category will correctly be assigned "Senior", and none of the other pieces of code will be executed. Similarly, if you enter an age corresponding to an adult or a child, only the correct assignment is made. Segment I fails because if you enter an age of 90, category will be assigned "Senior", but then will be changed to "Adult" when the age passes the second test. Segment II uses incorrect syntax. The segment will work if you change the second test to

   if (age >= 18 && age <= 64)

2. (A) The algorithm prints the current index of "o" in the string, then creates a new substring containing all remaining characters following that "o". Here is the series of substrings and the corresponding output for each (the symbol \( \_ \) denotes a blank character):

   How do you do? 1
   w do you do? 3
   o you do? 2
   u do? 3

3. (B) Here is a description of the algorithm:

   Make a copy of phrase in newPhrase.
   Find the first occurrence of ch in newPhrase (pos is the index).
   If you found it, concatenate to str the characters in newPhrase from 0 to pos-1.
   Change newPhrase to contain all characters from ch to the end, excluding ch.
   Repeat the process until there are no more occurrences of ch in newPhrase.

   So Line 12 is wrong because newPhrase.substring(0, pos-1) will not include the character at pos-1, which means that the string returned will lose a character that is not equal to ch.

4. (E) The program has found a stand-alone word if the characters before and after are both blank. Choice E tests that they are not letters between “a” and “z”, i.e., they must be blank. Choices A and B fail because you must use compareTo for inequality tests on strings. Choices C and D allow at least one of before and after to be a letter, which would mean that word was not a stand-alone word.
5. (A) The first line in choice A returns a random integer that lies between 0 and allResponses.length-1. This range corresponds to the range of the array indexes so it is correct. Choice B is garbage—you cannot cast a real number to a string. Choice C fails because Math.random() is type double and you require an int; you must do the cast to int shown in choice A. Choice D fails because the element allResponses[allResponses.length-1] will never be returned: i will contain a random int from 0 to allResponses.length-2. Choice E returns an int, not a String.

6. (D) The big defect of Algorithm 2 is that it eventually slows down. This is because every time it selects an empty element, it has to loop again. Each of the other choices is true. In choice A, for example, the element cards[0] always moves to shuffled[0], eliminating all permutations that have cards[0] in a different slot. For choice B, by the time you get to assign the last element, all but two slots of the cards array are marked empty. So, on average, you will need to go through NUMCARDS tries to find one of those two nonempty slots. For choice C, even though Algorithm 2 is slow, in theory every element in cards could land in any given slot in shuffled. This is not true for Algorithm 1, where the first element never budges out of the first slot. For choice E, because of the precise ordering of elements in Algorithm 1, the array will always eventually return to its original state, assuming there are sufficient iterations.

7. (B) If it starts with the value NUMCARDS, the method encounters cards[NUMCARDS] on Line 7 and throws an ArrayIndexOutOfBoundsException.

8. (B) Since dealNextCard and isWinningGame have the same code irrespective of which game is being played, they should be regular methods in the Table class. Method II, checkForMove, is unique to each game and therefore should be abstract in the superclass and overridden in each subclass.

9. (E) The actual letter and its point value must not be in quotes because their values must be printed. Everything else, including the parentheses, must be in quotes. (All text in quotes is printed literally, as is.) Choices A and C fail because they don’t place the opening word, letter, in quotes. Choice B doesn’t have the parentheses in quotes. Choice D incorrectly tries to cast an int to a String.

10. (C) Segment I will only be true if an object and its parameter are the same reference, which is not necessarily true for two matching tiles. Segment II fails similarly if the Tile class doesn’t have its own equals method. (The inherited method from Object compares references.)

11. (D) The matrix mat consists of an array of rows, mat[0], mat[1], mat[2], each of which is an array. The method alterArray swaps the first and last element of an array, then the second and second-last elements, and so on, until it reaches the middle of the array. The method call alterArray(mat[2]) performs this series of swaps on row 2 of the matrix, resulting in the matrix in choice D.

12. (A) Declaration I works because a Portrait is a DigitalPicture, and it will be assigned the default constructor from Picture, its superclass. Declaration II fails because a Picture is not a Landscape. Declaration III fails because you can’t create an instance of an interface.

13. (D) Segment I works because p is a reference to the element pixels[row][col]. Changing p with a mutator method will change the array. Segment II changes the two-dimensional array directly. Segment III is garbage: you cannot assign a value
through an accessor method.

14. (C) Look at Example 2 for this question:

<table>
<thead>
<tr>
<th>mat</th>
<th>mat after mirroring</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 2 3 4</td>
<td>1 2 2 1</td>
</tr>
<tr>
<td>5 6 7 8</td>
<td>5 6 6 5</td>
</tr>
<tr>
<td>9 10 11 12</td>
<td>9 10 10 9</td>
</tr>
</tbody>
</table>

Now consider one element, 12 say. It must be replaced by its vertical mirror image 9, i.e., \( \text{mat}[2][3] = \text{mat}[2][0] \). The value of width is 4. See which expression in the answer choices correctly makes this assignment. Eliminate choices A and D right away because \( \text{col} \) can only have the values 0 and 1 in this algorithm, so \( \text{mat}[2][3] \) will not be assigned. In choice B, when \( \text{col} \) has value 1, \( \text{mat}[2][3] = \text{mat}[2][1] \), an incorrect assignment. Choice C works: when \( \text{row} \) is 2 and \( \text{col} \) is 0, \( \text{mat}[2][3] = \text{mat}[2][0] \). In choice E, when \( \text{row} \) is 2 and \( \text{col} \) is 0, the assignment \( \text{mat}[2][3] = \text{mat}[0][2] \) is incorrect.

15. (A) Method alter places a mirror along the major diagonal and reflects the elements from left to right across this diagonal.

```
1 2 3
4 5 6
7 8 9
```

In this algorithm, when \( \text{row} \) is 1, \( \text{col} \) can only be 0, and when \( \text{row} \) is 2, \( \text{col} \) takes on the values 0 and 1. Thus, only 3 elements are altered: \( \text{mat}[0][1], \text{mat}[0][2], \) and \( \text{mat}[1][2] \). (Note that the method assigns values to \( \text{mat}[\text{col}][\text{row}] \).) These elements are all to the right of the diagonal. Choice A is the only choice that leaves elements to the left of the diagonal unchanged.
Practice
Exams
Answer Sheet: Practice Exam Two

1. A B C D E
2. A B C D E
3. A B C D E
4. A B C D E
5. A B C D E
6. A B C D E
7. A B C D E
8. A B C D E
9. A B C D E
10. A B C D E
11. A B C D E
12. A B C D E
13. A B C D E
14. A B C D E
15. A B C D E
16. A B C D E
17. A B C D E
18. A B C D E
19. A B C D E
20. A B C D E
21. A B C D E
22. A B C D E
23. A B C D E
24. A B C D E
25. A B C D E
26. A B C D E
27. A B C D E
28. A B C D E
29. A B C D E
30. A B C D E
31. A B C D E
32. A B C D E
33. A B C D E
34. A B C D E
35. A B C D E
36. A B C D E
37. A B C D E
38. A B C D E
39. A B C D E
40. A B C D E
How to Calculate Your (Approximate) AP Computer Science Score

Multiple Choice

Number correct (out of 40) = Multiple-Choice Score

Free Response

Question 1 (out of 9)

Question 2 (out of 9)

Question 3 (out of 9)

Question 4 (out of 9)

Total × 1.11 = Free-Response Score

Final Score

Multiple-Choice Score + Free-Response Score = Final Score

(Final Score

Chart to Convert to AP Grade

Computer Science

<table>
<thead>
<tr>
<th>Final Score Range</th>
<th>AP Grade</th>
</tr>
</thead>
<tbody>
<tr>
<td>62–80</td>
<td>5</td>
</tr>
<tr>
<td>47–61</td>
<td>4</td>
</tr>
<tr>
<td>37–46</td>
<td>3</td>
</tr>
<tr>
<td>29–36</td>
<td>2</td>
</tr>
<tr>
<td>0–28</td>
<td>1</td>
</tr>
</tbody>
</table>

*The score range corresponding to each grade varies from exam to exam and is approximate.*
Practice Exam Two

COMPUTER SCIENCE

SECTION I

Time—1 hour and 15 minutes
Number of questions—40
Percent of total grade—50

Directions: Determine the answer to each of the following questions or incomplete statements, using the available space for any necessary scratchwork. Then decide which is the best of the choices given and fill in the corresponding oval on the answer sheet. Do not spend too much time on any one problem.

Notes:
- Assume that the classes in the Quick Reference have been imported where needed.
- Assume that variables and methods are declared within the context of an enclosing class.
- Assume that method calls that have no object or class name prefixed, and that are not shown within a complete class definition, appear within the context of an enclosing class.
- Assume that parameters in method calls are not null unless otherwise stated.

1. A large Java program was tested extensively, and no errors were found. What can be concluded?
   (A) All of the preconditions in the program are correct.
   (B) All of the postconditions in the program are correct.
   (C) The program may have bugs.
   (D) The program has no bugs.
   (E) Every method in the program may safely be used in other programs.
Practice Exams

Questions 2–4 refer to the Worker class below:

```java
public class Worker {
    private String name;
    private double hourlyWage;
    private boolean isUnionMember;

    public Worker() {
        /* implementation not shown */
    }

    public Worker(String aName, double anHourlyWage, boolean union) {
        /* implementation not shown */
    }

    //Accessors getName, getHourlyWage, getUnionStatus are not shown.

    /** Permanently increase hourly wage by amt. */
    public void incrementWage(double amt) {
        /* implementation of incrementWage */
    }

    /** Switch value of isUnionMember from true to false and vice versa. */
    public void changeUnionStatus() {
        /* implementation of changeUnionStatus */
    }
}
```

2. Refer to the incrementWage method. Which of the following is a correct /* implementation of incrementWage */?

(A) return hourlyWage + amt;
(B) return getHourlyWage() + amt;
(C) hourlyWage += amt;
(D) getHourlyWage() += amt;
(E) hourlyWage = amt;

GO ON TO THE NEXT PAGE.
3. Consider the method changeUnionStatus. Which is a correct implementation of changeUnionStatus */?

   I if (isUnionMember)
       isUnionMember = false;
   else
       isUnionMember = true;
   II isUnionMember = !isUnionMember;
   III if (isUnionMember)
       isUnionMember = !isUnionMember;

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) I, II, and III  

4. A client method computePay will return a worker’s pay based on the number of hours worked.

   /** Precondition: Worker w has worked the given number of hours.  
   * @param w a Worker  
   * @param hours the number of hours worked  
   * @return amount of pay for Worker w  
   */
   public static double computePay(Worker w, double hours)
   { /* code */ }

Which replacement for /* code */ is correct?

(A) return hourlyWage * hours;
(B) return getHourlyWage() * hours;
(C) return w.getHourlyWage() * hours;
(D) return w.hourlyWage * hours;
(E) return w.getHourlyWage() * w.hours;

5. Consider this program segment. You may assume that wordList has been declared as ArrayList<String>.

   for (String s : wordList)
      if (s.length() < 4)
         System.out.println("SHORT WORD");

What is the maximum number of times that SHORT WORD can be printed?

(A) 3  
(B) 4  
(C) wordList.size()  
(D) wordList.size() - 1  
(E) s.length()
6. Refer to the following method.

```java
public static int mystery(int n)
{
    if (n == 1)
        return 3;
    else
        return 3 * mystery(n - 1);
}
```

What value does `mystery(4)` return?
(A) 3
(B) 9
(C) 12
(D) 27
(E) 81

7. Refer to the following declarations:

```java
String[] colors = {"red", "green", "black"};
List<String> colorList = new ArrayList<String>();
```

Which of the following correctly assigns the elements of the `colors` array to `colorList`? The final ordering of colors in `colorList` should be the same as in the `colors` array.

I  for (String col : colors)
    colorList.add(col);

II for (String col : colorList)
    colors.add(col);

III for (int i = colors.length - 1; i >= 0; i--)
    colorList.add(i, colors[i]);

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III
8. Often the most efficient computer algorithms use a divide-and-conquer approach, for example, one in which a list is repeatedly split into two pieces until a desired outcome is reached. Which of the following use a divide-and-conquer approach?
   I Mergesort
   II Insertion sort
   III Binary search

   (A) I only
   (B) II only
   (C) III only
   (D) I and III only
   (E) I, II, and III

9. An Insect class is to be written, containing the following data fields:
   age, which will be initialized to 0 when an Insect is constructed.
   nextAvailableID, which will be initialized to 0 outside the constructor and incremented each time an Insect is constructed.
   idNum, which will be initialized to the current value of nextAvailableID when an Insect is constructed.
   position, which will be initialized to the location in a garden where the Insect is placed when it is constructed.
   direction, which will be initialized to the direction the Insect is facing when placed in the garden.

   Which variable in the Insect class should be static?
   (A) age
   (B) nextAvailableID
   (C) idNum
   (D) position
   (E) direction
Practice Exams

Questions 10 and 11 refer to the classes Address and Customer given below.

```java
public class Address {
    private String street;
    private String city;
    private String state;
    private int zipCode;

    public Address(String aStreet, String aCity, String aState, int aZipCode) {
        // /* implementation not shown */
    }

    public String getStreet() {
        // /* implementation not shown */
    }

    public String getCity() {
        // /* implementation not shown */
    }

    public String getState() {
        // /* implementation not shown */
    }

    public int getZipCode() {
        // /* implementation not shown */
    }

    //Other methods are not shown.
}

public class Customer {
    private String name;
    private String phone;
    private Address address;
    private int ID;

    public Customer(String aName, String aPhone, Address anAddr, int anID) {
        // /* implementation not shown */
    }

    public Address getAddress() {
        // /* implementation not shown */
    }

    public String getName() {
        // /* implementation not shown */
    }

    public String getPhone() {
        // /* implementation not shown */
    }

    public int getID() {
        // /* implementation not shown */
    }

    //Other methods are not shown.
}
```

GO ON TO THE NEXT PAGE.
10. Which of the following correctly creates a Customer object c?

I  Address a = new Address("125 Bismark St", "Pleasantville", "NY", 14850);
    Customer c = new Customer("Jack Spratt", "747-1674", a, 7008);

II Customer c = new Customer("Jack Spratt", "747-1674", "125 Bismark St, Pleasantville, NY 14850", 7008);

III Customer c = new Customer("Jack Spratt", "747-1674", new Address("125 Bismark St", "Pleasantville", "NY", 14850), 7008);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only

11. Consider an AllCustomers class that has private instance variable

   private Customer[] custList;

Given the ID number of a particular customer, a method of the class, locate, must find the correct Customer record and return the name of that customer. Here is the method locate:

   /**
   * Precondition: custList contains a complete list of Customer objects.
   * @param idNum the ID number for a Customer
   * @return the name of the customer with the specified idNum
   */
   public String locate(int idNum)
   {
     for (Customer c : custList)
       if (c.getID() == idNum)
         return c.getName();
     return null;  //idNum not found
   }

A more efficient algorithm for finding the matching Customer object could be used if

(A) Customer objects were in alphabetical order by name.
(B) Customer objects were sorted by phone number.
(C) Customer objects were sorted by ID number.
(D) the custList array had fewer elements.
(E) the Customer class did not have an Address data member.
12. The following shuffling method is used to shuffle an array arr of int values. The method assumes the existence of a swap method, where swap(arr, i, j) interchanges the elements arr[i] and arr[j].

```java
public static void shuffle (int[] arr) {
    for (int k = arr.length - 1; k > 0; k--)
        { 
            int randIndex = (int) (Math.random() * (k + 1));
            swap(arr, k, randIndex);
        }
}
```

Suppose the initial state of arr is 1 2 3 4 5, and when the method is executed the values generated for randIndex are 3, 2, 0, and 1, in that order. What will be the final state of arr?

(A) 5 2 1 3 4  
(B) 1 2 5 3 4  
(C) 5 4 1 3 2  
(D) 4 5 1 3 2  
(E) 2 5 1 3 4
13. Refer to method `removeWord`.

```java
/** @param wordList an ArrayList of String objects  
 * @param word the word to be removed  
 * @Postcondition: All occurrences of word have been removed  
 * from wordList. */
public static void removeWord(ArrayList<String> wordList,
                          String word)
{
    for (int i = 0; i < wordList.size(); i++)
        if ((wordList.get(i)).equals(word))
            wordList.remove(i);
}
```

The method does not always work as intended. Consider the method call

```java
removeWord(wordList, "cat");
```

For which of the following lists will this method call fail?

(A) The cat sat on the mat
(B) The cat cat sat on the mat mat
(C) The cat sat on the cat
(D) cat
(E) The cow sat on the mat

14. A `Clock` class has hours, minutes, and seconds represented by `int` values. It also has each of the following methods: `setTime` to change the time on a `Clock` to the hour, minute, and second specified; `getTime` to access the time; and `toString` to return the time as a `String`. The `Clock` class has a constructor that allows a `Clock` to be created with three `int` parameters for hours, minutes, and seconds. Consider a two-dimensional array of `Clock` values called `allClocks`. A code segment manipulating `allClocks` is as follows:

```java
for (Clock[] row : allClocks)
    for (Clock c : row)
        /* more code */
```

Assuming the `Clock` class works as specified, which replacement for `/* more code */` will cause an error?

I `System.out.print(c);
II c.setTime(0, 0, 0);
III c = new Clock(0, 0, 0);

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I and II only

GO ON TO THE NEXT PAGE.
15. Consider the following method that will access a square matrix mat:

```java
/** Precondition: mat is initialized and is a square matrix. */
public static void printSomething(int[][] mat)
{
    for (int r = 0; r < mat.length; r++)
    {
        for (int c=0; c<=r; c++)
            System.out.print(mat[r][c] + " ");
        System.out.println();
    }
}
```

Suppose mat is originally

```
0 1 2 3
4 5 6 7
3 2 1 0
7 6 5 4
```

After the method call `printSomething(mat)` the output will be

(A) `0 1 2 3
4 5 6 7
3 2 1 0
7 6 5 4`

(B) `0
4 5
3 2 1
7 6 5 4`

(C) `0 1 2 3
4 5 6
3 2
7`

(D) `0
4
3
7`

(E) There will be no output. An `ArrayIndexOutOfBoundsException` will be thrown.
16. Consider two different ways of storing a set of nonnegative integers in which there are no duplicates.

Method One: Store the integers explicitly in an array in which the number of elements is known. For example, in this method, the set \{6, 2, 1, 8, 9, 0\} can be represented as follows:

<table>
<thead>
<tr>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>2</td>
<td>1</td>
<td>8</td>
<td>9</td>
<td>0</td>
</tr>
</tbody>
</table>

6 elements

Method Two: Suppose that the range of the integers is 0 to MAX. Use a boolean array indexed from 0 to MAX. The index values represent the possible values in the set. In other words, each possible integer from 0 to MAX is represented by a different position in the array. A value of true in the array means that the corresponding integer is in the set, a value of false means that the integer is not in the set. For example, using this method for the same set above, \{6, 2, 1, 8, 9, 0\}, the representation would be as follows (T = true, F = false):

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | ... | MAX |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| T | T | T | F | F | F | T | F | T | T | F | ... | F |

The following operations are to be performed on the set of integers:

I Search for a target value in the set.
II Print all the elements of the set.
III Return the number of elements in the set.

Which statement is true?
(A) Operation I is more efficient if the set is stored using Method One.
(B) Operation II is more efficient if the set is stored using Method Two.
(C) Operation III is more efficient if the set is stored using Method One.
(D) Operation I is equally efficient for Methods One and Two.
(E) Operation III is equally efficient for Methods One and Two.

17. An algorithm for finding the average of \(N\) numbers is

\[
\text{average} = \frac{\text{sum}}{N}
\]

where \(N\) and sum are both integers. In a program using this algorithm, a programmer forgot to include a test that would check for \(N\) equal to zero. If \(N\) is zero, when will the error be detected?

(A) At compile time
(B) At edit time
(C) As soon as the value of \(N\) is entered
(D) During run time
(E) When an incorrect result is output
18. What is wrong with this interface?

```java
public interface Bad
{
    void someMethod(String password)
    {
        System.out.println("Psst! The password is " + password);
    }
}
```

(A) A method in an interface should be declared public.
(B) A method in an interface should be declared abstract.
(C) There should not be a method implementation.
(D) There should be a class implementation provided.
(E) There should not be any method parameters.

19. Consider method `getCount` below:

```java
public static int getCount(String s, String sub)
{
    int count = 0;
    int pos = s.indexOf(sub);
    while (pos >= 0)
    {
        s = s.substring(pos);
        count++;
        pos = s.indexOf(sub);
    }
    return count;
}
```

What will the method call `getCount("a carrot and car", "car")` return?

(A) 0
(B) 1
(C) 2
(D) 3
(E) No value returned. The method is in an infinite loop.
20. Consider a program that deals with various components of different vehicles. Which of the following is a reasonable representation of the relationships among some classes that may comprise the program? Note that an open up-arrow denotes an inheritance relationship and a down-arrow denotes a composition relationship.

(A) ![Diagram A]

(B) ![Diagram B]

(C) ![Diagram C]

(D) ![Diagram D]

(E) ![Diagram E]
21. Consider the following program segment:

```java
/** Precondition: a[0]...a[n-1] is an initialized array of integers,
   * and 0 < n <= a.length. */
int c = 0;
for (int i = 0; i < n; i++)
   if (a[i] >= 0)
      { a[c] = a[i]; c++; }
n = c;
```

Which is the best postcondition for the segment?
(A) a[0]...a[n-1] has been stripped of all positive integers.
(B) a[0]...a[n-1] has been stripped of all negative integers.
(C) a[0]...a[n-1] has been stripped of all nonnegative integers.
(D) a[0]...a[n-1] has been stripped of all occurrences of zero.
(E) The updated value of n is less than or equal to the value of n before execution of the segment.

22. If a, b, and c are integers, which of the following conditions is sufficient to guarantee that the expression

```
a < c || a < b && !(a == c)
```

evaluates to true?
(A) a < c
(B) a < b
(C) a > b
(D) a == b
(E) a == c

23. Airmail Express charges for shipping small packages by integer values of weight. The charges for a weight w in pounds are as follows:

<table>
<thead>
<tr>
<th>Weight Range</th>
<th>Charge</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 &lt; w &lt;= 2</td>
<td>$4.00</td>
</tr>
<tr>
<td>2 &lt; w &lt;= 5</td>
<td>$8.00</td>
</tr>
<tr>
<td>5 &lt; w &lt;= 20</td>
<td>$15.00</td>
</tr>
</tbody>
</table>

The company does not accept packages that weigh more than 20 pounds. Which of the following represents the best set of data (weights) to test a program that calculates shipping charges?
(A) 0, 2, 5, 20
(B) 1, 4, 16
(C) −1, 1, 2, 3, 5, 16, 20
(D) −1, 0, 1, 2, 3, 5, 16, 20, 22
(E) All integers from −1 through 22
24. Consider the following instance variable and methods in the same class.

private int[][] matrix;

/** Precondition: array.length > 0. 
* @return the largest integer in array */
private int max(int[] array)
{
    /* implementation not shown */
}

/** @return num1 if num1 >= num2; otherwise return num2 */
public int max(int num1, int num2)
{
    /* implementation not shown */
}

Suppose matrix has a current value of

2 1 4 8
6 0 3 9
5 7 7 6
1 2 3 4

What will be returned by the following method call in the same class?

max(max(matrix[2]), max(matrix[3]))

(A) 9  
(B) 8  
(C) 7  
(D) 4  
(E) Compile-time error. No value returned.
Questions 25–26 are based on the following class declaration:

```java
public class AutoPart
{
    private String description;
    private int partNum;
    private double price;

    public AutoPart(String desc, int pNum, double aPrice)
    { /* implementation not shown */ }

    public String getDescription()
    { return description; }

    public int getPartNum()
    { return partNum; }

    public double getPrice()
    { return price; }

    // Other methods are not shown.
    // There is no compareTo method.
}
```

GO ON TO THE NEXT PAGE.
25. This question refers to the findCheapest method below, which occurs in a class that has an array of AutoPart as one of its private data fields:

```java
private AutoPart[] allParts;
```

The findCheapest method examines an array of AutoPart and returns the part number of the AutoPart with the lowest price whose description matches the partDescription parameter. For example, several of the AutoPart elements may have "headlight" as their description field. Different headlights will differ in both price and part number. If the partDescription parameter is "headlight", then findCheapest will return the part number of the cheapest headlight.

```java
/**
 * Precondition: allParts contains at least one element whose
 * description matches partDescription.
 * @param partDescription the description of a part in allParts
 * @return the part number of the cheapest AutoPart
 * whose description matches partDescription
 */
public int findCheapest(String partDescription)
{
    AutoPart part = null; //AutoPart with lowest price so far
    double min = LARGE_VALUE; //larger than any valid price
    for (AutoPart p : allParts)
    {
        /* more code */
    }
    return part.getPartNum();
}
```

Which of the following replacements for /* more code */ will find the correct part number?

I if (p.getPrice() < min)
{
    min = p.getPrice();
    part = p;
}

II if (p.getDescription().equals(partDescription))
    if (p.getPrice() < min)
    {
        min = p.getPrice();
        part = p;
    }

III if (p.getDescription().equals(partDescription))
    if (p.getPrice() < min)
        return p.getPartNum();

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I and III only
26. Consider the following method:

```java
/** Precondition: st1 and st2 are distinct String objects.
 * @return smaller of st1 and st2 */
public static String min(String st1, String st2)
{
    if (st1.compareTo(st2) < 0)
        return st1;
    else
        return st2;
}
```

A method in the same class has these declarations:

```java
AutoPart p1 = new AutoPart(<suitable values>);
AutoPart p2 = new AutoPart(<suitable values>);
```

Which of the following statements will cause an error?

I. `System.out.println(min(p1.getDescription(), p2.getDescription()));`

II. `System.out.println(min(((String) p1).getDescription(), ((String) p2).getDescription()));`

III. `System.out.println(min(p1, p2));`

(A) None  
(B) I only  
(C) II only  
(D) III only  
(E) II and III only

27. This question is based on the following declarations:

```java
String strA = "CARROT", strB = "Carrot", strC = "car";
```

Given that all uppercase letters precede all lowercase letters when considering alphabetical order, which is true?

(A) `strA.compareTo(strB) < 0 && strB.compareTo(strC) > 0`

(B) `strC.compareTo(strB) < 0 && strB.compareTo(strA) < 0`

(C) `strB.compareTo(strC) < 0 && strB.compareTo(strA) > 0`

(D) `!(strA.compareTo(strB) == 0) && strB.compareTo(strA) < 0`

(E) `!(strA.compareTo(strB) == 0) && strC.compareTo(strB) < 0`

GO ON TO THE NEXT PAGE.
28. A programmer has a file of names. She is designing a program that sends junk mail letters to everyone on the list. To make the letters sound personal and friendly, she will extract each person's first name from the name string. She plans to create a parallel file of first names only. For example,

<table>
<thead>
<tr>
<th>fullName</th>
<th>firstName</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ms. Anjali DeSouza</td>
<td>Anjali</td>
</tr>
<tr>
<td>Dr. John Roufaieil</td>
<td>John</td>
</tr>
<tr>
<td>Mrs. Mathilda Concia</td>
<td>Mathilda</td>
</tr>
</tbody>
</table>

Here is a method intended to extract the first name from a full name string.

```java
/**
 * Precondition:
 * - fullName starts with a title followed by a period.
 * - A single space separates the title, first name, and last name.
 * @param fullName a string containing a title, period, blank, and last name
 * @return the first name only in fullName
 */
public static String getFirstName(String fullName)
{
    final String BLANK = " ";
    String temp, firstName;

    /* code to extract first name */
    return firstName;
}
```

Which represents correct /* code to extract first name */?

I int k = fullName.indexOf(BLANK);
    temp = fullName.substring(k + 1);
    k = temp.indexOf(BLANK);
    firstName = temp.substring(0, k);

II int k = fullName.indexOf(BLANK);
    firstName = fullName.substring(k + 1);
    k = firstName.indexOf(BLANK);
    firstName = firstName.substring(0, k);

III int firstBlank = fullName.indexOf(BLANK);
    int secondBlank = fullName.indexOf(BLANK);
    firstName = fullName.substring(firstBlank + 1, secondBlank + 1);

(A) I only
(B) II only
(C) III only
(D) I and II only
(E) I, II, and III
Questions 29–31 refer to the ThreeDigitInteger and ThreeDigitCode classes below.

```java
public class ThreeDigitInteger {
    private int hundredsDigit;
    private int tensDigit;
    private int onesDigit;
    private int value;

    /** @param aValue a 3-digit int */
    public ThreeDigitInteger(int aValue) {
        /* implementation not shown */
    }

    /** @return the sum of digits for this ThreeDigitInteger */
    public int digitSum() {
        /* implementation not shown */
    }

    /** @return the sum of the hundreds digit and tens digit */
    public int twoDigitSum() {
        /* implementation not shown */
    }

    // Other methods are not shown.
}

public class ThreeDigitCode extends ThreeDigitInteger {
    private boolean isValid;

    /** @param aValue a 3-digit int */
    public ThreeDigitCode(int aValue) {
        /* implementation code */
    }

    /** A ThreeDigitCode is valid if and only if the remainder when
     * the sum of the hundreds and tens digits is divided by 7 equals
     * the ones digit. Thus 362 is valid while 364 is not.
     * @return true if ThreeDigitCode is valid, false otherwise */
    public boolean isValid() {
        /* implementation not shown */
    }
}
```

Go on to the next page.
29. Which is a true statement about the classes shown?
   (A) The ThreeDigitInteger class inherits the isValid method from the class ThreeDigitCode.
   (B) The ThreeDigitCode class inherits all of the public accessor methods from the ThreeDigitInteger class.
   (C) The ThreeDigitCode class inherits the constructor from the class ThreeDigitInteger.
   (D) The ThreeDigitCode class can directly access all the private variables of the ThreeDigitInteger class.
   (E) The ThreeDigitInteger class can access the isValid instance variable of the ThreeDigitCode class.

30. Which is correct /* implementation code */ for the ThreeDigitCode constructor?
   I super(value);
      isValid = isValid();
   II super(value, valid);
   III super(value);
      isValid = twoDigitSum() % 7 == onesDigit;

   (A) I only
   (B) II only
   (C) III only
   (D) I and III only
   (E) I, II, and III

31. Refer to these declarations in a client program:

   ```java
   ThreeDigitInteger code = new ThreeDigitCode(127);
   ThreeDigitInteger num = new ThreeDigitInteger(456);
   ```

   Which of the following subsequent tests will not cause an error?
   I if (code.isValid())
      ...
   II if (num.isValid())
      ...
   III if (((ThreeDigitCode) code).isValid())
      ...

   (A) I only
   (B) II only
   (C) III only
   (D) I and II only
   (E) I and III only
32. Consider the following hierarchy of classes:

```
Bird
  Parrot
  Parakeet
     Owl
```

Assuming that each class has a valid default constructor, which of the following declarations in a client program are correct?

I  Bird b1 = new Parrot();
   Bird b2 = new Parakeet();
   Bird b3 = new Owl();

II Parakeet p = new Parrot();
     Owl o = new Bird();

III Parakeet p = new Bird();

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III

33. Consider an array arr and a list list that is an ArrayList<String>. Both arr and list are initialized with string values. Which of the following code segments correctly appends all the strings in arr to the end of list?

I  for (String s : arr)
     list.add(s);

II for (String s : arr)
     list.add(list.size(), s);

III for (int i = 0; i < arr.length; i++)
     list.add(arr[i]);

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III

GO ON TO THE NEXT PAGE.
34. Refer to the `nextIntInRange` method below:

```java
/** @return a random integer in the range low to high, inclusive */
public int nextIntInRange(int low, int high)
{
    return /* expression */
}
```

Which /* expression */ will always return a value that satisfies the postcondition?

A) `(int) (Math.random() * high) + low;`
B) `(int) (Math.random() * (high - low)) + low;`
C) `(int) (Math.random() * (high - low + 1)) + low;`
D) `(int) (Math.random() * (high + low)) + low;`
E) `(int) (Math.random() * (high + low - 1)) + low;`

35. Consider the following `mergeSort` method and the private instance variable `a` both in the same `Sorter` class:

```java
private int[] a;

/** Sorts a[first] to a[last] in increasing order using mergesort. */
public void mergeSort(int first, int last)
{
    if (first != last)
    {
        int mid = (first + last) / 2;
        mergeSort(first, mid);
        mergeSort(mid + 1, last);
        merge(first, mid, last);
    }
}
```

Method `mergeSort` calls method `merge`, which has this header:

```java
/** Merge a[lb] to a[mi] and a[mi+1] to a[ub].
 * Precondition: a[lb] to a[mi] and a[mi+1] to a[ub] both
 * sorted in increasing order.
 * */
private void merge(int lb, int mi, int ub)
```

If the first call to `mergeSort` is `mergeSort(0,3)`, how many further calls will there be to `mergeSort` before an array `b[0]...b[3]` is sorted?

A) 2
B) 3
C) 4
D) 5
E) 6

---

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36. A large hospital maintains a list of patients’ records in no particular order. To find the record of a given patient, which represents the most efficient method that will work?
   (A) Do a sequential search on the name field of the records.
   (B) Do a binary search on the name field of the records.
   (C) Use insertion sort to sort the records alphabetically by name; then do a sequential search on the name field of the records.
   (D) Use mergesort to sort the records alphabetically by name; then do a sequential search on the name field of the records.
   (E) Use mergesort to sort the records alphabetically by name; then do a binary search on the name field of the records.

Use the following information for Questions 37 and 38.

Here is a diagram that shows the relationship between some of the classes that will be used in a program to draw a banner with block letters.

![Diagram showing hierarchy of classes](image)

The diagram shows that the Banner class uses BlockLetter objects, and that the BlockLetter class has 26 subclasses, representing block letters from A to Z.

The BlockLetter class has an abstract draw method

```java
public abstract void draw();
```

Each of the subclasses shown implements the draw method in a unique way to draw its particular letter. The Banner class gets an array of BlockLetter and has a method to draw all the letters in this array.

Here is a partial implementation of the Banner class:

```java
public class Banner {
    private BlockLetter[] letters;
    private int numLetters;

    /** Constructor. Gets the letters for the Banner. */
    public Banner() {
        numLetters = <some integer read from user input>
        letters = getLetters();
    }
}
```
/** @return an array of block letters */
public BlockLetter[] getLetters()
{
    String letter;
    letters = new BlockLetter[numLetters];
    for (int i = 0; i < numLetters; i++)
    {
        <read in capital letter>
        if (letter.equals("A"))
            letters[i] = new LetterA();
        else if (letter.equals("B"))
            letters[i] = new LetterB();
        ...  //similar code for C through Y
        else
            letters[i] = new LetterZ();
    }
    return letters;
}

/** Draw all the letters in the Banner. */
public void drawLetters()
{
    for (BlockLetter letter : letters)
        letter.draw();
}

//Other methods are not shown.

37. You are given the information that BlockLetter is an abstract class that is used in the program. Which of the following can you conclude about the class?

I  All of its methods must be abstract.
II  It must have at least one subclass.
III  No instances of BlockLetter can be created.

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III

38. Which is a true statement about method drawLetters?
(A) It is an overloaded method in the Banner class.
(B) It is an overridden method in the Banner class.
(C) It uses polymorphism to draw the correct letters.
(D) It will cause a compile-time error because draw is not implemented in the BlockLetter class.
(E) It will cause a run-time error because draw is not implemented in the BlockLetter class.

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39. Consider method1 and method2 below, which are identical except for the second last line of code. Each method returns a new matrix based on the input matrix mat.

```java
public static int[][] method1(int[][] mat)
{
    int numRows = mat.length;
    int numCols = mat[0].length;
    int[][] newMat = new int[numRows][numCols];
    for (int row = 0; row < numRows; row++)
        for (int col = 0; col < numCols; col++)
            newMat[numRows - row - 1][col] = mat[row][col];
    return newMat;
}
```

```java
public static int[][] method2(int[][] mat)
{
    int numRows = mat.length;
    int numCols = mat[0].length;
    int[][] newMat = new int[numRows][numCols];
    for (int row = 0; row < numRows; row++)
        for (int col = 0; col < numCols; col++)
            newMat[row][col] = mat[numRows - row - 1][col];
    return newMat;
}
```

Suppose the same input matrix is used for method1 and method2, and the output for method1 is matrix1 while the output for method2 is matrix2. Which is a true statement about matrix1 and matrix2?

(A) matrix1 is identical to matrix2.
(B) The rows of matrix1 are the columns of matrix2.
(C) matrix1 is a reflection of matrix2 across a vertical line on the edge of either matrix.
(D) matrix1 is a reflection of matrix2 across a horizontal line on the bottom or top edge of either matrix.
(E) The rows of matrix1 are the rows of matrix2 in reverse order.
40. Consider an ArrayList cards of Card objects that needs to be shuffled. The following algorithm is used for shuffling:

Create a temporary ArrayList<Card>
Do the following cards.size() number of times
  - Generate a random integer r that can index any card in cards
  - Remove the card found at position r in cards and add it to the end of the temporary ArrayList
Set cards to the temporary ArrayList

Here is the method that implements this algorithm.

Line 1: public void shuffle()
Line 2: {
Line 3:   int size = cards.size();
Line 4:   List<Card> temp = new ArrayList<Card>();
Line 5:   for (int j = 1; j < size; j++)
Line 6:     {
Line 7:       int index = (int) (Math.random() * size);
Line 8:       temp.add(cards.get(index));
Line 9:     }
Line 10:    cards = temp;
Line 11:  }

The method does not work as intended. Which of the following changes to shuffle would ensure that it works correctly?

I Replace Line 5 with
   for (int j = 0; j < size; j++)

II Replace Line 7 with
   int index = (int) (Math.random() * cards.size());

III Replace Line 8 with
   temp.add(cards.remove(index));

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III

END OF SECTION I
1. Consider a system for processing names and addresses from a mailing list. A Recipients class will be used as part of this system. The lines in the mailing list are stored in an ArrayList<String>, a private instance variable in the Recipients class. The blank line that separates recipients in the mailing list is stored as the empty string in this list, and the final element in the list is an empty string.

A portion of the mailing list is shown below, with the corresponding part of the ArrayList.

Mr. J. Adams
6 Rose St.
Ithaca, NY 14850

Jack S. Smith
12 Posy Way
Suite 201
Glendale, CA 91203

Ms. M.K. Delgado
2 River Dr.
New York, NY 10013

...
The `Recipients` class that processes this data is shown below.

```java
public class Recipients {
    /** The list of lines in the mailing list */
    private List<String> lines;

    /** Constructor. Fill lines with mailing list data.
     * Postcondition:
     * - Each element in lines is one line of the mailing list.
     * - Lines appear in the list in the same order
     *   that they appear in the mailing list.
     * - Blank line separators in the mailing list are stored
     *   as empty strings.
     */
    public Recipients()
    { /* implementation not shown */ }

    /** Postcondition: Returns the city contained in the cityZip
     * string of an address.
     * @param cityZip contains the city, state, and zipcode
     * @return the city substring contained in cityZip
     */
    public String extractCity(String cityZip)
    { /* to be implemented in part (a) */ }

    /** Precondition: The recipient name is the first line of each
     * label on the mailing list.
     * Postcondition: Prints a list of recipient names to console,
     * one per line.
     */
    public void printNames()
    { /* to be implemented in part (b) */ }
}
```

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/** Postcondition: Returns the address of the recipient with 
   * the specified name. 
   * @param name a name in the lines ArrayList 
   * @return the address of the recipient with the given name 
   */
public String getAddress(String name)
{ /* to be implemented in part (c) */ }

// Other methods are not shown.
}

(a) Write the `extractCity` method of the `Recipients` class. In the `cityZip` parameter the city is followed by a comma, then one blank space, then two capital letters for a state abbreviation, then a space and 5-digit zip code. For example, if `cityZip` is "Ithaca, NY 14850", the method call `extractCity(cityZip)` should return "Ithaca".

Complete method `extractCity` below.

/** Postcondition: Returns the city contained in the `cityZip` string of an address. 
   * @param cityZip contains the city, state, and zipcode 
   * @return the city substring contained in cityZip 
   */
public String extractCity(String cityZip)

(b) Write the `printNames` method of the `Recipients` class. Method `printNames` prints the names of all recipients to the console, one per line. For the sample part of the mailing list shown at the beginning of the question, the output for `printNames` would be:

Mr. J. Adams
Jack S. Smith
Ms. M.K. Delgado

GO ON TO THE NEXT PAGE.
Complete method `printNames` below.

```java
/** Precondition: The recipient name is the first line of each label on the mailing list.
 * Postcondition: Prints a list of recipient names to console, one per line.
 */
public void printNames()
```

(c) Write the `getAddress` method of the `Recipients` class. This method should return a string that contains only the address of the corresponding `name` parameter. For example, if `name` is “Jack S. Smith”, a string containing the three subsequent lines of his address should be returned. This string should contain line breaks in appropriate places, including after the last line of the address. This ensures that the address will have the proper address format when printed by a client class.

Complete method `getAddress` below.

```java
/** Postcondition: Returns the address of the recipient with the specified name.
 * @param name a name in the lines ArrayList
 * @return the address of the recipient with the given name
 */
public String getAddress(String name)
```
2. A `WordSet`, whose partial implementation is shown in the class declaration below, stores a set of `String` objects in no particular order and contains no duplicates. Each word is a sequence of capital letters only.

```java
public class WordSet {
    /** Constructor initializes set to empty. */
    public WordSet() {
        /* implementation not shown */
    }

    /** @return the number of words in set */
    public int size() {
        /* implementation not shown */
    }

    /** Adds word to set (no duplicates).
     * @param word the word to be added
     */
    public void insert(String word) {
        /* implementation not shown */
    }

    /** Removes word from set if present, else does nothing.
     * @param word the word to be removed
     */
    public void remove(String word) {
        /* implementation not shown */
    }

    /** Returns kth word in alphabetical order, where 1 <= k <= size().
     * @param k position of word to be returned
     * @return the kth word
     */
    public String findkth(int k) {
        /* implementation not shown */
    }

    /** @return true if set contains word, false otherwise */
    public boolean contains(String word) {
        /* implementation not shown */
    }

    // Other instance variables, constructors, and methods are not shown.
}
```
The `findkth` method returns the \( k \)th word in alphabetical order in the set, even though the implementation of `WordSet` may not be sorted. The number \( k \) ranges from 1 (corresponding to first in alphabetical order) to \( N \), where \( N \) is the number of words in the set. For example, if `WordSet s` stores the words \{“GRAPE”, “PEAR”, “FIG”, “APPLE”\}, here are the values when \( s.findkth(k) \) is called.

<table>
<thead>
<tr>
<th>( k ) values of ( s.findkth(k) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>4</td>
</tr>
</tbody>
</table>

(a) Write a client method `countA` that returns the number of words in `WordSet s` that begin with the letter “A.” In writing `countA`, you may call any of the methods of the `WordSet` class. Assume that the methods work as specified.

Complete method `countA` below.

```java
/** @param s the current `WordSet`
 * @return the number of words in s that begin with "A"
 */
public static int countA(WordSet s)
```

(b) Write a client method `removeA` that removes all words that begin with “A.” If there are no such words in \( s \), then `removeA` does nothing. In writing `removeA`, you may call method `countA` specified in part (a). Assume that `countA` works as specified, regardless of what you wrote in part (a).

```
Complete method `removeA` below:

```java
/** @param s the current `WordSet`
 * @Postcondition: `WordSet s` contains no words that begin with
 * "A", but is otherwise unchanged.
 */
public static void removeA(WordSet s)
```
(c) Write a client method `commonElements` that returns the `WordSet` containing just those elements occurring in both of its `WordSet` parameters.

For example, if `s1` is `{"BE", "NOT", "AFRAID"}` and `s2` is `{"TO", "BE", "OR", "NOT"}`, then `commonElements(s1, s2)` should return the `WordSet` `{"BE", "NOT"}`. (If you are familiar with mathematical set theory, `commonElements` returns the intersection of `s1` and `s2`.)

Complete method `commonElements` below.

```java
/** @param s1 the first given set
 * @param s2 the second given set
 * @return the WordSet containing only the elements that occur in both s1 and s2
 */
public static WordSet commonElements(WordSet s1, WordSet s2)
```

3. A puzzle-solving competition is held in a large hall with a two-dimensional arrangement of contestants. Each square below represents one contestant.

```
0
  0  1  2  ...  CONTESTANTS_PER_ROW-1
1
  :  :  :  ...  :
:  :
NUM_ROWS-1
  :  :  :  ...  :
```

Since contestants may be moved around during the competition, each contestant keeps track of his or her location, which is the row number and column number. A `Location` object is represented by the class below.
public class Location
{
    private int rowNumber;
    private int colNumber;

    /** Create a new Location.
     * @param row the row number
     * @param col the column number */
    public Location (int row, int col)
    {
        rowNumber = row;
        colNumber = col;
    }

    /** @return the row number of this Location */
    public int getRowNumber()
    { return rowNumber; }

    /** @return the column number of this Location */
    public int getColNumber()
    { return colNumber; }

    public String toString()
    { /* implementation not shown */}
}

A contestant in the contest can be represented by a Contestant class, whose partial implementation is shown below.

public class Contestant
{
    private String name;
    private int score;
    private Location loc;

    /** @return the name of this contestant */
    public String getName()
    { return name; }

    /** @return the score of this contestant */
    public int getScore()
    { return score; }

    /** @return the location of this contestant */
    public Location getLocation()
    { return loc; }

    /** Changes the location of this contestant to a new row
     * and column.
     * @param newRow the new row
     * @param newCol the new column */
    public void updateLocation(int newRow, int newCol)
    { /* to be implemented in part (a) */ }

    //Constructor and other methods are not shown.
}
(a) Write the Contestant method updateLocation, which changes the contestant's location to have the new row and column numbers.

Complete method updateLocation below.

```java
/** Changes the location of this contestant to a new row
* and column.
* @param newRow the new row
* @param newCol the new column
*/
public void updateLocation(int newRow, int newCol)
```

In parts (b) and (c) you will write two methods of a ContestOrganizer class, whose partial implementation is shown below. A contest organizer keeps track of contestants in a two-dimensional array.

```java
public class ContestOrganizer {

    /** the number of rows of contestants */
    public static final int NUM_ROWS = <some integer>;

    /** the number of columns of contestants */
    public static final int CONTESTANTS_PER_ROW = <some integer>;

    /** The two-dimensional array of contestants */
    private Contestant[][] contestants;

    /** Sorts arr in increasing order by score.
    * Postcondition:
    * - arr sorted in increasing order by score.
    * - Location of each contestant correctly updated such that
    *   column number matches contestant's position in arr.
    * @param arr the array to be sorted
    */
    private void sort(Contestant[] arr) {
        /* implementation not shown */
    }

    /** Sorts each row of contestants into increasing order by score.
    * Postcondition: Contestant with highest score in row[k] is
    * in the rightmost column of row[k], 0<=k<NUM_ROWS.
    */
    public void sortAllRows() {
        /* to be implemented in part(b) */
    }

    /** Returns name of contestant with highest score.
    * Precondition:
    * - Contestants have not been sorted by score.
    * - Top score is unique.
    * - Only one contestant has the highest score.
    * @return name of contestant with highest score
    */
    public String findWinnerName() {
        /* to be implemented in part(c) */
    }
}
```

GO ON TO THE NEXT PAGE.
(b) Write the ContestOrganizer method sortAllRows. This method should sort the contestants by score in each row, from lowest to highest.
Example: Suppose contestants are as shown below:

<table>
<thead>
<tr>
<th></th>
<th>0</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>John</td>
<td>Mary</td>
<td>Jay</td>
</tr>
<tr>
<td></td>
<td>160</td>
<td>185</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>(0,0)</td>
<td>(0,1)</td>
<td>(0,2)</td>
</tr>
<tr>
<td>1</td>
<td>Harry</td>
<td>Ted</td>
<td>Joan</td>
</tr>
<tr>
<td></td>
<td>190</td>
<td>100</td>
<td>88</td>
</tr>
<tr>
<td></td>
<td>(1,0)</td>
<td>(1,1)</td>
<td>(1,2)</td>
</tr>
</tbody>
</table>

Here is what contestants will be after a call to sortAllRows:

<table>
<thead>
<tr>
<th></th>
<th>0</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Jay</td>
<td>John</td>
<td>Mary</td>
</tr>
<tr>
<td></td>
<td>22</td>
<td>160</td>
<td>185</td>
</tr>
<tr>
<td></td>
<td>(0,0)</td>
<td>(0,1)</td>
<td>(0,2)</td>
</tr>
<tr>
<td>1</td>
<td>Joan</td>
<td>Ted</td>
<td>Harry</td>
</tr>
<tr>
<td></td>
<td>88</td>
<td>100</td>
<td>190</td>
</tr>
<tr>
<td></td>
<td>(1,0)</td>
<td>(1,1)</td>
<td>(1,2)</td>
</tr>
</tbody>
</table>

In writing sortAllRows, your method must use the ContestantOrganizer method sort. You may assume that sort works as specified.

Complete method sortAllRows below.

```java
/** Sorts each row of contestants into increasing order by score.
 * Postcondition: Contestant with highest score in row[k] is in the rightmost column of row[k], 0<=k<NUM_ROWS.
 */
public void sortAllRows()
```

(c) Write the Contestant method findWinnerName, which returns the name of the contestant with the highest score. For example, if the contestants are as shown above, a call to findWinnerName should return “Harry”.
When writing findWinnerName, you should assume that the contestants have not yet been sorted by score, and that there is only one contestant with the highest score. In writing your solution, you must use method sortAllRows. You may assume that sortAllRows works as specified, regardless of what you wrote in part (b).

Complete method findWinnerName below.

```java
/** Returns name of contestant with highest score.
 * Precondition:
 * - Contestants have not been sorted by score.
 * - Top score is unique.
 * - Only one contestant has the highest score.
 */
public String findWinnerName()
```
4. Consider the hierarchy of classes shown for a small part of a bird sanctuary.

Notice that an Owl is a Bird, a SnowyOwl is a Owl, and an ElfOwl is a Owl. The class Bird is specified as an abstract class as shown in the following implementation. Each Bird has a name and a noise that are specified when it is constructed.

```java
public abstract class Bird {
    private String name;
    private String noise;

    /** Constructor for objects of class Bird */
    public Bird(String birdName, String birdNoise)
    {
        name = birdName;
        noise = birdNoise;
    }

    public String getName()
    { return name; }

    public String getNoise()
    { return noise; }

    public abstract String getFood();
}
```

An Owl is a Bird whose noise is "hoot". The food it eats depends on the type of Owl, which means that getFood cannot be implemented in the Owl class. Here is the implementation for the Owl class.

```java
public abstract class Owl extends Bird {
    //Constructor
    public Owl(String owlName)
    {
        super(owlName, "hoot");
    }
}
```

GO ON TO THE NEXT PAGE.
(a) A SnowyOwl is an Owl whose name is always "Snowy owl". A SnowyOwl will randomly eat a hare, a lemming, or a small bird (depending on what’s available!), where each type of food is equally likely. The SnowyOwl class should use a random number to determine which food the SnowyOwl will eat. Assuming that the Owl class has been correctly defined, and given the class hierarchy shown previously, write a complete declaration of the class SnowyOwl, including implementation of its constructor and method(s).

(b) Consider the following partial declaration of class BirdSanctuary.

```java
public class BirdSanctuary
{
    /** The list of birds */
    private Bird[] birdList;

    /** Precondition: Each Bird in birdList has a getFood *
     * method implemented for it. *
     * Postcondition: For each Bird in the birdList array, its name *
     * followed by the result of a call to its getFood *
     * method has been printed, one line per Bird. */
    public void allEat()
    { /* to be implemented in this part */ }

    //The constructor and other methods are not shown.
}
```

Write the BirdSanctuary method allEat. For each Bird in BirdSanctuary, allEat prints a line with the name of the Bird followed by the result of a call to its getFood method, one line per Bird.

Complete method allEat below.

```java
/** Precondition: Each Bird in birdList has a getFood *
     * method implemented for it. *
     * Postcondition: For each Bird in the birdList array, its name *
     * followed by the result of a call to its getFood *
     * method has been printed, one line per Bird. */
public void allEat()
```
ANSWER KEY (Section I)

<p>| | | | | | | | | | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>2. C</td>
<td>16. C</td>
<td>30. A</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4. C</td>
<td>18. C</td>
<td>32. A</td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8. D</td>
<td>22. A</td>
<td>36. A</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>13. B</td>
<td>27. C</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

ANSWERS EXPLAINED

Section I

1. (C) Testing a program thoroughly does not prove that a program is correct. For a large program, it is generally impossible to test every possible set of input data.

2. (C) The private instance variable hourlyWage must be incremented by amt. Eliminate choice E, which doesn’t increment hourlyWage; it simply replaces it by amt. Choice D is wrong because you can’t use a method call as the left-hand side of an assignment. Choices A and B are wrong because the incrementWage method is void and should not return a value.

3. (D) The value of the boolean instance variable isUnionMember must be changed to the opposite of what it currently is. Segments I and II both achieve this. Note that !true has a value of false and !false a value of true. Segment III fails to do what’s required if the current value of isUnionMember is false.

4. (C) computePay is a client method and, therefore, cannot access the private variables of the class. This eliminates choices A and D. The method getHourlyWage() must be accessed with the dot member construct; thus, choice B is wrong, and choice C is correct. Choice E is way off base—hours is not part of the Worker class, so w.hours is meaningless.

5. (C) If a.length() < 4 for all strings in wordList, then SHORT WORD will be printed on each pass through the for loop. Since there are wordList.size() passes through the loop, the maximum number of times that SHORT WORD can be printed is wordList.size().
6. (E)  \[ \text{mystery}(4) = 3 \times \text{mystery}(3) \]
\[ = 3 \times 3 \times \text{mystery}(2) \]
\[ = 3 \times 3 \times 3 \times \text{mystery}(1) \]
\[ = 3 \times 3 \times 3 \times 3 \]
\[ = 81 \]

7. (A) The declaration of the `colors` array makes the following assignments: `colors[0] = "red", colors[1] = "green", and colors[2] = "black"`. The loop in segment I adds these values to `colorList` in the correct order. Segment II fails because `colors` is an array and therefore can’t use the `get` method. The code also confuses the lists. Segment III, in its first pass through the loop, attempts to add `colors[2]` to index position 2 of `colorList`. This will cause an `IndexOutOfBoundsException` to be thrown, since index positions 0 and 1 do not yet exist!

8. (D) Mergesort repeatedly splits an array of \(n\) elements in half until there are \(n\) arrays containing one element each. Now adjacent arrays are successively merged until there is a single merged, sorted array. A binary search repeatedly splits an array into two, narrowing the region that may contain the key. Insertion sort, however, does no array splitting. It takes elements one at a time and finds their insertion point in the sorted piece of the array. Elements are shifted to allow correct insertion of each element. Even though this algorithm maintains the array in two parts—a sorted part and yet-to-be-sorted part—this is not a divide-and-conquer approach.

9. (B) A static variable is shared by all instances of the class. “Static” means that there will be just one memory slot allocated, no matter how many `Insect` objects are constructed. All instances of `Insect` access the same information stored in that slot. When an `Insect` is created, it will get tagged with the current value of `nextAvailableID` for that memory slot, which will then be incremented for the next `Insect` created. All of the other variables—age, idNum, position, direction—are specific to one instance of `Insect` and should therefore be private instance variables in the class.

10. (E) A new `Address` object must be created, to be used as the `Address` parameter in the `Customer` constructor. To do this correctly requires the keyword `new` preceding the `Address` constructor. Segment II omits `new` and does not use the `Address` constructor correctly. (In fact, it inserts a new `String` object in the `Address` slot of the `Customer` constructor.)

11. (C) The algorithm used in method `locate` is a sequential search, which may have to examine all the objects to find the matching one. A binary search, which repeatedly discards a chunk of the array that does not contain the key, is more efficient. However, it can only be used if the values being examined—in this case customer ID numbers—are sorted. Note that it doesn’t help to have the array sorted by name or phone number since the algorithm doesn’t look at these values.

12. (A) The values of \(k\) are consecutively 4, 3, 2, and 1. The values of `randIndex` are consecutively 3, 2, 0, and 1. Thus, the sequence of swaps and corresponding states of `arr` will be:
13. (B) The remove method of ArrayList removes the indicated element, shifts the remaining elements down one slot (i.e., it does not leave gaps in the list), and adjusts the size of the list. Consider the list in choice B. The index values are shown:

```
1 2 3 4
```

After the first occurrence of cat has been removed:

```
1 2 3 4
```

The value of i, which was 1 when cat was removed, has now been incremented to 2 in the for loop. This means that the word to be considered next is sat. The second occurrence of cat has been missed. Thus, the given code will fail whenever occurrences of the word to be removed are consecutive. You fix it by not allowing the index to increment when a removal occurs:

```
swap arr[4] and arr[3] 1 2 3 5 4
swap arr[3] and arr[2] 1 2 5 3 4
swap arr[2] and arr[0] 5 2 1 3 4
swap arr[1] and arr[1] 5 2 1 3 4
```

14. (C) You cannot use a for-each loop to replace elements, only to access (as in segment I) or modify using a mutator method (as in segment II). Note that segment III will compile and execute, but won’t replace the clocks in allClocks as intended.

15. (B) When r is 0, c goes from 0 to 0, and just one element, mat[0][0], will be printed. When r is 1, c goes from 0 to 1, and two elements, mat[1][0] and mat[1][1], will be printed, and so on. When r is 3, all four elements of row 3 will be printed.

16. (C) To return the number of elements in the set for Method One requires no more than returning the number of elements in the array. For Method Two, however, the number of cells that contain true must be counted, which requires a test for each of the MAX values. Note that searching for a target value in the set is more efficient for Method Two. For example, to test whether 2 is in the set, simply check if a[2] == true. In Method One, a sequential search must be done, which is less efficient. To print all the elements in Method One, simply loop over the known number of elements and print. Method Two is less efficient because the whole array must be examined: Each cell must be tested for true before printing.

17. (D) An ArithmeticException will be thrown at run time. Note that if N were of type double, no exception would be thrown. The variable sum would be assigned the value Infinity, and the error would only be detected in the output.
18. (C) An interface should provide method declarations only. No code! Note that the methods are automatically public and abstract, so there is no need to specify this explicitly.

19. (E) The first value of pos is 2, the index of the first occurrence of "car" in "a carrot and car". Then s gets assigned "carrot and car" and pos is now 0. Since pos is not advanced, it is stuck with a value of 0 and the method has an infinite loop. Notice that you can fix this problem by changing \( s=s.substring(pos); \) to \( s=s.substring(pos+1); \)

20. (A) The correct diagram uses two up arrows to show that a Car is-a Vehicle and a Truck is-a Vehicle (inheritance relationship). The two down arrows indicate that a Car has-a AirBag and a Truck has-a AirBag (composition relationship). In each of the incorrect choices, at least one of the relationships does not make sense. For example, in choice B a Vehicle has-a Truck, and in choice E an AirBag is-a Car.

21. (B) The postcondition should be a true assertion about the major action of the segment. The segment overwrites the elements of array a with the nonnegative elements of b. Then n is adjusted so that now the array \( a[0]...a[n-1] \) contains just nonnegative integers. Note that even though choice E is a correct assertion about the program segment, it is not a good postcondition because it doesn't describe the main modification to array a (namely all negative integers have been removed).

22. (A) Note the order of precedence for the expressions involved: (1) parentheses, (2) !, (3) <, (4) ==, (5) & & (6) ||. This means that \( a < c, a < b, \) and \( !(a == b) \) will all be evaluated before || and & & are considered. The given expression then boils down to \( value1 || (value2 & & value3) \), since & & has higher precedence than ||. Notice that if \( value1 \) is true, the whole expression is true since (true || any) evaluates to true. Thus, \( a < c \) will guarantee that the expression evaluates to true. None of the other conditions will guarantee an outcome of true. For example, suppose \( a < b \) (choice B). If \( a == c \), then the whole expression will be false because you get F || F.

23. (D) Test data should always include a value from each range in addition to all boundary values. The given program should also handle the cases in which weights over 20 pounds or any negative weights are entered. Note that choice E contains redundant data. There is no new information to be gained in testing two weights from the same range—both 3 and 4 pounds, for example.

24. (C) The max methods shown are overloaded methods (same name but different parameter types). In the given statement, \( \text{max} [\text{matrix}[2]] \) and \( \text{max} [\text{matrix}[3]] \) refer to row 2 and row 3 of the matrix, respectively, each of which is an array of int. \( \text{max} [\text{matrix}[2]] \) is the largest element in row 2, namely 7, and \( \text{max} [\text{matrix}[3]] \) is the largest element in row 3, namely 4. The given statement is therefore equivalent to \( \text{max}(7, 4) \), which will return 7.

25. (B) Segment II correctly checks that the part descriptions match and keeps track of the current part with minimum price. If this is not done, the part whose number must be returned will be lost. Segment I is incorrect because it doesn’t check that partDescription matches the description of the current part being examined in the array. Thus, it simply finds the AutoPart with the lowest price, which is not what was required. Segment III incorrectly returns the part number of the first part it finds with a matching description.
26. (E) Statement I is fine: The parameters are String objects and can be compared. Statement II will throw a ClassCastException because an AutoPart cannot be cast to a String. Statement III will fail because p1 and p2 are not String objects and min applies to strings. Also, the AutoPart class as currently written does not have a compareTo method, so AutoPart objects cannot be compared.

27. (C) Ordering of strings involves a character-by-character comparison starting with the leftmost character of each string. Thus, strA precedes strB (since "A" precedes "a") or strA.compareTo(strB) < 0. This eliminates choices B and D. Eliminate choices A and E since strB precedes strC (because "C" precedes "c") and therefore strB.compareTo(strC) < 0. Note that string1.compareTo(string2) == 0 if and only if string1 and string2 are equal strings.

28. (D) Suppose fullName is Dr. John Roufaiel. In segment I the expression fullName.indexOf(BLANK) returns 3. Then temp gets assigned the value of fullName.substring(4), which is John Roufaiel. Next k gets assigned the value temp.indexOf(BLANK), namely 4, and firstName gets assigned temp.substring(0, 4), which is all the characters from 0 to 3 inclusive, namely John. Note that segment II works the same way, except firstName gets assigned John Roufaiel and then reassigned John. This is not good style, since a variable name should document its contents as precisely as possible. Still, the code works. Segment III fails because index0f returns the first occurrence of its String parameter. Thus, firstBlank and secondBlank will both contain the same value, 3.

29. (B) ThreeDigitCode is a subclass of ThreeDigitInteger and therefore inherits all the public methods of ThreeDigitInteger except constructors. All of the statements other than B are false. For choice A, ThreeDigitInteger is the superclass and therefore cannot inherit from its subclass. For choice C, constructors are never inherited (see p. 135). For choice D, a subclass can access private variables of the superclass through accessor methods only (see p. 135). For choice E, a superclass cannot access any additional instance variables of its subclass.

30. (A) Implementation II is wrong because the constructor has no boolean validity parameter. Implementation III is wrong because a subclass cannot access a private instance variable of its superclass.

31. (C) A compile-time error will occur for both tests I and II because at compile time the types of code and num are both ThreeDigitInteger, and the class ThreeDigitInteger does not have an isValid method. To avoid this error, the code object must be cast to ThreeDigitCode, its actual type. Note that if you try to cast num to ThreeDigitCode, you'll get a runtime error (ClassCastException) because num is not an instance of ThreeDigitCode.

32. (A) The isa relationship must work from right-to-left: a Parrot isa Bird, a Parakeet isa Bird, and an Owl isa Bird. All are correct. This relationship fails in declarations II and III: a Parrot is not necessarily a Parakeet, a Bird is not necessarily an Owl, and a Bird is not necessarily a Parakeet.

33. (E) All three segments traverse the array, accessing one element at a time, and appening it to the end of the ArrayList. In segment II, the first parameter of the add method is the position in list where the next string s will be added. Since list.size() increases by one after each insertion, this index is correctly updated in each pass through the for-each loop.
34. (C) Suppose you want random integers from 2 to 8, that is, low = 2 and high = 8. This is 7 possible integers, so you need
   
   \((\text{int}) (\text{Math.random()} * 7)\)
   
   which produces 0, 1, 2, \ldots, or 6. Therefore the quantity
   
   \((\text{int}) (\text{Math.random()} * 7) + 2\)
   
   produces 2, 3, 4, \ldots, or 8. The only expression that yields the right answer with these values is
   
   \((\text{int}) (\text{Math.random()} * (\text{high} - \text{low} + 1)) + \text{low};\)
   
35. (E) Here is a “box diagram” for mergeSort(0,3). The boldface numbers 1–6 show the order in which the mergeSort calls are made.

```
mergeSort(0,3)
  mid=(0+3)/2=1
  mergeSort(0,1)
  mergeSort(2,3)
  merge(0,1,3)

mergeSort(0,1)
  mid=(0+1)/2=0
  mergeSort(0,0)
  mergeSort(1,1)
  merge(0,0,1)

mergeSort(2,3)
  mid=(2+3)/2=2
  mergeSort(2,2)
  mergeSort(3,3)
  merge(2,2,3)
```

The mergeSort calls in which first == last are base case calls, which means that there will be no further method calls.

36. (A) Since the records are not sorted, the quickest way to find a given name is to start at the beginning of the list and sequentially search for that name. Choices C, D, and E will all work, but it’s inefficient to sort and then search because all sorting algorithms take longer than simply inspecting each element. Choice B won’t work: A binary search can only be used for a sorted list.

37. (D) Statement I is false: An abstract class may have no abstract methods. The point about an abstract class is that it represents an abstract concept, and no instance of it will ever be created. The only instances that will be created are instances of its subclasses. Statement II must be true, since you are told the abstract class is actually used in the program. Statement III is true because an abstract class cannot be instantiated.

38. (C) The draw method is polymorphic, which means that it is a superclass method that is overridden in at least one of its subclasses. During run time, there is dynamic binding between the calling object and the method, that is, the actual instance is bound to its particular overridden method. In the drawLetters method, the correct version of draw is called during each iteration of the for loop, and a banner with the appropriate letters is drawn.
39. (A) \texttt{method1} creates a mirror image of its parameter \texttt{mat} across a horizontal line placed under \texttt{mat}. If \texttt{mat} is the matrix
\begin{equation}
\begin{array}{ccc}
1 & 2 & 3 \\
4 & 5 & 6 \\
\end{array}
\end{equation}
then the mirror image created below it is
\begin{equation}
\begin{array}{ccc}
4 & 5 & 6 \\
1 & 2 & 3 \\
\end{array}
\end{equation}
\texttt{method2} also creates a mirror image, this time with the mirror placed \textit{above} its parameter \texttt{mat}. Note that the reflection across a horizontal line above
\begin{equation}
\begin{array}{ccc}
1 & 2 & 3 \\
4 & 5 & 6 \\
\end{array}
\end{equation}
is also
\begin{equation}
\begin{array}{ccc}
4 & 5 & 6 \\
1 & 2 & 3 \\
\end{array}
\end{equation}
A good general hint to solve a problem like this is to take a very simple matrix \texttt{mat} and generate some elements of \texttt{newMat}. It won’t take long to see that the two methods produce the same matrix.

40. (E) All three changes must be made! In order to move all the \texttt{Card} elements to the temporary \texttt{ArrayList}, the \texttt{for} loop must be executed \texttt{size} times. If you start \texttt{j} at 1, the loop will be executed \texttt{size}-1 times. The error in Line 7 is subtle. With each iteration of the loop, the size of the \texttt{cards ArrayList} is being reduced by 1, so the range of random indexes is getting smaller and smaller. This won’t happen if you use \texttt{size}, the length of the \texttt{original cards list}. You must use \texttt{cards.size()}, which is the length of the current, shorter list. If you don’t make correction III, the random element will not be removed from \texttt{cards}. It will (incorrectly) remain there while a copy of it will be added to \texttt{temp}. If this error isn’t corrected, execution of the method is likely to cause the \texttt{temp} list to hold more than one copy of a given card!
Section II

1. (a) public String extractCity(String cityZip)
   {
       int commaPos = cityZip.indexOf(“,“);
       return cityZip.substring(0, commaPos);
   }

   (b) public void printNames()
   {
       System.out.println(lines.get(0));
       int index = 1;
       while(index < lines.size() - 1)
       {
           if (lines.get(index).equals(“”))
               System.out.println(lines.get(index + 1));
           index++;
       }
   }

   (c) public String getAddress(String name)
   {
       int index = 0;
       while(index < lines.size() && !name.equals(lines.get(index))
           index++;
       index++;
       String s = “”;
       while (!(lines.get(index).equals(“”)))
       {
           s += lines.get(index) + “\n”;
           index++;
       }
       return s;
   }

NOTE

- In part (b), the empty string signals that the next element in the list will be a name. This is why you should be careful that you don’t miss the first name in the list, which is at index 0. Notice, too, that you can avoid the empty string at the end of the list by having

  \[ \text{index < lines.size() - 1} \]

  as the test in the while loop. If you don’t do this, the final

  \[ \text{lines.get(index + 1)} \]

  will cause an IndexOutOfBoundsException.

- Part (c) first finds the name that matches the parameter, and then builds a string out of the next two or three lines that comprise the address. Again, the empty string signals that the end of the address has been reached.

- The escape character string, "\n", inserts a line break into the string.
2. (a) public static int countA(WordSet s)  
   {  
       int count = 0;  
       while (count < s.size() &&  
               s.findkth(count + 1).substring(0, 1).equals("A"))  
           count++;  
       return count;  
   }  

   Alternatively,  
   public static int countA(WordSet s)  
   {  
       boolean done = false;  
       int count = 0;  
       while (count < s.size() && !done)  
       {  
           String nextWord = s.findkth(count + 1);  
           if (nextWord.substring(0, 1).equals("A"))  
               count++;  
           else  
               done = true;  
       }  
       return count;  
   }

(b) public static void removeA(WordSet s)  
   {  
       int numA = countA(s);  
       for (int i = 1; i <= numA; i++)  
           s.remove(s.findkth(1));  
   }  

   Alternatively,  
   public static void removeA(WordSet s)  
   {  
       while (s.size() != 0 &&  
               s.findkth(1).substring(0, 1).equals("A"))  
           s.remove(s.findkth(1));  
   }

(c) public static WordSet commonElements(WordSet s1, WordSet s2)  
   {  
       WordSet temp = new WordSet();  
       for (int i = 1; i <= s1.size(); i++)  
       {  
           String nextWord = s1.findkth(i);  
           if (s2.contains(nextWord))  
               temp.insert(nextWord);  
       }  
       return temp;  
   }
NOTE

- To test whether a word starts with "A", you must compare the first letter of word, that is, word.substring(0,1), with "A".
- In part (a), you must check that your solution works if s is empty. For the given algorithm, count < s.size() will fail and short circuit the test, which is desirable since s.findkth(1) will violate the precondition of findkth(k), namely that k cannot be greater than size().
- The parameter for s.findkth must be greater than 0. Hence the use of s.findkth(count+1) in part (a).
- For the first solution in part (b), you get a subtle intent error if your last step is s.remove(s.findkth(i)). Suppose that s is initially {"FLY", "ASK", "ANT"}. After the method call s.remove(s.findkth(1)), s will be {"FLY", "ASK"}. After the statement s.remove(s.findkth(2)), s will be {"ASK"}!! The point is that s is adjusted after each call to s.remove. The algorithm that works is this: If N is the number of words that start with "A", simply remove the first element in the list N times. Note that the alternative solution avoids the pitfall described by simply repeatedly removing the first element if it starts with 'A.' The alternative solution, however, has its own pitfall: The algorithm can fail if a test for s being empty isn’t done for each iteration of the while loop.
- Part (c) could also be accomplished by going through each element in s2 and checking if it’s included in s1.

3. (a) public void updateLocation(int newRow, int newCol)
   {
     loc = new Location(newRow, newCol);
   }
(b) public void sortAllRows()
   {
     for(Contestant[] row: contestants)
       sort(row);
   }
(c) public String findWinnerName()
   {
     sortAllRows();
     int max = contestants[0][0].getScore();
     String winner = contestants[0][0].getName();
     for(int k = 0; k < NUM_ROWS; k++)
     {
       Contestant c = contestants[k][CONTESTANTS_PER_ROW - 1];
       if (c.getScore() > max)
       {
         winner = c.getName();
         max = c.getScore();
       }
     }
     return winner;
   }
NOTE

- In part (a), since the Location class does not contain mutator methods to set a new row and new column, you need to use the constructor of Location to set those new values.
- Part (b) uses the Java feature that a two-dimensional array is an array of arrays. Thus, each row, which is an array of Contestant, can be sorted using the helper method sort.
- Part (c) uses the fact that after you sort all the rows of contestants, the winning contestant will be in the last column of the matrix of contestants. When you go through the loop, searching for a score that's higher than the current max, be sure to store the name that goes with that score!

4. (a) public class SnowyOwl extends Owl
{
    //Constructor
    public SnowyOwl()
    { super ("Snowy owl"); }

    //Returns type of food for this SnowyOwl
    public String getFood()
    {
        int num = (int)(Math.random()*3);
        if (num == 0)
            return "hare";
        else if (num == 1)
            return "lemming";
        else
            return "small bird";
    }
}

(b) public void allEat()
{
    for (Bird b: birdList)
        System.out.println(b.getName() + " " + b.getFood());
}

NOTE

- The Owl class inherits the abstract getFood method. Since the food type for an Owl depends on the type of Owl, the Owl class does not provide implementation code for getFood. This is the reason that the Owl class is an abstract class.
- In part (a), since SnowyOwl is a concrete (nonabstract) class, it must provide implementation code for getFood.
- In part (a), super must be used in the constructor because there is no direct access to the private instance variables of the Bird class.
- Note that the noise for Owl will always be "hoot". Thus, noise does not need to be provided as a parameter in the SnowyOwl constructor.
The statement `super(owlName, "hoot")` will use the superclass—namely `Bird`—constructor to automatically assign "hoot" as a SnowyOwl’s noise. Similarly, the SnowyOwl does not need any parameters in its constructor: using the superclass (Owl) constructor will automatically provide it with its name through the statement `super("Snowy owl")`.

- In part (b), polymorphism will determine which `getFood` method to print for the actual instance of each `Bird` in `birdList`. 
Answer Sheet: Practice Exam Three

1. A B C D E
2. A B C D E
3. A B C D E
4. A B C D E
5. A B C D E
6. A B C D E
7. A B C D E
8. A B C D E
9. A B C D E
10. A B C D E
11. A B C D E
12. A B C D E
13. A B C D E
14. A B C D E
15. A B C D E
16. A B C D E
17. A B C D E
18. A B C D E
19. A B C D E
20. A B C D E
21. A B C D E
22. A B C D E
23. A B C D E
24. A B C D E
25. A B C D E
26. A B C D E
27. A B C D E
28. A B C D E
29. A B C D E
30. A B C D E
31. A B C D E
32. A B C D E
33. A B C D E
34. A B C D E
35. A B C D E
36. A B C D E
37. A B C D E
38. A B C D E
39. A B C D E
40. A B C D E
How to Calculate Your (Approximate) AP Computer Science Score

Multiple Choice
Number correct (out of 40) = _______ \leftarrow \text{Multiple-Choice Score}

Free Response

\begin{align*}
\text{Question 1} & \quad \text{(out of 9)} \\
\text{Question 2} & \quad \text{(out of 9)} \\
\text{Question 3} & \quad \text{(out of 9)} \\
\text{Question 4} & \quad \text{(out of 9)} \\
\text{Total} & \quad \times \quad 1.11 \quad = \quad _______ \leftarrow \text{Free-Response Score} \\
\text{(Do not round.)}
\end{align*}

Final Score

\begin{align*}
\text{Multiple-Choice Score} + \text{Free-Response Score} & = \text{Final Score} \\
\text{(Round to nearest whole number.)}
\end{align*}

Chart to Convert to AP Grade

\begin{center}
\begin{tabular}{|c|c|}
\hline
Final Score Range & AP Grade$^a$ \\
\hline
62–80 & 5 \\
47–61 & 4 \\
37–46 & 3 \\
29–36 & 2 \\
0–28 & 1 \\
\hline
\end{tabular}
\end{center}

$^a$The score range corresponding to each grade varies from exam to exam and is approximate.
Practice Exam Three
COMPUTER SCIENCE
SECTION I

Time—1 hour and 15 minutes
Number of questions—40
Percent of total grade—50

Directions: Determine the answer to each of the following questions or incomplete statements, using the available space for any necessary scratchwork. Then decide which is the best of the choices given and fill in the corresponding oval on the answer sheet. Do not spend too much time on any one problem.

Notes:

• Assume that the classes in the Quick Reference have been imported where needed.
• Assume that variables and methods are declared within the context of an enclosing class.
• Assume that method calls that have no object or class name prefixed, and that are not shown within a complete class definition, appear within the context of an enclosing class.
• Assume that parameters in method calls are not null unless otherwise stated.

1. What output is produced by the following line of code?

   System.out.println("\"This is
very strange\" ");

   (A) \This is\nvery strange\n
   (B) "This is very strange"

   (C) This is
very strange

   (D) \"This is
very strange\"

   (E) "This is
very strange"

GO ON TO THE NEXT PAGE.
2. A certain class, SomeClass, contains a method with the following header:

   public int getValue(int n)

Suppose that methods with the following headers are now added to SomeClass:

   I public int getValue()
   II public double getValue(int n)
   III public int getValue(double n)

Which of the above headers will cause an error?
(A) None  
(B) I only  
(C) II only  
(D) III only  
(E) I and III only

3. Consider the following statement:

   int num = /* expression */;

Which of the following replacements for /* expression */ creates in num a random integer from 2 to 50, including 2 and 50?
(A) \(\text{(int)}(\text{Math.random()} \times 50) - 2\)  
(B) \(\text{(int)}(\text{Math.random()} \times 49) - 2\)  
(C) \(\text{(int)}(\text{Math.random()} \times 49) + 2\)  
(D) \(\text{(int)}(\text{Math.random()} \times 50) + 2\)  
(E) \(\text{(int)}(\text{Math.random()} \times 48) + 2\)

4. Consider the following code segment.

   int num = 0, score = 10;
   if (num != 0 && score / num > SOME_CONSTANT)
     statement1;
   else
     statement2;

What is the result of executing this statement?
(A) An ArithmeticException will be thrown.  
(B) A syntax error will occur.  
(C) statement1, but not statement2, will be executed.  
(D) statement2, but not statement1, will be executed.  
(E) Neither statement1 nor statement2 will be executed; control will pass to the first statement following the if statement.
5. The following shuffle algorithm is used to shuffle an array of int values, nums.

```java
public void shuffle ()
{
    for (int k = nums.length - 1; k > 0; k--)
    {
        int randPos = (int) (Math.random() * (k + 1));
        int temp = nums[k];
        nums[k] = nums[randPos];
        nums[randPos] = temp;
    }
}
```

Suppose the initial state of nums is 8, 7, 6, 5, 4, and when the method is executed the values generated for randPos are 3, 2, 0, 0, in that order. What element will be contained in nums[2] after execution?

(A) 8  
(B) 7  
(C) 6  
(D) 5  
(E) 4

6. Consider the following instance variables and method assignValues in the same class:

```java
private int numRows;
private int numCols;
private int[][] mat;

/** arr has numCols elements */
private void assignValues(int[] arr, int value)
{
    for (int k = 0; k < arr.length; k++)
        arr[k] = value;
}
```

Which of the following code segments will correctly assign mat to have the value 100 in each slot? You may assume that the instance variables have all been correctly initialized.

I for (int row = 0; row < numRows; row++)
    assignValues(mat[row], 100);

II for (int col = 0; col < numCols; col++)
    assignValues(mat[col], 100);

III for (int[] row: mat)
    for (int num: row)
        num = 100;

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) I and III only
7. Consider the following inheritance hierarchy.

```
    Cereal  <<abstract>>
      /       |
WheatCereal RiceCereal
```

Which of the following declarations will *not* cause an error? You may assume that each of the classes above has a default constructor.

I WheatCereal w = new Cereal();
II Cereal c1 = new Cereal();
III Cereal c2 = new RiceCereal();

(A) I only
(B) II only
(C) III only
(D) I and III only
(E) I, II, and III
Questions 8 and 9 refer to the following class definitions.

```java
public interface Class1
{ void method1(); }

public class Class2 implements Class1
{
    public void method1()
    { /* implementation not shown */ }

    //Private instance variables and other methods are not shown.
}

public class Class3 extends Class2
{
    public void method2(Class3 other)
    { /* implementation not shown */ }

    //Private instance variables and other methods are not shown.
}
```

8. Assuming that both Class2 and Class3 have default constructors, which is (are) valid in a client class?

I Class1 c1 = new Class2();
II Class2 c2 = new Class3();
III Class1 c3 = new Class3(); 

(A) I only 
(B) II only 
(C) III only 
(D) I and II only 
(E) I, II, and III

9. Consider the following declarations in a client class.

Class3 ob3 = new Class3();
Class2 ob2 = new Class2();

Which method calls would be legal?

I ob3.method1();
II ob2.method2(ob3);
III ob3.method2(ob2);

(A) I only 
(B) II only 
(C) III only 
(D) II and III only 
(E) I, II, and III
10. Refer to the following program segment.

```java
for (int n = 50; n > 0; n = n / 2)
    System.out.println(n);
```

How many lines of output will this segment produce?
(A) 50  
(B) 49  
(C) 7  
(D) 6  
(E) 5

11. Let list be an ArrayList<String> containing only these elements:

"John", "Mary", "Harry", "Luis"

Which of the following statements will cause an error to occur?

I list.set(2, "6");  
II list.add(4, "Pat");  
III String s = list.get(4);

(A) I only  
(B) II only  
(C) III only  
(D) II and III only  
(E) I, II, and III

12. Consider the following static method.

```java
public static int compute(int n) {
    for (int i = 1; i < 4; i++)
        n *= n;
    return n;
}
```

Which of the following could replace the body of `compute`, so that the new version returns the identical result as the original for all n?

(A) return 4 * n;  
(B) return 8 * n;  
(C) return 64 * n;  
(D) return (int) Math.pow(n, 4);  
(E) return (int) Math.pow(n, 8);
13. Consider the following instance variable and method.

```java
private int[] nums;

/** Precondition: nums contains int values in no particular order. */
public int getValue()
{
    for (int k = 0; k < nums.length; k++)
    {
        if (nums[k] % 2 != 0)
            return k;
    }
    return -1;
}
```

Suppose the following statement is executed:

```java
int j = getValue();
```

If the value returned in `j` is a positive integer, which of the following best describes the contents of `nums`?

(A) The only odd int in `nums` is at position `j`.
(B) All values in positions 0 through `j-1` are odd.
(C) All values in positions 0 through `j-1` are even.
(D) All values in positions `nums.length-1` down to `j+1` are odd.
(E) All values in positions `nums.length-1` down to `j+1` are even.

14. Consider the following method.

```java
public int mystery (int n)
{
    if (n == 0)
        return 0;
    else if (n % 2 == 1)
        return n;
    else
        return n + mystery(n - 1);
}
```

What will be returned by a call to `mystery(6)`?

(A) 6
(B) 11
(C) 12
(D) 27
(E) 30
15. Consider the following code segment.

```c
int num1 = value1, num2 = value2, num3 = value3;
while (num1 > num2 || num1 > num3)
{
    /* body of loop */
}
```

You may assume that value1, value2, and value3 are int values. Which of the following is sufficient to guarantee that /* body of loop */ will never be executed?

(A) There is no statement in /* body of loop */ that leads to termination
(B) num1 < num2
(C) num1 < num3
(D) num1 > num2 && num1 > num3
(E) num1 < num2 && num1 < num3
16. Consider the following two classes.

```java
public class Performer
{
    public void act()
    {
        System.out.print(" bow");
        perform();
    }

    public void perform()
    {
        System.out.print(" act");
    }
}

public class Singer extends Performer
{
    public void act()
    {
        System.out.print(" rise");
        super.act();
        System.out.print(" encore");
    }

    public void perform()
    {
        System.out.print(" aria");
    }
}
```

Suppose the following declaration appears in a class other than Performer or Singer:

```java
Performer p = new Singer();
```

What is printed as a result of the call `p.act()`?

(A) rise bow aria encore
(B) rise bow act encore
(C) rise bow act
(D) bow act aria
(E) bow aria encore
Use the program description below for Questions 17–19.

A car dealer needs a program that will maintain an inventory of cars on his lot. There are three types of cars: sedans, station wagons, and SUVs. The model, year, color, and price need to be recorded for each car, plus any additional features for the different types of cars. The program must allow the dealer to

- Add a new car to the lot.
- Remove a car from the lot.
- Correct any data that’s been entered.
- Display information for any car.

17. The programmer decides to have these classes: Car, Inventory, Sedan, SUV, and StationWagon. Which statement is true about the relationships between these classes and their attributes?

I. There are no inheritance relationships between these classes.
II. The Inventory class has-a list of Car objects.
III. The Sedan, StationWagon, and SUV classes are independent of each other.

(A) I only  
(B) II only  
(C) III only  
(D) I and II only  
(E) II and III only

18. Suppose that the programmer decides to have a Car class and an Inventory class. The Inventory class will maintain a list of all the cars on the lot. Here are some of the methods in the program:

```java
addCar         //adds a car to the lot
removeCar     //removes a car from the lot
displayCar    //displays all the features of a given car
setColor      //sets the color of a car to a given color
              //May be used to correct data
getPrice      //returns the price of a car
displayAllCars //displays features for every car on the lot
```

In each of the following, a class and a method are given. Which is the least suitable choice of class to be responsible for the given method?

(A) Car, setColor  
(B) Car, removeCar  
(C) Car, getPrice  
(D) Car, displayCar  
(E) Inventory, displayAllCars
19. Suppose Car is a superclass and Sedan, StationWagon, and SUV are subclasses of Car. Which of the following is the most likely method of the Car class to be overridden by at least one of the subclasses (Sedan, StationWagon, or SUV)?
   (A) setColor(newColor)  //sets color of Car to newColor
   (B) getModel()  //returns model of Car
   (C) displayCar()  //displays all features of Car
   (D) setPrice(newPrice)  //sets price of Car to newPrice
   (E) getYear()  //returns year of Car

20. Consider the following segment of code.

   String word = "conflagration";
   int x = word.indexOf("flag");
   String s = word.substring(0, x);

What will be the result of executing the above segment?
   (A) A syntax error will occur.
   (B) String s will be the empty string.
   (C) String s will contain "flag".
   (D) String s will contain "conf".
   (E) String s will contain "con".

21. Consider the following class declaration:

   public abstract class AClass
   {
     private int v1;
     private double v2;

     //methods of the class
     ...
   }

Which is true about AClass?
   (A) Any program using this class will have an error: An abstract class cannot contain private instance variables.
   (B) AClass must have a constructor with two parameters in order to initialize v1 and v2.
   (C) At least one method of AClass must be abstract.
   (D) A program that uses AClass must have another class that is a subclass of AClass.
   (E) In a program that uses AClass, more than one instance of AClass can be created.
22. A class of 30 students rated their computer science teacher on a scale of 1 to 10 (1 means awful and 10 means outstanding). The responses array is a 30-element integer array of the student responses. An 11-element array freq will count the number of occurrences of each response. For example, freq[6] will count the number of students who responded 6. The quantity freq[0] will not be used.

Here is a program that counts the students’ responses and outputs the results.

```java
public class StudentEvaluations {
    public static void main(String args[]) {
        int[] responses = {6, 6, 7, 8, 10, 1, 5, 4, 6, 7,
                           5, 4, 3, 4, 9, 8, 6, 7, 10,
                           6, 7, 8, 9, 6, 7, 8, 9, 2};
        int[] freq = new int[11];
        for (int i = 0; i < responses.length; i++)
            freq[responses[i]]++;
        // output results
        System.out.print("rating" + " frequency\n");
        for (int rating = 1; rating < freq.length; rating++)
            System.out.print(rating + " + freq[rating] + "\n");
    }
}
```

Suppose the last entry in the initializer list for the responses array was incorrectly typed as 12 instead of 2. What would be the result of running the program?

(A) A rating of 12 would be listed with a frequency of 1 in the output table.
(B) A rating of 1 would be listed with a frequency of 12 in the output table.
(C) An ArrayIndexOutOfBoundsException would be thrown.
(D) A StringIndexOutOfBoundsException would be thrown.
(E) A NullPointerException would be thrown.
Questions 23–25 are based on the three classes below:

```java
public class Employee {
    private String name;
    private int employeeNum;
    private double salary, taxWithheld;

    public Employee(String aName, int empNum, double aSalary, double aTax) {
        /* implementation not shown */
    }

    /** @return pre-tax salary */
    public double getSalary() {
        return salary;
    }

    public String getName() {
        return name;
    }

    public int getEmployeeNum() {
        return employeeNum;
    }

    public double getTax() {
        return taxWithheld;
    }

    public double computePay() {
        return salary - taxWithheld;
    }
}
```

```java
public class PartTimeEmployee extends Employee {
    private double payFraction;

    public PartTimeEmployee(String aName, int empNum, double aSalary, double aTax, double aPayFraction) {
        /* implementation not shown */
    }

    public double getPayFraction() {
        return payFraction;
    }

    public double computePay() {
        return getSalary() * payFraction - getTax();
    }
}
```

```java
public class Consultant extends Employee {
    private static final double BONUS = 5000;

    public Consultant(String aName, int empNum, double aSalary, double aTax) {
        /* implementation not shown */
    }

    public double computePay() {
        /* implementation code */
    }
}
```

GO ON TO THE NEXT PAGE.
23. The `computePay` method in the `Consultant` class redefines the `computePay` method of the `Employee` class to add a bonus to the salary after subtracting the tax withheld. Which represents correct /* implementation code */ of `computePay` for `Consultant`?

I return super.computePay() + BONUS;

II super.computePay();
   return getSalary() + BONUS;

III return getSalary() - getTax() + BONUS;

(A) I only  
(B) II only  
(C) III only  
(D) I and III only  
(E) I and II only

24. Consider these valid declarations in a client program:

```java
Employee e = new Employee("Noreen Rizvi", 304, 65000, 10000);
Employee p = new PartTimeEmployee("Rafael Frongillo", 287, 40000, 7000, 0.8);
Employee c = new Consultant("Dan Lepage", 694, 55000, 8500);
```

Which of the following method calls will cause an error?

(A) double x = e.computePay();
(B) double y = p.computePay();
(C) String n = c.getName();
(D) int num = p.getEmployeeNum();
(E) double g = p.getPayFraction();

GO ON TO THE NEXT PAGE.
25. Consider the `writePayInfo` method:

```java
/** Writes Employee name and pay on one line. */
public static void writePayInfo(Employee e)
{ System.out.println(e.getName() + " " + e.computePay()); }
```

The following piece of code invokes this method:

```java
Employee[] empList = new Employee[3];
empList[0] = new Employee("Lila Fontes", 1, 10000, 850);
empList[1] = new Consultant("Momo Liu", 2, 50000, 8000);
empList[2] = new PartTimeEmployee("Moses Wilks", 3, 25000, 3750, 0.6);
for (Employee e : empList)
   writePayInfo(e);
```

What will happen when this code is executed?

(A) A list of employees' names and corresponding pay will be written to the screen.
(B) A `NullPointerException` will be thrown.
(C) A `ClassCastException` will be thrown.
(D) A compile-time error will occur, with the message that the `getName` method is not in the `Consultant` class.
(E) A compile-time error will occur, with the message that an instance of an `Employee` object cannot be created.
26. Consider an array `arr` that is initialized with `int` values. The following code segment stores in `count` the number of positive values in `arr`.

   ```java
   int count = 0, index = 0;
   while (index < arr.length)
   {
       if (arr[index] > 0)
           count++;
       index++;
   }
   ```

Which of the following is equivalent to the above segment?

I int count = 0;
   for (int num : arr)
   {
       if (arr[num] > 0)
           count++;
   }

II int count = 0;
   for (int num : arr)
   {
       if (num > 0)
           count++;
   }

III int count = 0;
   for (int i = 0; i < arr.length; i++)
   {
       if (arr[i] > 0)
           count++;
   }

(A) I only  
(B) II only  
(C) III only  
(D) II and III only  
(E) I and III only
27. A square matrix is declared as

```java
int[][] mat = new int[SIZE][SIZE];
```

where `SIZE` is an appropriate integer constant. Consider the following method:

```java
public static void mystery(int[][] mat, int value, int top, int left,
                          int bottom, int right)
{
    for (int i = left; i <= right; i++)
    {
        mat[top][i] = value;
        mat[bottom][i] = value;
    }
    for (int i = top + 1; i <= bottom - 1; i++)
    {
        mat[i][left] = value;
        mat[i][right] = value;
    }
}
```

Assuming that there are no out-of-range errors, which best describes what method `mystery` does?

(A) Places value in corners of the rectangle with corners (top, left) and (bottom, right).

(B) Places value in the diagonals of the square with corners (top, left) and (bottom, right).

(C) Places value in each element of the rectangle with corners (top, left) and (bottom, right).

(D) Places value in each element of the border of the rectangle with corners (top, left) and (bottom, right).

(E) Places value in the topmost and bottommost rows of the rectangle with corners (top, left) and (bottom, right).

28. Which of the following statements about a class `SomeClass` that implements an interface is (are) true?

I It is illegal to create an instance of `SomeClass`.

II Any superclass of `SomeClass` must also implement that interface.

III `SomeClass` must implement every method of the interface.

(A) None

(B) I only

(C) II only

(D) III only

(E) II and III only

GO ON TO THE NEXT PAGE.
29. Assume that a Book class has a compareTo method where, if b1 and b2 are Book objects, b1.compareTo(b2) is a negative integer if b1 is less than b2, a positive integer if b1 is greater than b2, and 0 if b1 equals b2. The following method is intended to return the index of the “smallest” book, namely the book that would appear first in a sorted list of Book objects.

```java
/**
 * Precondition:
 * - books is initialized with Book objects.
 * - books.length > 0.
 */
public static int findMin(Book[] books)
{
    int minPos = 0;
    for (int index = 1; index < books.length; index++)
    {
        if ( /* condition */ )
        {
            minPos = index;
        }
    }
    return minPos;
}
```

Which of the following should be used to replace /* condition */ so that findMin works as intended?
(A) books[minPos] > books[index]
(B) books[index] > books[minPos]
(C) books[index].compareTo(books[minPos]) > 0
(D) books[index].compareTo(books[minPos]) >= 0
(E) books[index].compareTo(books[minPos]) < 0

30. Refer to the static method removeNegs shown below.

```java
/**
 * Precondition: list is an ArrayList<Integer>.
 * Postcondition: All negative values have been removed from list.
 * @param list the list of Integer objects
 */
public static void removeNegs(List<Integer> list)
{
    int index = 0;
    while (index < list.size())
    {
        if (list.get(index).intValue() < 0)
        {
            list.remove(index);
        }
        index++;
    }
}
```

For which of the following lists will the method not work as intended?
(A) 6 -1 -2 5
(B) -1 2 -3 4
(C) 2 4 6 8
(D) -3
(E) 1 2 3 -8
31. A sorted list of 120 integers is to be searched to determine whether the value 100 is in the list. Assuming that the most efficient searching algorithm is used, what is the maximum number of elements that must be examined?
   (A) 7
   (B) 8
   (C) 20
   (D) 100
   (E) 120

32. Consider a sorted array $arr$ of $n$ elements, where $n$ is large and $n$ is even. Under which conditions will a sequential search of $arr$ be faster than a binary search?
   I. The target is not in the list.
   II. The target is in the first position of the list.
   III. The target is in $arr[1 + n/2]$.
   (A) I only
   (B) II only
   (C) III only
   (D) I and III only
   (E) II and III only
33. Refer to the following data field and method.

```java
private int[] arr;

/** Precondition: arr.length > 0 and index < arr.length. */
public void remove(int index)
{
    int[] b = new int[arr.length - 1];
    int count = 0;
    for (int i = 0; i < arr.length; i++)
    {
        if (i != index)
        {
            b[count] = arr[i];
            count++;
        }
    }

    /* assertion */
    arr = b;
}
```

Which of the following assertions is true when the /* assertion */ line is reached during execution of remove?
(A) `b[k] == arr[k]` for `0 <= k < arr.length`.
(B) `b[k] == arr[k + 1]` for `0 <= k < arr.length`.
(C) `b[k] == arr[k]` for `0 <= k <= index` and `b[k] == arr[k + 1]` for `index < k < arr.length - 1`.
(D) `b[k] == arr[k]` for `0 <= k <= index` and `b[k] == arr[k + 1]` for `index <= k < arr.length - 1`.
(E) `b[k] == arr[k]` for `0 <= k < index` and `b[k] == arr[k + 1]` for `index <= k < arr.length`.

34. When an integer is represented in base 16 (hexadecimal), the digits 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F are used, where A–F represent the numbers 10–15. If base 16 is represented with the subscript `hex` and base 10 is represented with the subscript `dec`, then the decimal number 196 could be represented in hexadecimal as shown below:

```
196_{dec} = C4_{hex}
```

Which of the following is equal to `2AF_{hex}`?
(A) `27_{dec}`
(B) `300_{dec}`
(C) `687_{dec}`
(D) `4002_{dec}`
(E) `6896_{dec}`

GO ON TO THE NEXT PAGE.
Questions 35–37 refer to the TennisPlayer, GoodPlayer, and WeakPlayer classes below. These classes are to be used in a program to simulate a game of tennis.

```java
public abstract class TennisPlayer {
    private String name;

    public TennisPlayer(String aName) {
        name = aName;
    }

    public String getName() {
        return name;
    }

    public abstract boolean serve();
    public abstract boolean serviceReturn();
}

public class GoodPlayer extends TennisPlayer {
    public GoodPlayer(String aName) {
        /* implementation not shown */
    }

    /** @return true if serve is in (80% probability),
     * false if serve is out (20% probability)
     */
    public boolean serve() {
        /* implementation not shown */
    }

    /** @return true if service return is in (70% probability),
     * false if service return is out (30% probability)
     */
    public boolean serviceReturn() {
        /* implementation not shown */
    }
}

public class WeakPlayer extends TennisPlayer {
    public WeakPlayer(String aName) {
        /* implementation not shown */
    }

    /** @return true if serve is in (45% probability),
     * false if serve is out (55% probability)
     */
    public boolean serve() {
        /* implementation not shown */
    }

    /** @return true if service return is in (30% probability),
     * false if service return is out (70% probability)
     */
    public boolean serviceReturn() {
        /* implementation not shown */
    }
}
```

GO ON TO THE NEXT PAGE.
35. Which of the following declarations will cause an error? You may assume all the constructors are correctly implemented.
(A) TennisPlayer t = new TennisPlayer("Smith");
(B) TennisPlayer g = new GoodPlayer("Jones");
(C) TennisPlayer w = new WeakPlayer("Henry");
(D) TennisPlayer p = null;
(E) WeakPlayer q = new WeakPlayer("Grady");

36. Refer to the serve method in the WeakPlayer class:

```java
/** @return true if serve is in (45% probability), * false if serve is out (55% probability) */
public boolean serve()
{
 return /* implementation */
}
```

Which of the following replacements for /* implementation */ satisfy the post-condition of the serve method?

I double value = Math.random();
 return value >= 0 || value < 0.45;

II double value = Math.random();
 return value < 0.45;

III int val = (int) (Math.random() * 100);
 return val < 45;

(A) I only
(B) II only
(C) III only
(D) II and III only
(E) I, II, and III
37. Consider the following class definition:

```java
public class Beginner extends WeakPlayer {
    private double costOfLessons;

    // methods of Beginner class
    ...
}
```

Refer to the following declarations and method in a client program:

```java
TennisPlayer g = new GoodPlayer("Sam");
TennisPlayer w = new WeakPlayer("Harry");
TennisPlayer b = new Beginner("Dick");

public void giveEncouragement(WeakPlayer t) {
    /* implementation not shown */
}
```

Which of the following method calls will not cause an error?
(A) `giveEncouragement((WeakPlayer) g);`
(B) `giveEncouragement((WeakPlayer) b);`
(C) `giveEncouragement((Beginner) w);`
(D) `giveEncouragement(w);`
(E) `giveEncouragement(b);`
38. A matrix class that manipulates matrices contains the following declaration:

```java
private int[][] mat = new[numRows][numCols];
```

Consider the following method that alters matrix mat.

```java
public void doSomething()
{
    int width = mat[0].length;
    int numRows = mat.length;
    for (int row = 0; row < numRows; row++)
    {
        for (int col = 0; col < width/2; col++)
            mat[row][col] = mat[row][width - 1 - col];
    }
}
```

If mat has current value

```
1 2 3 4 5 6
1 3 5 7 9 11
```

what will the value of mat be after a call to doSomething?

(A) 1 2 3 3 2 1
    1 3 5 5 3 1
(B) 6 5 4 4 5 6
    11 9 7 7 9 11
(C) 6 5 4 3 2 1
    11 9 7 5 3 1
(D) 1 2 3 4 5 6
    1 2 3 4 5 6
(E) 1 3 5 7 9 11
    1 3 5 7 9 11
Questions 39 and 40 refer to the following information.

Consider an array arr that is sorted in increasing order, and method findMost given below. Method findMost is intended to find the value in the array that occurs most often. If every value occurs exactly once, findMost should return -1. If there is more than one value that occurs the most, findMost should return any one of those. For example, if arr contains the values [1,5,7,7,10], findMost should return 7. If arr contains [2,2,2,7,8,8,9,9,9], findMost should return 2 or 9. If arr contains [1,2,7,8], findMost should return -1.

```java
public static int findMost(int[] arr)
{
    int maxCountSoFar = 1;
    int mostSoFar = arr[0];
    int count = 1;
    int index = 0;
    while (index < arr.length - 1)
    {
        if (arr[index] == arr[index + 1])
        {
            count++;
            index++;
        }
        else
        {
            maxCountSoFar = count;
            mostSoFar = arr[index];
            count = 1;
        }
        index++;
    }
    return mostSoFar;
}
```

39. The method findMost does not always work as intended. An incorrect result will be returned if arr contains the values
   (A) [1,2,3,4,5]
   (B) [6,6,6,6]
   (C) [1,2,2,3,4,5]
   (D) [1,1,3,4,5,5,5,7]
   (E) [2,2,2,4,5,5]

40. Which of the following changes should be made so that method findMost will work as intended?
   (A) Insert the statement count = 1; between Lines 20 and 21.
   (B) Insert the statement count = 1; between Lines 21 and 22.
   (C) Insert the statement count = 1; between Lines 16 and 17.
   (D) Insert the statement count = 0; between Lines 23 and 24.
   (E) Insert the statement count = 1; between Lines 23 and 24.

END OF SECTION I
1. Consider the problem of keeping track of the available seats in a theater. Theater seats can be represented with a two-dimensional array of integers, where a value of 0 shows a seat is available, while a value of 1 indicates that the seat is occupied. For example, the array below shows the current seat availability for a show in a small theater.

```
[0] [0] [1] [1] [0] [1]
[0] [1] [0] [1] [0] [1]
[2] [1] [0] [0] [0] [0]
```

The seat at slot [1] [3] is taken, but seat [0] [4] is still available. A show can be represented by the `Show` class shown below.
public class Show
{
    /** The seats for this show */
    private int[][] seats;

    private final int SEATS_PER_ROW = <some integer value>;
    private final int NUM_ROWS = <some integer value>;

    /** Returns true if the seat with the specified row and seat
     * number is an aisle seat, false otherwise.
     * @param row the row number
     * @param seatNumber the seat number
     * @return true if an aisle seat, false otherwise */
    public boolean isAisleSeat (int row, int seatNumber)
    { /* to be implemented in part (a) */ }

    /** Reserve two adjacent seats and return true if this was
     * successfully done.
     * If two adjacent seats could not be found, leave the state
     * of the show unchanged, and return false.
     * @return true if two adjacent seats were found, false
     * otherwise */
    public boolean twoTogethers()
    { /* to be implemented in part (b) */ }

    /** Return the lowest seat number in the specified row for a
     * block of empty adjacent seats. If no such block exists,
     * return -1.
     * @param row the row number
     * @param seatsNeeded the number of adjacent empty seats needed
     * @return lowest seat number for a block of needed adjacent
     * seats or -1 if no such block exists */
    public int findAdjacent(int row, int seatsNeeded)
    { /* to be implemented in part (c) */ }

    //There may be instance variables, constructors, and methods
    //that are not shown.
}

(a) Write the Show method isAisleSeat, which should return true if the seat
with the specified row and seat number is an aisle seat, false otherwise.
Aisle seats are the first and the last columns of the two-dimensional array
representing the theater. For example, in the diagram shown above, if show
is a Show variable, here are some results of calling the isAisleSeat method.

<table>
<thead>
<tr>
<th>Method call</th>
<th>Return value</th>
</tr>
</thead>
<tbody>
<tr>
<td>show.isAisleSeat(2,5)</td>
<td>true</td>
</tr>
<tr>
<td>show.isAisleSeat(0,4)</td>
<td>false</td>
</tr>
<tr>
<td>show.isAisleSeat(1,0)</td>
<td>true</td>
</tr>
</tbody>
</table>

Complete method isAisleSeat below.
/** Returns true if the seat with the specified row and seat number is an aisle seat, false otherwise.
 * @param row the row number
 * @param seatNumber the seat number
 * @return true if an aisle seat, false otherwise */

public boolean isAisleSeat(int row, int seatNumber)

(b) Write the Show method twoTogether, which reserves two adjacent seats and returns true if this was successfully done. If it is not possible to find two adjacent seats that are unoccupied, the method should leave the show unchanged and return false. For example, suppose this is the state of a show.

```
[0] [1] [2] [3] [4] [5]
[0] 0 0 1 1 0 1
[1] 0 1 0 1 0 1
[2] 1 0 0 0 1 1
```

A call to twoTogether should return true, and the final state of the show could be any one of the following three configurations.

1. `OR`

```
[0] [1] [2] [3] [4] [5]
[0] 1 1 1 1 0 1
[1] 0 1 0 1 0 1
[2] 1 0 0 0 1 1
```

2. `OR`

```
[0] [1] [2] [3] [4] [5]
[0] 0 0 1 1 0 1
[1] 0 1 0 1 0 1
[2] 1 1 1 0 1 1
```

3. `OR`

```
[0] [1] [2] [3] [4] [5]
[0] 0 0 1 1 0 1
[1] 0 1 0 1 0 1
[2] 1 0 1 1 1 1
```

For the following state of a show, a call to twoTogether should return false and leave the two-dimensional array as shown.

```
[0] [1] [2] [3] [4] [5]
[0] 0 1 0 1 1 0
[1] 1 1 0 1 0 1
[2] 0 1 1 1 1 1
```
Information repeated from the beginning of the question

```java
public class Show
{
    private int[][] seats
    private final int SEATS_PER_ROW
    private final int NUM_ROWS
    public boolean isAisleSeat(int row, int seatNumber)
    public boolean twoTogether()
    public int findAdjacent(int row, int seatsNeeded)
}
```

Complete method `twoTogether` below.

```java
/** Reserve two adjacent seats and return true if this was
 * successfully done.
 * If two adjacent seats could not be found, leave the state
 * of the show unchanged, and return false.
 * @return true if two adjacent seats were found, false
 * otherwise */
public boolean twoTogether()
```

(c) Write the `Show` method `findAdjacent`, which finds the lowest seat number in the specified row for a block of empty adjacent seats. If no such block exists, the `findAdjacent` method should return -1. No changes should be made to the state of the show, irrespective of the value returned.

For example, suppose the diagram of seats is as shown.

```
[0] [1] [2] [3] [4] [5]
[0] 0 1 1 0 0 0
[1] 0 0 0 0 1 1
[2] 1 0 0 1 0 0
```

The following table shows some examples of calling `findAdjacent` for `show`.

<table>
<thead>
<tr>
<th>Method call</th>
<th>Return value</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>show.findAdjacent(0,3)</code></td>
<td>3</td>
</tr>
<tr>
<td><code>show.findAdjacent(1,3)</code></td>
<td>0 or 1</td>
</tr>
<tr>
<td><code>show.findAdjacent(2,2)</code></td>
<td>1 or 4</td>
</tr>
<tr>
<td><code>show.findAdjacent(1,5)</code></td>
<td>-1</td>
</tr>
</tbody>
</table>

Complete method `findAdjacent` below.

```java
/** Return the lowest seat number in the specified row for a
 * block of empty adjacent seats. If no such block exists,
 * return -1.
 * @param row the row number
 * @param seatsNeeded the number of adjacent empty seats needed
 * @return lowest seat number for a block of needed adjacent
 * seats or -1 if no such block exists */
public int findAdjacent(int row, int seatsNeeded)
```

GO ON TO THE NEXT PAGE.
2. A company sends a form letter to all of its potential customers. In order to personalize each letter, various tokens (symbols) in the form letter are replaced by either the customer’s name, city, or state, depending on the token. A customer can be represented by a `Customer` class, whose partial implementation is shown below.

```java
public class Customer {
    private String name;
    private String city;
    private String state;

    /** @return the name of this customer */
    public String getName() { return name; }

    /** @return the city of this customer */
    public String getCity() { return city; }

    /** @return the state of this customer */
    public String getState() { return state; }

    //Constructor and other methods are not shown.
}
```

A `FormLetter` object has a list of lines that make up the letter, and a list of customers who will receive the letter. In this question you will be asked to write two methods of the `FormLetter` class, whose partial implementation is shown below.

```java
public class FormLetter {

    /** The list of lines that make up this form letter */
    private List<String> lines;

    /** The list of customers */
    private List<Customer> customers;

    /** @return a copy of lines */
    public List<String> makeCopy() {
        List<String> newLines = new ArrayList<String>();
        for (String line: lines)
            newLines.add(line);
        return newLines;
    }
}
```

`GO ON TO THE NEXT PAGE.`
/** Replace all occurrences of sub in line with replacement string, repl.
 * @param line a String
 * @param sub a substring to be replaced
 * @param replacement the replacement string.
 * @Precondition: sub is not a substring of repl, the replacement string.
 * @return line with each occurrence of sub replaced by replacement */
public String replaceAll(String line, String sub, String repl)
{ /* to be implemented in part (a) */ }

/** Write letter for one customer, using personalized lines contained in customerLines.
 * @param customerLines the personalized lines for one customer */
public void writeLetter(List<String> customerLines)
{ /* implementation not shown */ }

/** Creates and prints a personalized form letter for each customer in the customers list.
 * @Postcondition: In each customer letter:
 * - every occurrence of "@" is replaced by the customer's name;
 * - every occurrence of "&" is replaced by the customer's city;
 * - every occurrence of "$" is replaced by the customer's state.
 * - A letter with the replacements is printed for each customer. */
public void createPersonalizedLetters()
{ /* to be implemented in part (b) */ }

//Constructors and other methods are not shown.
}

(a) Write the FormLetter method replaceAll, which examines a given string and replaces all occurrences of a specified substring with a replacement string. In writing your solution, you may not use the replace, replaceAll, or replaceFirst methods in the Java String class. Suppose f is a FormLetter. The following table shows the result of calling f.replaceAll(line,substring,replacement).

<table>
<thead>
<tr>
<th>line</th>
<th>substring</th>
<th>replacement</th>
<th>string returned</th>
</tr>
</thead>
<tbody>
<tr>
<td>oh me oh my</td>
<td>oh</td>
<td>aah</td>
<td>aah me aah my</td>
</tr>
<tr>
<td>sing to me a sin</td>
<td>sin</td>
<td>brin</td>
<td>bring to me a brin</td>
</tr>
<tr>
<td>ooh la la</td>
<td>ah</td>
<td>oh</td>
<td>ooh la la</td>
</tr>
</tbody>
</table>

GO ON TO THE NEXT PAGE.
Complete method `replaceAll` below.

```java
/** Replace all occurrences of sub in line with replacement
 * string, repl.
 * @param line a String
 * @param sub a substring to be replaced
 * @param replacement the replacement string
 * @pre sub is not a substring of repl,
 *      the replacement string.
 * @return line with each occurrence of sub replaced by replacement */
public String replaceAll(String line, String sub, String repl)
```

(b) Write the `FormLetter` method `createPersonalizedLetters`. For each customer in the customers list, method `createPersonalizedLetters` should create then print a letter that

- replaces all occurrences of `@` in `lines`, with the customer’s name
- replaces all occurrences of `&` in `lines`, with the customer’s city
- replaces all occurrences of `$` in `lines`, with the customer’s state

For example, suppose the first five lines in the form letter are:

```plaintext
Dear @,
If you buy a garden gnome you will
have the best-looking house in &,
heck, @, in the whole state of $!
@, @, @, don’t delay.
```

The letter generated for a customer Joan from Glendale, California, should have these replacement lines:

```plaintext
Dear Joan,
If you buy a garden gnome you will
have the best-looking house in Glendale,
heck, Joan, in the whole state of California!
Joan, Joan, Joan, don’t delay.
```

In writing method `createPersonalizedLetters`, you *must* use the method `replaceAll` that you wrote in part (a). Assume that `replaceAll` works as specified, regardless of what you wrote in part (a).

Complete method `createPersonalizedLetters` below.

```java
/** Creates and prints a personalized form letter for each
 * customer in the customers list.
 * @post In each customer letter:
 * - every occurrence of "@" is replaced by the customer’s name;
 * - every occurrence of "&" is replaced by the customer’s city;
 * - every occurrence of "$" is replaced by the customer’s state.
 * - A letter with the replacements is printed for each customer. */
public void createPersonalizedLetters()
```
3. A clothing store sells shoes, pants, and tops. The store also allows a customer to buy an “outfit,” which consists of three items: one pair of shoes, one pair of pants, and one top.

Each clothing item has a description and a price. The four types of clothing items are represented by the four classes Shoes, Pants, Top, and Outfit. All four classes implement the following ClothingItem interface.

```java
public interface ClothingItem {
    /** @return the description of the clothing item */
    String getDescription();

    /** @return the price of the clothing item */
    double getPrice();
}
```

The following diagram shows the relationship between the ClothingItem interface and the Shoes, Pants, Top, and Outfit classes.

```
ClothingItem <<<interface>>>
  
  Shoes  Pants  Top  Outfit
```

The store allows customers to create Outfit clothing items each of which includes a pair of shoes, pants, and a top. The description of the outfit consists of the description of the shoes, pants, and top, in that order, separated by "/" and followed by a space and "outfit". The price of an outfit is calculated as follows. If the sum of the prices of any two items equals or exceeds $100, there is a 25% discount on the sum of the prices of all three items. Otherwise there is a 10% discount.

For example, an outfit consisting of sneakers ($40), blue jeans ($50), and a T-shirt ($10), would have the name "sneakers/blue jeans/T-shirt outfit" and a price of $90.00. An outfit consisting of loafers ($50), cutoffs ($20), and dress-shirt ($60), would have the description "loafers/cutoffs/dress-shirt outfit" and price $97.50. Write the Outfit class that implements the ClothingItem interface. Your implementation must include a constructor that takes three parameters representing a pair of shoes, pants, and a top.

The code segment below should have the following behavior.

GO ON TO THE NEXT PAGE.
Shoes shoes;
Pants pants;
Top top;
/* Code to initialize shoes, pants, and top */

ClothingItem outfit =
    new Outfit (shoes, pants, top); //Compiles without error
ClothingItem outfit =
    new Outfit (pants, shoes, top); //Compile-time error
ClothingItem outfit =
    new Outfit (shoes, top, pants); //Compile-time error

Write your solution below.

4. A word creation game uses letter tiles, each of which has a letter and numerical value printed on it. A partial implementation of the Tile class is shown below.

    public class Tile
    {
        private String letter;
        private int value;

        /** @return the value on this Tile */
        public int getValue()
        { return value; }

        /** @return the letter on this Tile */
        public String getLetter()
        { return letter; }

        //Constructor and other methods are not shown.
    }

All tiles for the word game are called the tile set, which is represented by the TileSet class, whose partial implementation is shown below.
public class TileSet
{
    /** tiles contains all the tiles in the word game,
     * both used and not-yet-used. */
    private List<Tile> tiles;

    /** unusedSize is the number of tiles that are not yet used. */
    private int unusedSize;

    /** Determines if there are still unused tiles.
      * @return true if all the tiles have been used; false otherwise */
    public boolean allUsed()
    { return unusedSize == 0; }

    /** @return the number of unused tiles in this tile set */
    public int getUnusedSize()
    { return unusedSize; }

    /** Shuffles the tiles in the tile set, and
       * resets unusedSize to the total number of tiles in the set. */
    public void shuffle()
    { /* to be implemented in part (a) */ }

    /** Get an unused tile from this tile set.
       * @return an unused tile, or null if all tiles have been used */
    public Tile getNewTile()
    { /* implementation not shown */ }

    //Constructors and other methods are not shown.
}

(a) Write the shuffle method for the TileSet class. Your method should use the following algorithm.

for k starting at the end of the tiles list and going down to 1:
    pick a random index in 0, 1, 2, ..., k
    swap the tiles at position index and position k
    Reset unusedSize to the number of tiles in the tile set.

Complete method shuffle below.

/** Shuffles the tiles in the tile set, and resets
  * unusedSize to the total number of tiles in the set. */
public void shuffle()
For parts (b) and (c) you will write methods from the Player class, whose partial implementation is shown below. A player in the word game has NUM_LETTERS tiles in front of her. After she makes a word, she helps herself to unused tiles to maintain NUM_LETTERS tiles, if possible.

```java
public class Player {
    /** NUM_LETTERS is the number of letter tiles a player should have (if tiles have not yet all been used) at the start of her turn. */
    public static final int NUM_LETTERS = <some integer>;

    /** playerTiles is the list of tiles for this player. */
    private List<Tile> playerTiles;

    /** Adds a sufficient number of unused tiles from tileSet t to playerTiles so that this player has NUM_LETTERS tiles.
     * If there are insufficient unused tiles, the player should take all of the remaining available tiles.
     * Precondition: playerTiles.size() < NUM_LETTERS.
     * Postcondition: playerTiles.size() <= NUM_LETTERS.
     * @param t the tile set for the word game
     */
    public void replaceTiles(TileSet t) {
        /* to be implemented in part (b) */
    }

    /** Returns the score a player receives for using tiles from his playerTiles at his turn. The score is the sum of values on each tile used. Indexes of tiles used are contained in the indexes array. If index[0] is -1, the player has used no tiles at his turn and the method returns a score of 0. If the player uses all of the tiles in playerTiles, a bonus of 20 points is added to his score.
     * @param indexes the array of positions of tiles in playerTiles that the player uses at his turn
     * Precondition:
     * - playerTiles contains NUM_LETTERS tiles.
     * - indexes[0 .. n] is sorted in increasing order, n < NUM_LETTERS.
     */
    public int getWordScore(int[] indexes) {
        /* to be implemented in part (c) */
    }
}
```

(b) Write the Player method replaceTiles. This method should, if possible, add unused tiles to the player’s playerTiles list, until playerTiles contains NUM_LETTERS tiles. If there are insufficient unused tiles in the tile set, the player should take all of the remaining tiles.
Complete method replaceTiles below.

```java
/** Adds a sufficient number of unused tiles from tileSet t
 * to playerTiles so that this player has NUM_LETTERS tiles.
 * If there are insufficient unused tiles, the player should
 * take all of the remaining available tiles.
 * Precondition: playerTiles.size() < NUM_LETTERS.
 * Postcondition: playerTiles.size() <= NUM_LETTERS.
 * @param t the tile set for the word game
 */
public void replaceTiles(TileSet t)
```

(c) Write the Player method getWordScore. This method returns the total of the values of tiles in playerTiles whose positions are indicated in the indexes parameter. If indexes contains \{0, 1, 4\}, this means that the player will use the tiles at positions 0, 1, and 4 in his playerTiles list at his turn, and his score will be the sum of values of those tiles. If the player uses all of his tiles at his turn, a bonus of 20 points is added to his score. If the only value in the indexes array is -1, this means that the player passes at his turn, and getWordScore should return a value of 0.

For example, suppose NUM_LETTERS is 5, and playerTiles has the following state before the method call.

```
0 1 2 3 4
| "O" | "C" | "V" | "E" | "N"
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3</td>
<td>4</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>
```

State of indexes array | Result of getWordScore(indexes)
------------------------|------------------------
\{0,2,3,4\}             | 7                      
\{0,1,2,3,4\}           | 30                     
\{0,1,4\}               | 5                      
\{-1\}                  | 0                      

Complete method getWordScore below.

```java
/** Returns the score a player receives for using tiles from
 * his playerTiles at his turn. The score is the sum of values
 * on each tile used. Indexes of tiles used are contained in
 * the indexes array. If index[0] is -1, the player
 * has used no tiles at his turn and the method returns a
 * score of 0. If the player uses all of the tiles in
 * playerTiles, a bonus of 20 points is added to his score.
 * @param indexes the array of positions of tiles in
 * playerTiles that the player uses at his turn
 * @param playerTiles contains NUM_LETTERS tiles.
 * @param indexes[0 .. n] is sorted in increasing order,
 * n < NUM_LETTERS.
 */
public int getWordScore(int[] indexes)
```

END OF EXAMINATION
ANSWER KEY (Section I)

2. C  16. A  30. A
3. C  17. E  31. A
5. A  19. C  33. D
6. A  20. E  34. C
7. C  21. D  35. A
13. C  27. D
14. B  28. A

ANSWERS EXPLAINED

Section I

1. (E) The string parameter in the line of code uses two escape characters: \n, which means print a newline character (i.e., go to the next line).
\", which means print a double quote.

2. (C) The intent of the programmer is to have overloaded getValue methods in SomeClass. Overloaded methods have different signatures, where the signature of a method includes the name and parameter types only. Thus, the signature of the original method is getValue(int). The signature in header I is getValue(). The signature in header II is getValue(int). The signature in header III is getValue(double). Since the signature in header II is the same as that of the given method, the compiler will flag it and say that the method already exists in SomeClass. Note: The return type of a method is not included in its signature.

3. (C) The expression (int) (Math.random() * 49) produces a random integer from 0 through 48. (Note that 49 is the number of possibilities for num.) To shift this range from 2 to 50, add 2 to the expression.

4. (D) Short-circuit evaluation of the boolean expression will occur. The expression (num != 0) will evaluate to false, which makes the entire boolean expression false. Therefore the expression (score/num > SOME_CONSTANT) will not be evaluated. Hence no division by zero will occur, and there will be no ArithmeticException thrown. When the boolean expression has a value of false, only the else part of the statement, statement2, will be executed.
5. (A) The values of \( k \) are, consecutively, 4, 3, 2, and 1. The values of \( \text{randPos} \) are, consecutively, 3, 2, 0, and 0. Thus, the sequence of swaps and corresponding states of \( \text{nums} \) will be:

\[
\begin{align*}
\text{swap nums}[4] \text{ and nums}[3] & \quad 8 \ 7 \ 6 \ 4 \ 5 \\
\text{swap nums}[3] \text{ and nums}[2] & \quad 8 \ 7 \ 4 \ 6 \ 5 \\
\text{swap nums}[2] \text{ and nums}[0] & \quad 4 \ 7 \ 8 \ 6 \ 5 \\
\text{swap nums}[1] \text{ and nums}[0] & \quad 7 \ 4 \ 8 \ 6 \ 5 \\
\end{align*}
\]

Thus, the element in \( \text{nums}[2] \) is 8.

6. (A) A matrix is stored as an array of arrays, that is, each row is an array. Therefore it is correct to call a method with an array parameter for each row, as is done in Segment I. Segment II fails because \( \text{mat} \) is not an array of columns. The segment would cause an error, since \( \text{mat}[\text{col}] \) refers to a row, not a column. (If the number of rows were less than the number of columns, the method would throw an \( \text{ArrayIndexOutOfBoundsException} \). If the number of rows were greater than the number of columns, the method would correctly assign the value 100 to the first \( n \) rows, where \( n \) is the number of columns. The rest of the rows would retain the values before execution of the method.) Segment III fails because you cannot assign new elements in a for-each loop. The matrix remains unchanged.

7. (C) Declarations I and II fail because you can't create an instance of an abstract class. Additionally, declaration I fails this test: \( \text{Cereal is-a WheatCereal?} \) No. Notice that declaration III passes this test: \( \text{RiceCereal is-a Cereal?} \) Yes.

8. (E) All satisfy the \( \text{is-a test! Class2 is-a Class1. Class3 is-a Class2. Class3 is-a Class1.} \) Note: Since \( \text{Class3} \) is a subclass of \( \text{Class2} \), it automatically implements any interfaces implemented by \( \text{Class2} \), its superclass.

9. (A) Method call I works because \( \text{Class3} \) inherits all the methods of \( \text{Class2} \). Method call II fails because \( \text{Class2} \), the superclass, does not inherit the methods of \( \text{Class3} \), its subclass. Method call III uses a parameter that fails the \( \text{is-a test: ob2 is not a Class3} \), which the parameter requires.

10. (D) After each execution of the loop body, \( n \) is divided by 2. Thus, the loop will produce output when \( n \) is 50, 25, 12, 6, 3, and 1. The final value of \( n \) will be 1/2, which is 0, and the test will fail.

11. (C) Statement III will cause an \( \text{IndexOutOfBoundsException} \) because there is no slot 4. The final element, "Luis", is in slot 3. Statement I is correct: It replaces the string "Harry" with the string "6". It may look peculiar in the list, but the syntax is correct. Statement II looks like it may be out of range because there is no slot 4. It is correct, however, because you must be allowed to add an element to the end of the list.

12. (E) The effect of the given algorithm is to raise \( n \) to the 8th power.

When \( i = 1 \), the result is \( n \times n = n^2 \).
When \( i = 2 \), the result is \( n^2 \times n^2 = n^4 \).
When \( i = 3 \), the result is \( n^4 \times n^4 = n^8 \).

13. (C) The method traverses \( \text{nums} \), starting at position 0, and returns the current position the first time it finds an odd value. This implies that all values in positions 0 through the current index – 1 contained even numbers.

14. (B) Since \( n \) == 6 fails the two base case tests, method call \( \text{mystery(6)} \) returns \( 6 + \text{mystery(5)} \). Since 5 satisfies the second base case test, \( \text{mystery(5)} \) returns 5, and there are no more recursive calls. Thus, \( \text{mystery(6)} = 6 + 5 = 11 \).
15. (E) In order for /* body of loop */ not to be executed, the test must be false the first time it is evaluated. A compound OR test will be false if and only if both pieces of the test are false. Thus, choices B and C are insufficient. Choice D fails because it guarantees that both pieces of the test will be true. Choice A is wrong because /* body of loop */ may be executed many times, until the computer runs out of memory (an infinite loop!).

16. (A) When p.act() is called, the act method of Singer is executed. This is an example of polymorphism. The first line prints rise. Then super.act() goes to the act method of Performer, the superclass. This prints bow, then calls perform(). Again, using polymorphism, the perform method in Singer is called, which prints aria. Now, completing the act method of Singer, encore is printed. The result?

```
rise bow aria encore
```

17. (E) Statement I is false: The Sedan, StationWagon, and SUV classes should all be subclasses of Car. Each one satisfies the is_a Car relationship. Statement II is true: The main task of the Inventory class should be to keep an updated list of Car objects. Statement III is true: A class is independent of another class if it does not require that class to implement its methods.

18. (B) The Inventory class is responsible for maintaining the list of all cars on the lot. Therefore methods like addCar, removeCar, and displayAllCars must be the responsibility of this class. The Car class should contain the setColor, getPrice, and displayCar methods, since all these pertain to the attributes of a given Car.

19. (C) Each subclass may contain additional attributes for the particular type of car that are not in the Car superclass. Since displayCar displays all features of a given car, this method should be overridden to display the original plus additional features.

20. (E) The expression word.indexOf("flag") returns the index of the first occurrence of "flag" in the calling string, word. Thus, x has value 3. (Recall that the first character in word is at index 0.) The method call word.substring(0, x) is equivalent to word.substring(0, 3), which returns the substring in word from 0 to 2, namely "con". The character at index 3 is not included.

21. (D) A program that uses an abstract class must have at least one subclass that is not abstract, since instances of abstract classes cannot be created. Thus, choice E is false. Choice A is false: An abstract class can contain any number of private instance variables. Choice B is wrong—for example v1 and v2 could be initialized in a default constructor (constructor with no parameters). Choice C is incorrect: The point of an abstract class is that no instances of it will be created. The class does not need to contain any abstract methods.

22. (C) If the responses array contained an invalid value like 12, the program would attempt to add 1 to freq[12]. This is out of bounds for the freq array.

23. (D) Implementation I calls super.computePay(), which is equivalent to the computePay method in the Employee superclass. The method returns the quantity (salary - taxWithheld). The BONUS is then correctly added to this expression, as required. Implementation III correctly uses the public accessor methods getSalary and getTax that the Consultant class has inherited. Note that the Consultant class does not have direct access to the private instance variables salary and taxWithheld. Implementation II incorrectly returns the salary plus
BONUS—there is no tax withheld. The expression super.computePay() returns a value equal to salary minus tax. But this is neither stored nor included in the return statement.

24. (E) Note that p is declared to be of type Employee, and the Employee class does not have a getPayFraction method. To avoid the error, p must be cast to PartTimeEmployee as follows:

```java
double g = ((PartTimeEmployee) p).getPayFraction();
```

25. (A) The code does exactly what it looks like it should. The writePayInfo parameter is of type Employee and each element of the empList array is a Employee and therefore does not need to be downcast to its actual instance type. There is no ClassCastException (choice C) since nowhere is there an attempt made to cast an object to a class of which it is not an instance. None of the array elements is null; therefore, there is no NullPointerException (choice B). Choice D won’t happen because the getName method is inherited by both the Consultant and PartTimeEmployee classes. Choice E would occur if the Employee superclass were abstract, but it’s not.

26. (D) Segment I is incorrect because num is not an index in the loop. It is a value in the array. Thus, the correct test is if (num > 0), which is correctly used in segment II. Segment III is a regular for loop, exactly equivalent to the given while loop.

27. (D) The first for loop places value in the top and bottom rows of the defined rectangle. The second for loop fills in the remaining border elements on the sides. Note that the top + 1 and bottom - 1 initializer and terminating conditions avoid filling in the corner elements twice.

28. (A) Statement I is false: An interface may not be instantiated, but a class that implements the interface can be instantiated, provided it is not an abstract class. Statement II is false: Any subclass of SomeClass will automatically implement the interface, but not necessarily the superclass. For example, suppose a superclass Animal has a subclass Bird. And suppose Bird implements CanFly, which is an interface with a single method, fly. Clearly, Animal shouldn’t implement CanFly—not all animals fly. Statement III appears to be true: This is what it means for a class to implement an interface—it’s a promise that the class will contain all methods of that interface. This is not true, however, if SomeClass is an abstract class. Any method of the interface that is not implemented in SomeClass then automatically becomes an abstract method of SomeClass and must be implemented by any nonabstract subclass of SomeClass.

29. (E) Eliminate choices A and B: When comparing Book objects, you cannot use simple inequality operators; you must use compareTo. For the calling object to be less than the parameter object, use the less than 0 test (a good way to remember this!)

30. (A) Method removeNags will not work whenever there are consecutive negative values in the list. This is because removal of an element from an ArrayList causes the elements to the right of it to be shifted left to fill the “hole.” The index in the given algorithm, however, always moves one slot to the right. Therefore in choice A, when -1 is removed, -2 will be passed over, and the final list will be 6 -2 5.
31. (A) If the list is sorted, a binary search is the most efficient algorithm to use. Binary search chops the current part of the array being examined in half, until you have found the element you are searching for, or there are no elements left to look at. In the worst case, you will need to divide by 2 seven times:

\[
\begin{align*}
120/2 & \to 60 \\
60/2 & \to 30 \\
30/2 & \to 15 \\
15/2 & \to 7 \\
7/2 & \to 3 \\
3/2 & \to 1 \\
1/2 & \to 0
\end{align*}
\]

32. (B) For a sequential search, all \(n\) elements will need to be examined. For a binary search, the array will be chopped in half a maximum of \(\log_2 n\) times. When the target is in the first position of the list, a sequential search will find it in the first comparison. The binary search, which examines a middle element first, will not. Condition I is a worst case situation for both the sequential search and binary search. Condition III is approximately the middle of the list, but it won’t be found on the first try of the binary search. (The first try examines \(\text{arr}[n/2]\).) Still, the target will be located within fewer than \(\log n\) tries, whereas the sequential search will need more than \(n/2\) tries.

33. (D) The `remove` method removes from `arr` the element `arr[index]`. It does this by copying all elements from `arr[0]` up to but not including `arr[index]` into array `b`. Thus, `b[k] == arr[k]` for \(0 \leq k < \text{index}\) is true. Then it copies all elements from `arr[index + 1]` up to and including `arr[arr.length - 1]` into `b`. Since no gaps are left in `b`, `b[k] == arr[k + 1]` for `\text{index} \leq k < \text{arr.length} - 1`. The best way to see this is with a small example. If `arr` is 2, 6, 4, 8, 1, 7, and the element at `index` 2 (namely the 4) is to be removed, here is the picture:

\[
\begin{align*}
\text{arr} & \quad \to \quad \begin{bmatrix} 2 & 6 & 4 & 8 & 1 & 7 \end{bmatrix} \\
\text{b} & \quad \to \quad \begin{bmatrix} 2 & 6 & 8 & 1 & 7 \end{bmatrix}
\end{align*}
\]

\[
\begin{align*}
b[0] & = \text{arr}[0] \\
b[1] & = \text{arr}[1] \\
b[4] & = \text{arr}[5]
\end{align*}
\]

Notice that `arr.length` is 6, but \(k\) ends at 4.

34. (C) 

\[
2AF_{\text{hex}} = (F)(16^0) + (A)(16^1) + (2)(16^2)
\]

\[
= 15 + 10(16) + (2)(256)
\]

\[
= 15 + 160 + 512
\]

\[
= 687_{\text{dec}}
\]

35. (A) Choice A is illegal because you cannot create an instance of an abstract class.
36. (D) The statement

```java
double value = Math.random();
```

generates a random double in the range \(0 \leq \text{value} < 1\). Since random doubles are uniformly distributed in this interval, 45 percent of the time you can expect \text{value} to be in the range \(0 \leq \text{value} < 0.45\). Therefore, a test for \text{value} in this range can be a test for whether the serve of a WeakPlayer went in. Since Math.random() never returns a negative number, the test in implementation II, \text{value} < 0.45, is sufficient. The test in implementation I would be correct if \text{value} were changed to \&\& ("or" changed to "and"—both parts must be true). Implementation III also works. The expression

```
(int) (Math.random() * 100)
```

returns a random integer from 0 to 99, each equally likely. Thus, 45 percent of the time, the integer \text{val} will be in the range \(0 \leq \text{val} \leq 44\). Therefore, a test for \text{val} in this range can be used to test whether the serve was in.

37. (B) Choice B is fine: \text{b}, the Beginner, isa WeakPlayer. Choices A and C will each cause a ClassCastException to be thrown: You can't cast a GoodPlayer to a WeakPlayer, and you can't cast a WeakPlayer to a Beginner. Choices D and E will each cause a compile-time error: The parameter must be of type WeakPlayer, but \text{a} and \text{b} are declared to be of type TennisPlayer. Each of these choices can be corrected by casting the parameter to WeakPlayer.

38. (B) The method copies the elements from columns 3, 4, and 5 into columns 2, 1, and 0, respectively, as if there were a vertical mirror down the middle of the matrix. To see this, here are the values for the given matrix: \text{width} = 6, \text{width}/2 = 3, \text{numRows} = 2. The variable \text{row} goes from 0 to 1 and \text{column} goes from 0 to 2. The element assignments are

```java
mat[0][0] = mat[0][5]
mat[0][1] = mat[0][4]
mat[0][2] = mat[0][3]
mat[1][0] = mat[1][5]
mat[1][1] = mat[1][4]
mat[1][2] = mat[1][3]
```

39. (E) In choice E, findMost returns the value 5. This is because \text{count} has not been reset to 1, so that when 5 is encountered, the test \text{count} > \text{maxCountSoFar} is true, causing \text{mostSoFar} to be incorrectly re-assigned to 5. In choices A, B, and C, the outer while loop is not entered again, since a second run of equal values doesn't exist in the array. So \text{mostSoFar} comes out with the correct value. In choice D, when the outer loop is entered again, the test \text{count} > \text{maxCountSoFar} just happens to be true anyway and the correct value is returned. The algorithm fails whenever a new string of equal values is found whose length is shorter than a previous string of equal values.

40. (B) The \text{count} variable must be reset to 1 as soon as \text{index} is incremented in the outer while loop, so that when a new run of equal values is found, \text{count} starts out as 1.
Section II

1. (a) public boolean isAisleSeat(int row, int seatNumber)
   {
       return seatNumber == 0 || seatNumber == SEATS_PER_ROW - 1;
   }

(b) public boolean twoTogether()
   {
       for (int r = 0; r < NUM_ROWS; r++)
           for (int c = 0; c < SEATS_PER_ROW-1; c++)
               if (seats[r][c] == 0 && seats[r][c+1] == 0)
                   seats[r][c] = 1;
                   seats[r][c+1] = 1;
                   return true;
       return false;
   }

(c) public int findAdjacent(int row, int seatsNeeded)
   {
       int index = 0, count = 0, lowIndex = 0;
       while (index < SEATS_PER_ROW)
       {
           while (index < SEATS_PER_ROW && seats[row][index] == 0)
           {
               count++; index++;
               if (count == seatsNeeded)
                   return lowIndex;
           }
           count = 0; index++;
           lowIndex = index;
       }
       return -1;
   }

NOTE

• In part (a), the seat numbers go from 0 to SEATS_PER_ROW - 1.
• In part (b), you need the test c < SEATS_PER_ROW-1, because when you refer to seats[r][c+1], you must worry about going off the end of the row and causing an ArrayIndexOutOfBoundsException exception.
• In part (c), every time you increment index, you need to test that it is in range. This is why you need this test twice: index < SEATS_PER ROW.
• In part (c), every time you reset the count, you need to reset the lowIndex, because this is the value you’re asked to return.
• In parts (b) and (c), the final return statements are executed only if all rows in the show have been examined unsuccessfully.
2. (a) public String replaceAll(String line, String sub, String repl)
    {
        int pos = line.indexOf(sub);
        while (pos >= 0)
        {
            line = line.substring(0, pos) + repl +
            line.substring(pos + sub.length());
            pos = line.indexOf(sub);
        }
        return line;
    }
(b) public void createPersonalizedLetters()
    {
        for (int i = 0; i < customers.size(); i++)
        {
            List<String> tempLines = makeCopy();
            Customer c = customers.get(i);
            for (int j = 0; j < tempLines.size(); j++)
            {
                tempLines.set(j,
                    replaceAll(tempLines.get(j), "@", c.getName()));
                tempLines.set(j,
                    replaceAll(tempLines.get(j), "&", c.getCity()));
                tempLines.set(j,
                    replaceAll(tempLines.get(j), "$", c.getState()));
            }
            writeLetter(tempLines);
        }
    }

NOTE

- In part (a), each time you encounter sub in line, you simply create a new line that concatenates the “before” substring, the replacement, and the “after” substring. This guarantees termination of the loop: Eventually sub won’t be found in line because all occurrences have been replaced, and line.indexOf(sub) will return -1 (sub not found in line).
- In part (b), you need a nested loop: for each customer, loop through all the lines and do the replacements.
- In part (b), one of the tricky lines of code is

        List<String> tempLines = makeCopy();

You need a fresh, unchanged copy of lines for each customer. If, by mistake, you use the line

        List<String> tempLines = lines;

then tempLines and lines will be the same reference, so any changes to tempLines will also be made to lines, and the second (and all subsequent) customers won’t have a fresh copy of lines with the tokens. Instead, lines will contain the first customer’s information.
3. public class Outfit implements ClothingItem {
    private Shoes shoes;
    private Pants pants;
    private Top top;

    public Outfit (Shoes aShoes, Pants aPants, Top aTop) {
        shoes = aShoes;
        pants = aPants;
        top = aTop;
    }

    public String getDescription() {
        return shoes.getDescription() + "/" + pants.getDescription() + "/" + top.getDescription() + " outfit";
    }

    public double getPrice() {
        if (shoes.getPrice() + pants.getPrice() >= 100
            || shoes.getPrice() + top.getPrice() >= 100
            || top.getPrice() + pants.getPrice() >= 100)
            return 0.75 * (shoes.getPrice() + pants.getPrice() + top.getPrice());
        else
            return 0.90 * (shoes.getPrice() + pants.getPrice() + top.getPrice());
    }
}

NOTE
• To access the price and descriptions of items that make up an outfit, your
  class needs to have variables of type Shoes, Pants, and Top.

4. (a) public void shuffle() {
    for (int k = tiles.size() - 1; k > 0; k--)
    {
        int randIndex = (int) (Math.random() * (k + 1));
        Tile temp = tiles.get(k);
        tiles.set(k, tiles.get(randIndex));
        tiles.set(randIndex, temp);
    }
    unusedSize = tiles.size();
}
(b) public void replaceTiles(TileSet t) {
    int numTiles = NUM_LETTERS - playerTiles.size();
    if (numTiles <= t.getUnusedSize()) {
        for (int i = 1; i <= numTiles; i++)
            playerTiles.add(t.getNewTile());
    } else {
        for (int i = 1; i <= t.getUnusedSize(); i++)
            playerTiles.add(t.getNewTile());
    }
}

Alternatively

while (NUM_LETTERS > playerTiles.size() && !t.allUsed())
    playerTiles.add(t.getNewTile());

(c) public int getWordScore(int[] indexes) {
    if (indexes[0] == -1)
        return 0;
    int total = 0;
    if (indexes.length == NUM_LETTERS)
        total += 20;
    for (int i = 0; i < indexes.length; i++)
        total += playerTiles.get(indexes[i]).getValue();
    return total;
}

NOTE

• In part (a), the line
  
  int randIndex = (int) (Math.random() * (k + 1));

  returns a random integer in the range 0, 1, 2, ..., k.

• In part (b), there are two things to check:
  1. How many new tiles does the player need?
  2. Are there enough unused tiles available?

• In part (c), notice that indexes[i] are the positions of the tiles whose scores you need to access.
Appendix: Glossary of Useful Computer Terms

I hate definitions.
—Benjamin Disraeli, Vivian Grey (1826)

API library: Applications Program Interface library. A library of classes for use in other programs. The library provides standard interfaces that hide the details of the implementations.

Applet: A graphical Java program that runs in a web browser or applet viewer.

Application: A stand-alone Java program stored in and executed on the user’s local computer.

Binary number system: Base 2.

Bit: From “binary digit.” Smallest unit of computer memory, taking on only two values, 0 or 1.

Buffer: A temporary storage location of limited size. Holds values waiting to be used.

Byte: Eight bits. Similarly, megabyte (MB, \(10^6\) bytes) and gigabyte (GB, \(10^9\) bytes).

Bytecode: Portable (machine-independent) code, intermediate between source code and machine language. It is produced by the Java compiler and interpreted (executed) by the Java Virtual Machine.

Cache: A small amount of “fast” memory for the storage of data. Typically, the most recently accessed data from disk storage or “slow” memory is saved in the main memory cache to save time if it’s retrieved again.

Compiler: A program that translates source code into object code (machine language).

CPU: The central processing unit (computer’s brain). It controls the interpretation and execution of instructions. It consists of the arithmetic/logic unit, the control unit, and some memory, usually called “on-board memory” or cache memory. Physically, the CPU consists of millions of microscopic transistors on a chip.

Debugger: A program that helps find errors by tracing the values of variables in a program.

Decimal number system: Base 10.

GUI: Graphical user interface.

Hardware: The physical components of computers. These are the ones you can touch, for example, the keyboard, monitor, printer, CPU chip.
**Hertz (Hz):** One cycle per second. It refers to the speed of the computer’s internal clock and gives a measure of the CPU speed. Similarly, megahertz (MHz, $10^6$ Hz) and gigahertz (GHz, $10^9$ Hz).

**Hexadecimal number system:** Base 16.

**High-level language:** A human-readable programming language that enables instructions that require many machine steps to be coded concisely, for example, Java, C++, Pascal, BASIC, FORTRAN.

**HTML:** Hypertext Markup Language. The instructions read by web browsers to format web pages, link to other websites, and so on.

**IDE:** Integrated Development Environment. Provides tools such as an editor, compiler, and debugger that work together, usually with a graphical interface. Used for creating software in a high-level language.

**Interpreter:** A program that reads instructions that are not in machine language and executes them one at a time.

**Javadoc:** A program that extracts comments from Java source files and produces documentation files in HTML. These files can then be viewed with a web browser.

**JavaScript:** (Not to be confused with Java, the programming language.) A dynamic programming language most commonly used as part of web browsers.

**JVM (Java Virtual Machine):** An interpreter that reads and executes Java bytecode on any local machine.

**Linker:** A program that links together the different modules of a program into a single executable program after they have been compiled into object code.

**Low-level language:** Assembly language. This is a human-readable version of machine language, where each machine instruction is coded as one statement. It is translated into machine language by a program called an assembler. Each different kind of CPU has its own assembly language.

**Mainframe computer:** A large computer, typically used by large institutions, such as government agencies and big businesses.

**Malware:** (Short for malicious software.) Any software designed to disrupt computer operation or gain access to private computer systems. For example, viruses, spyware, etc.

**Microcomputer:** Personal computer.

**Minicomputer:** Small mainframe.

**Modem:** A device that connects a computer to a phone line or TV cable.

**Network:** Several computers linked together so that they can communicate with each other and share resources.

**Object code:** Machine language. Produced by compiling source code.

**Octal number system:** Base 8.

**Operating system:** A program that controls access to and manipulation of the various files and programs on the computer. It also provides the interface for user interaction with the computer. Some examples: Windows, MacOS, and Linux.
Appendix: Glossary of Useful Computer Terms

Primary memory: RAM. This gets erased when you turn off your computer.

RAM: Random Access Memory. This stores the current program and the software to run it.

ROM: Read Only Memory. This is permanent and nonerasable. It contains, for example, programs that boot up the operating system and check various components of the hardware. In particular, ROM contains the BIOS (Basic Input Output System)—a program that handles low-level communication with the keyboard, disk drives, and so on.

SDK: Sun's Java Software Development Kit. A set of tools for developing Java software.

Secondary memory: Hard drive, disk, magnetic tapes, CD-ROM, and so on.

Server: The hub of a network of computers. Stores application programs, data, mail messages, and so on, and makes them available to all computers on the network.

Software: Computer programs written in some computer language and executed on the hardware after conversion to machine language. If you can install it on your hard drive, it’s software (e.g., programs, spreadsheets, word processors).

Source code: A program in a high-level language like Java, C++, Pascal, or FORTRAN.

Swing: A Java toolkit for implementing graphical user interfaces.

Transistor: Microscopic semiconductor device that can serve as an on-off switch.


USB flash drive: A removable and rewritable device that fits into a USB port of a computer.

Virus: A computer program that can replicate itself and spread from one computer to another. A form of malware.

Workstation: Desktop computer that is faster and more powerful than a microcomputer.
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